

IRAFS-22. INTERNATIONAL SYMPOSIUM ON «SCIENCE & THEOLOGY»
PUL, October 20-21, 2022

Looking for **Quantum Gravity imprints in the Universe**



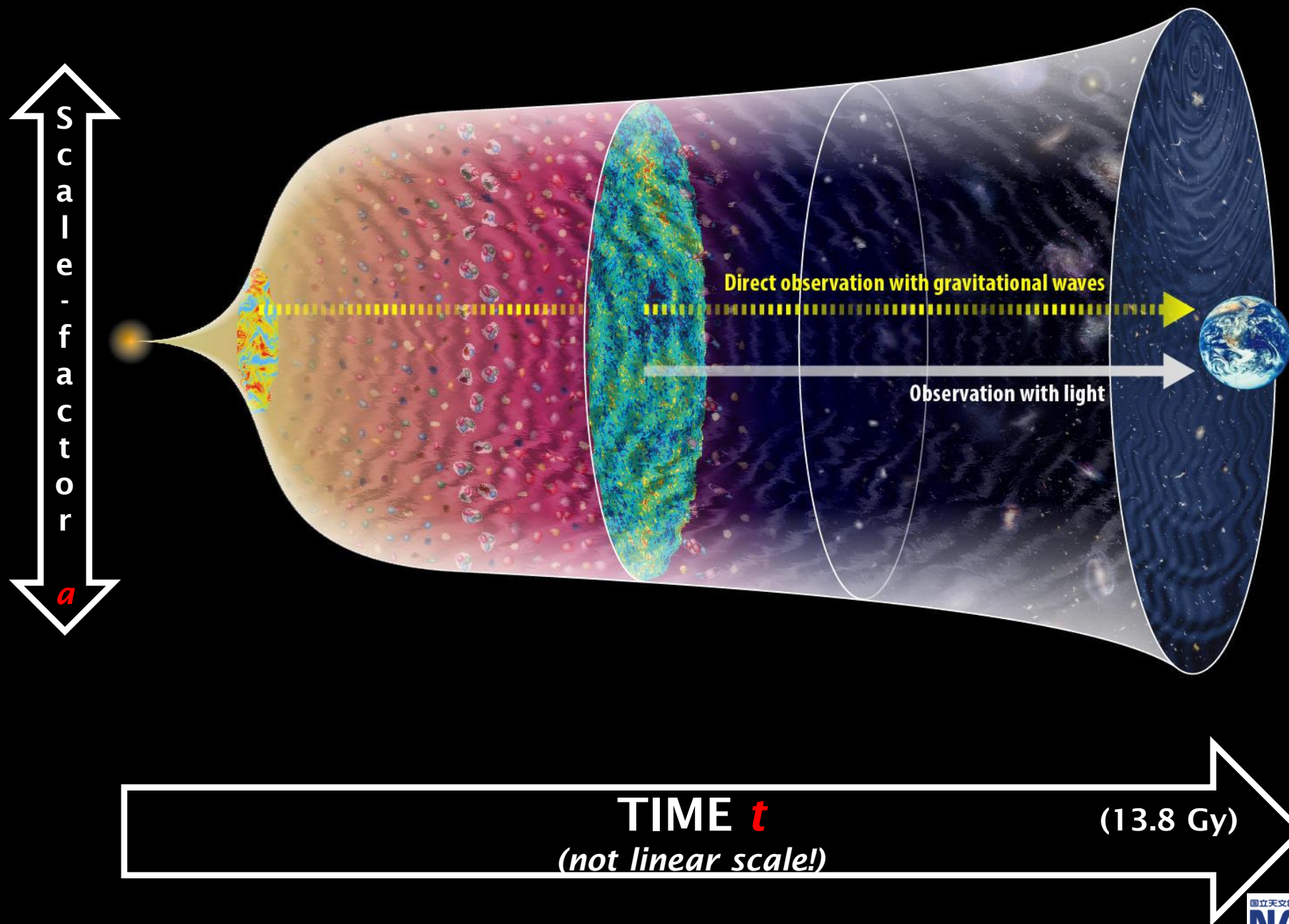
**Vatican
Observatory**



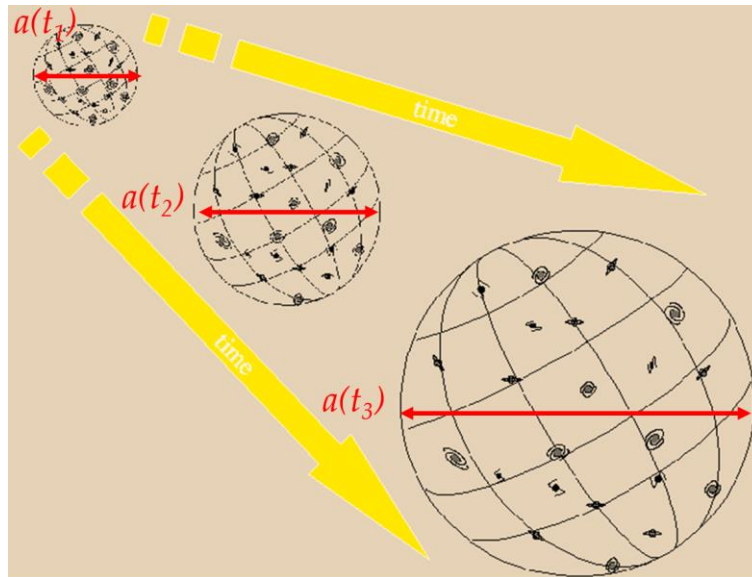
Matteo Galaverni

Looking for Quantum Gravity imprints in the Universe

- Brief “history” of the universe
- Gravitational waves
- Cosmic Microwave Background Radiation (Temperature & Polarization)
- Conclusions



Universe expansion

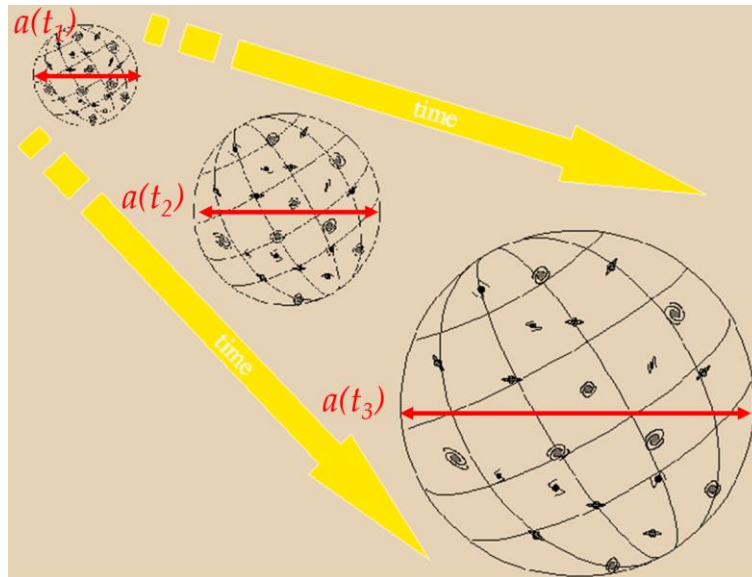


$$ds^2 = a^2(t)(dx^2 + dy^2 + dz^2)$$

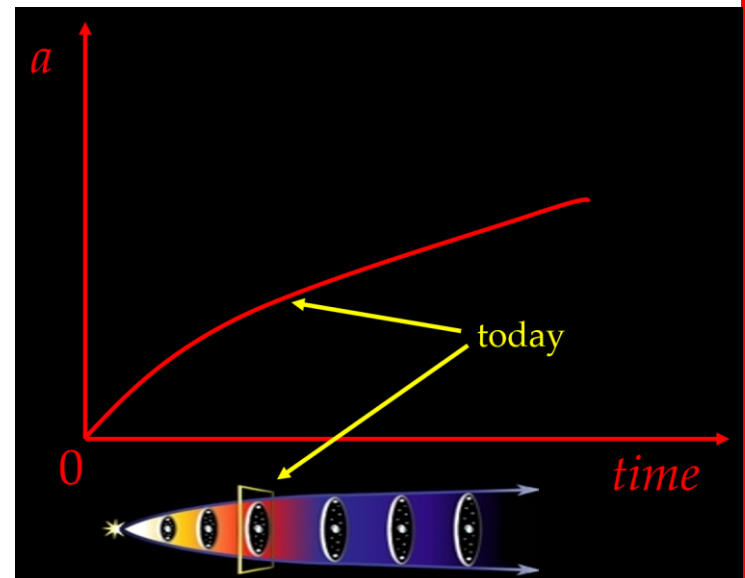
Scale factor

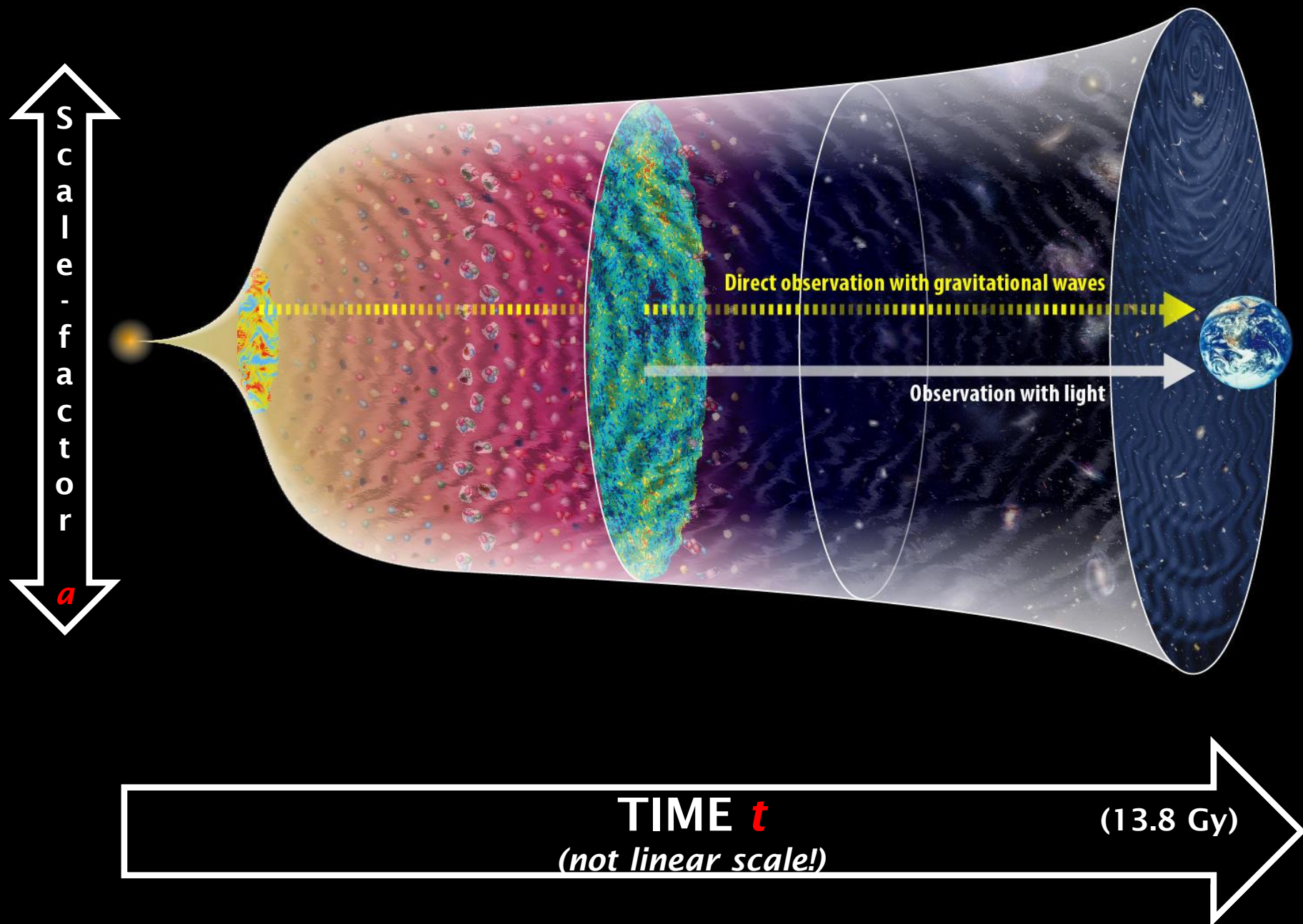
a

Universe expansion



$$ds^2 = a^2(t)(dx^2 + dy^2 + dz^2)$$





Time-scale defined using the fundamental constants of Gravity and Quantum Mechanics

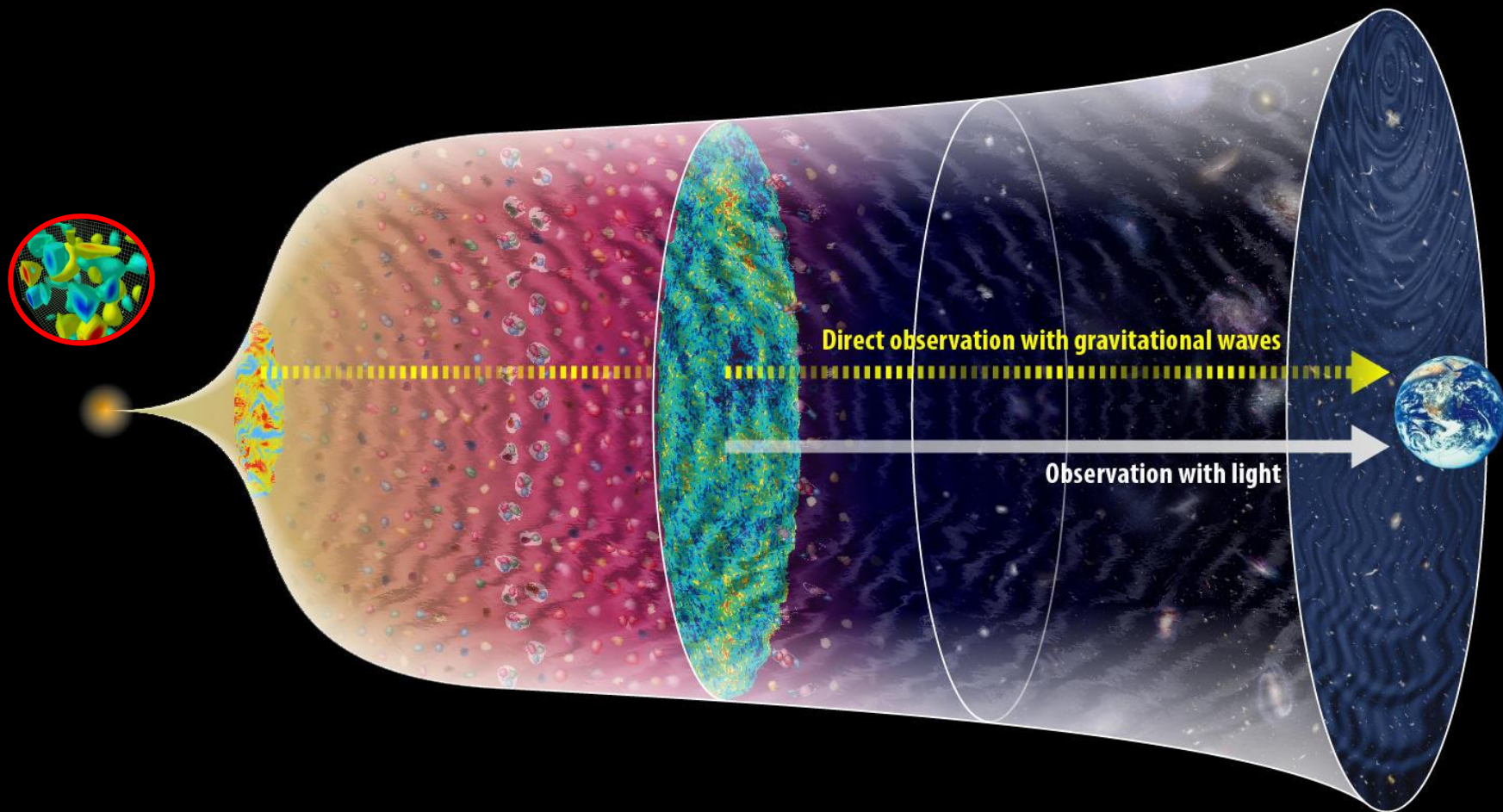
(Gravitational constant $G = 6,674 \times 10^{-11} \text{ m}^3 \text{ kg}^{-1} \text{ s}^{-2}$

Planck constant $\hbar = 1,055 \times 10^{-34} \text{ m}^2 \text{ kg s}^{-1}$

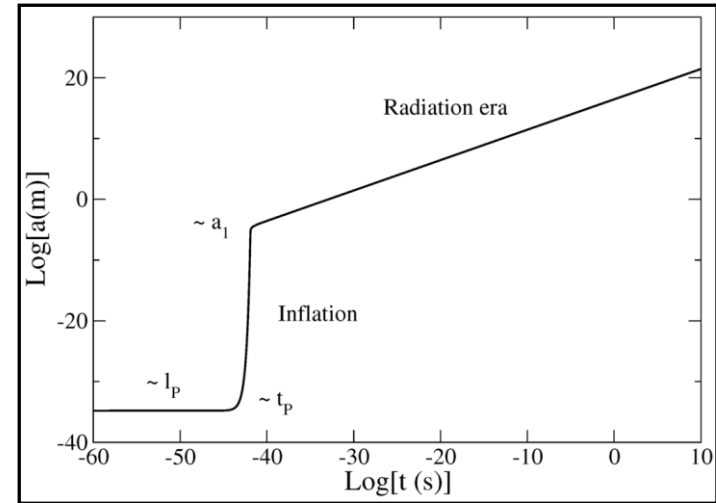
Speed of light $c = 2,997 \times 10^8 \text{ m s}^{-1}$):

$$t_p = \sqrt{\frac{G\hbar}{c^5}}$$
$$= 5.391 \times 10^{-44} \text{ seconds}$$

→ At Planck's Time Quantum Gravity is needed!



Cosmic inflation: the universe underwent a phase of **exponential expansion** that sets up its very special initial conditions



Quantum vacuum fluctuations during inflation turn out to play an important role. They give the initial condition for all the structures in the Universe.

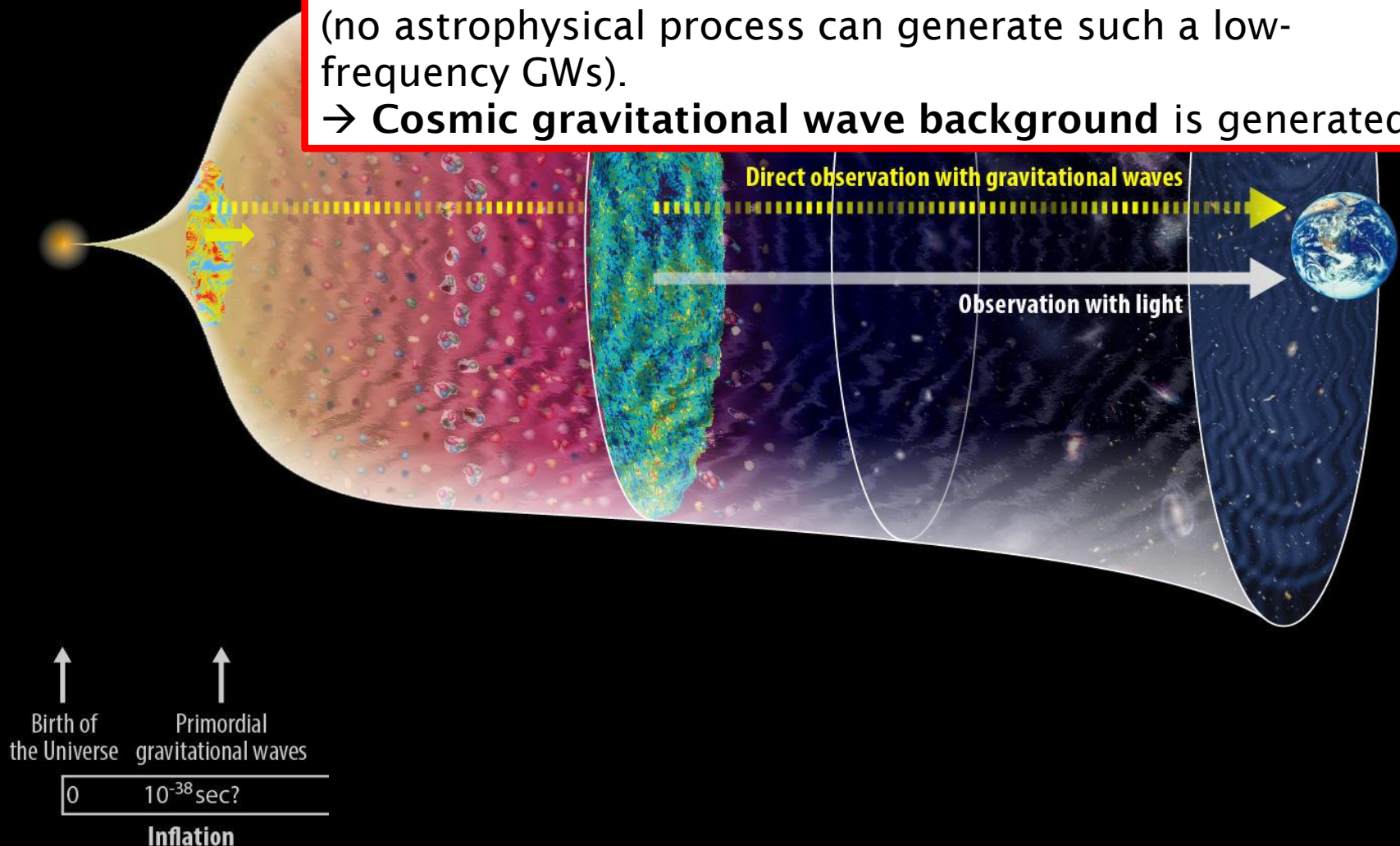
-A **microscopic wavelength** of quantum fluctuations is stretched by enormous expansion of space to become a **macroscopic** one.

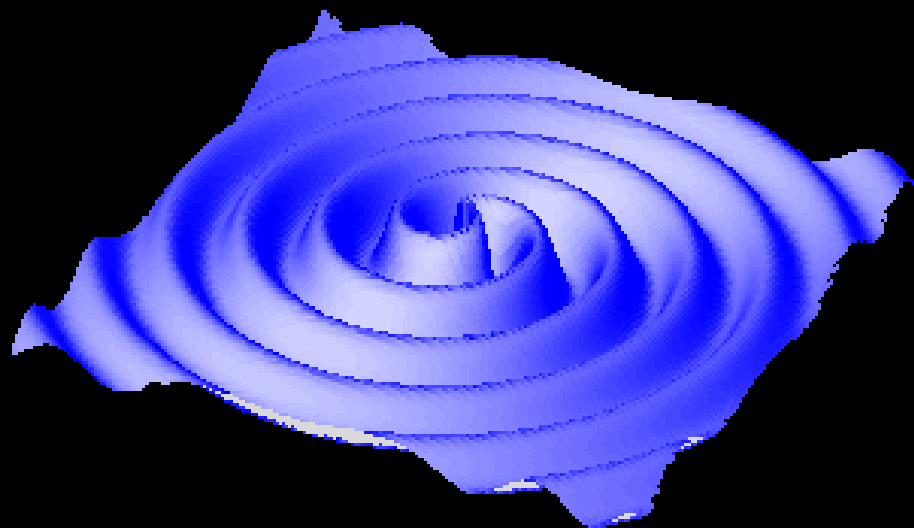
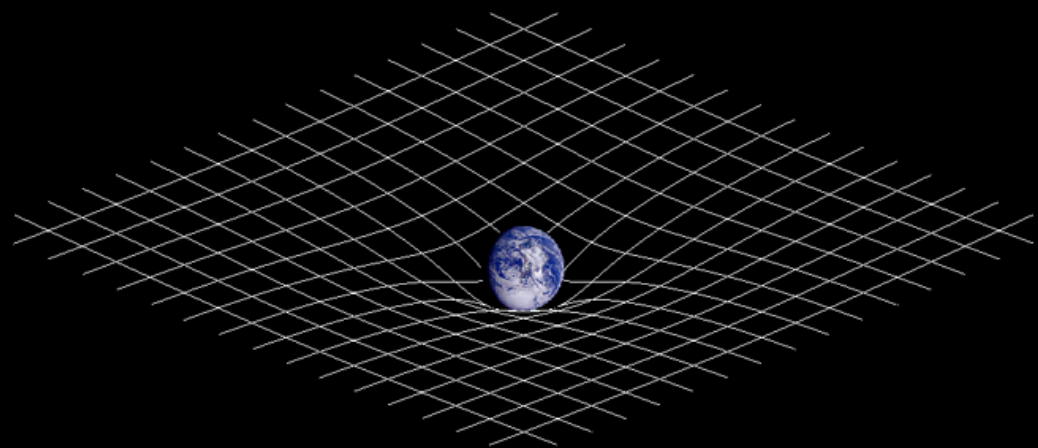
-The **origin of cosmic structures** is explained by a combination of quantum mechanics and general relativity.

The simplest model of inflation (single energy component driving exponential inflation) predicts a **stochastic background of gravitational waves**

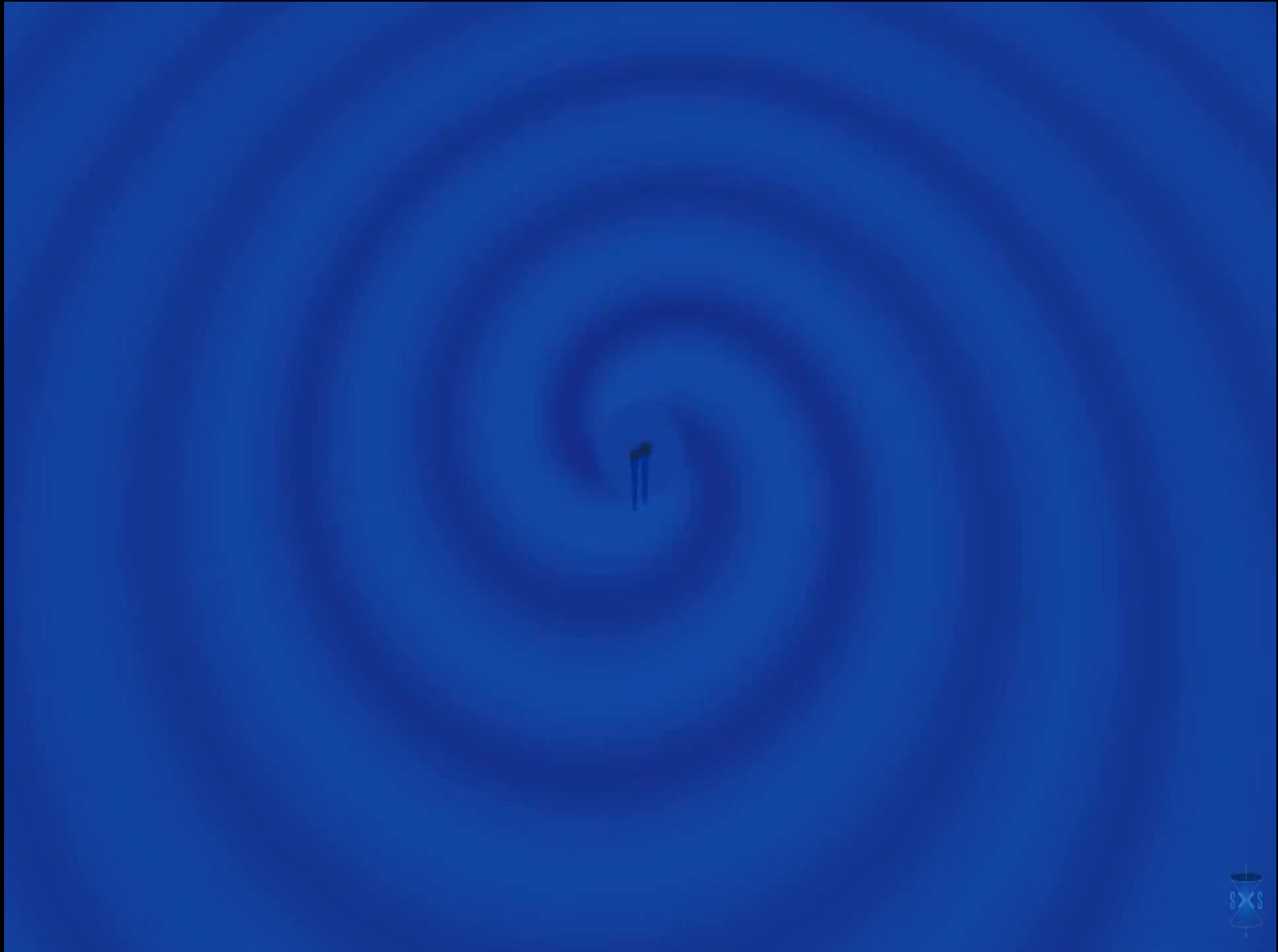
(no astrophysical process can generate such a low-frequency GWs).

→ **Cosmic gravitational wave background is generated.**





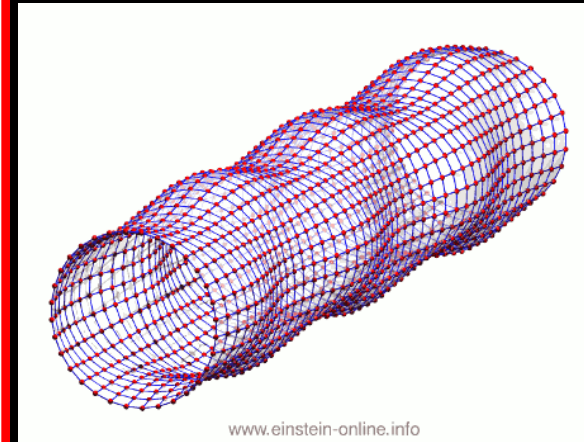
A computer **simulation of gravitational waves from merging black holes** [Simulating eXtreme Spacetimes (SXS) project]



If we consider a plane gravitational wave propagating in one direction:

- the gravitational wave shall be transverse (the direction of distortion is perpendicular to the propagation direction).
- the gravitational wave shall not change the area.

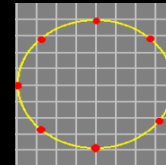
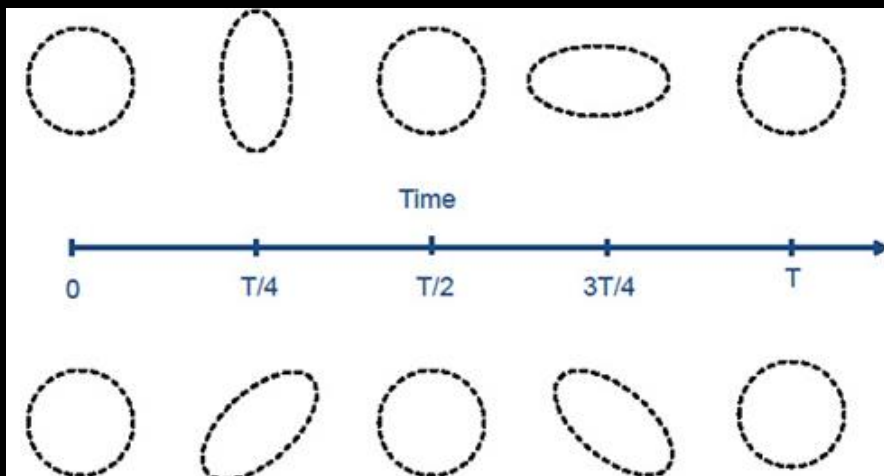
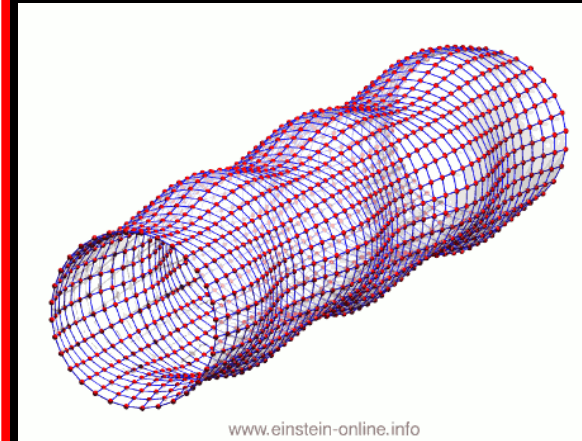
→ There are two degrees of freedom



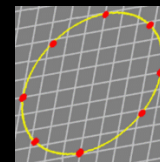
If we consider a plane gravitational wave propagating in one direction:

- the gravitational wave shall be transverse (the direction of distortion is perpendicular to the propagation direction).
- the gravitational wave shall not change the area.

→ There are two degrees of freedom



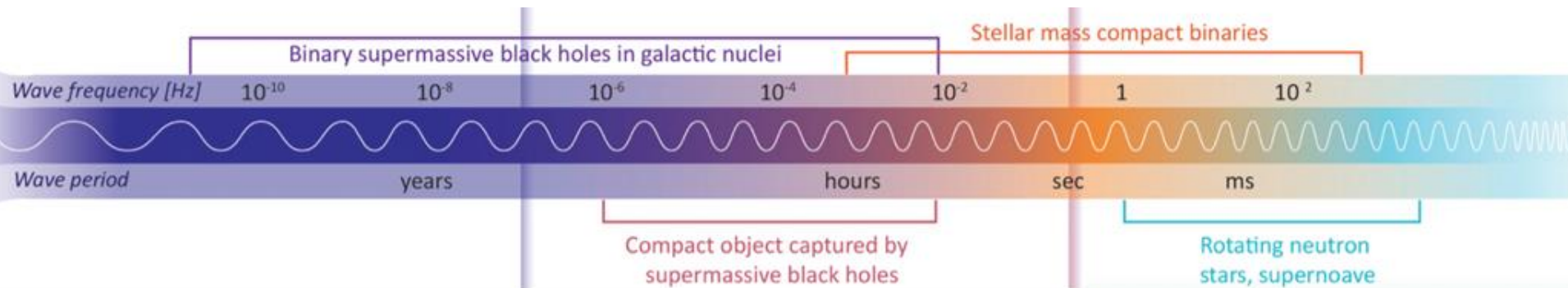
h_+ polarization



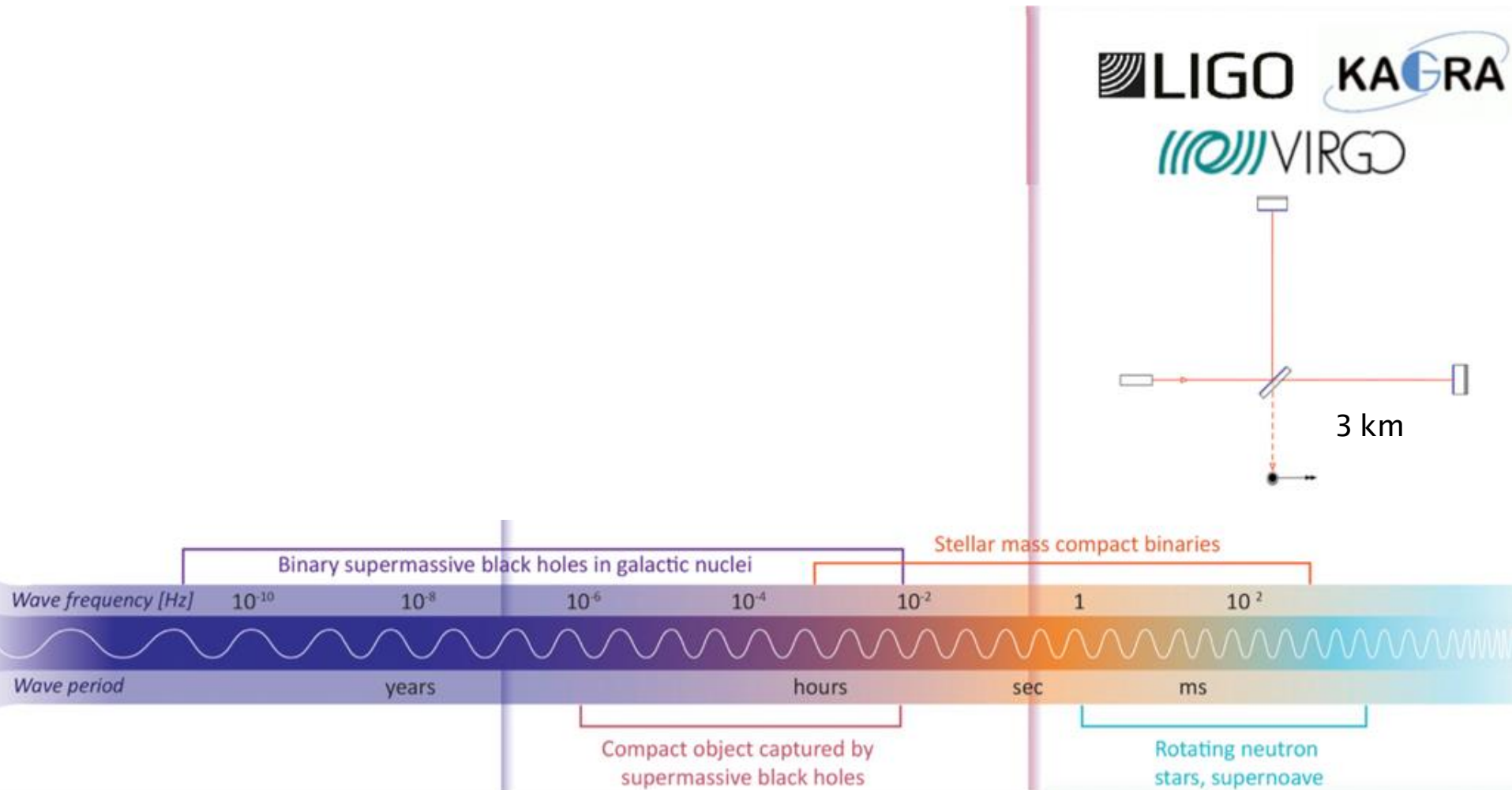
h_x polarization

$$h_{\mu\nu}^{\text{TT}}(t, z) = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & h_+ & h_\times & 0 \\ 0 & h_\times & -h_+ & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}_{\mu\nu} \cos[\omega(t - z/c)],$$

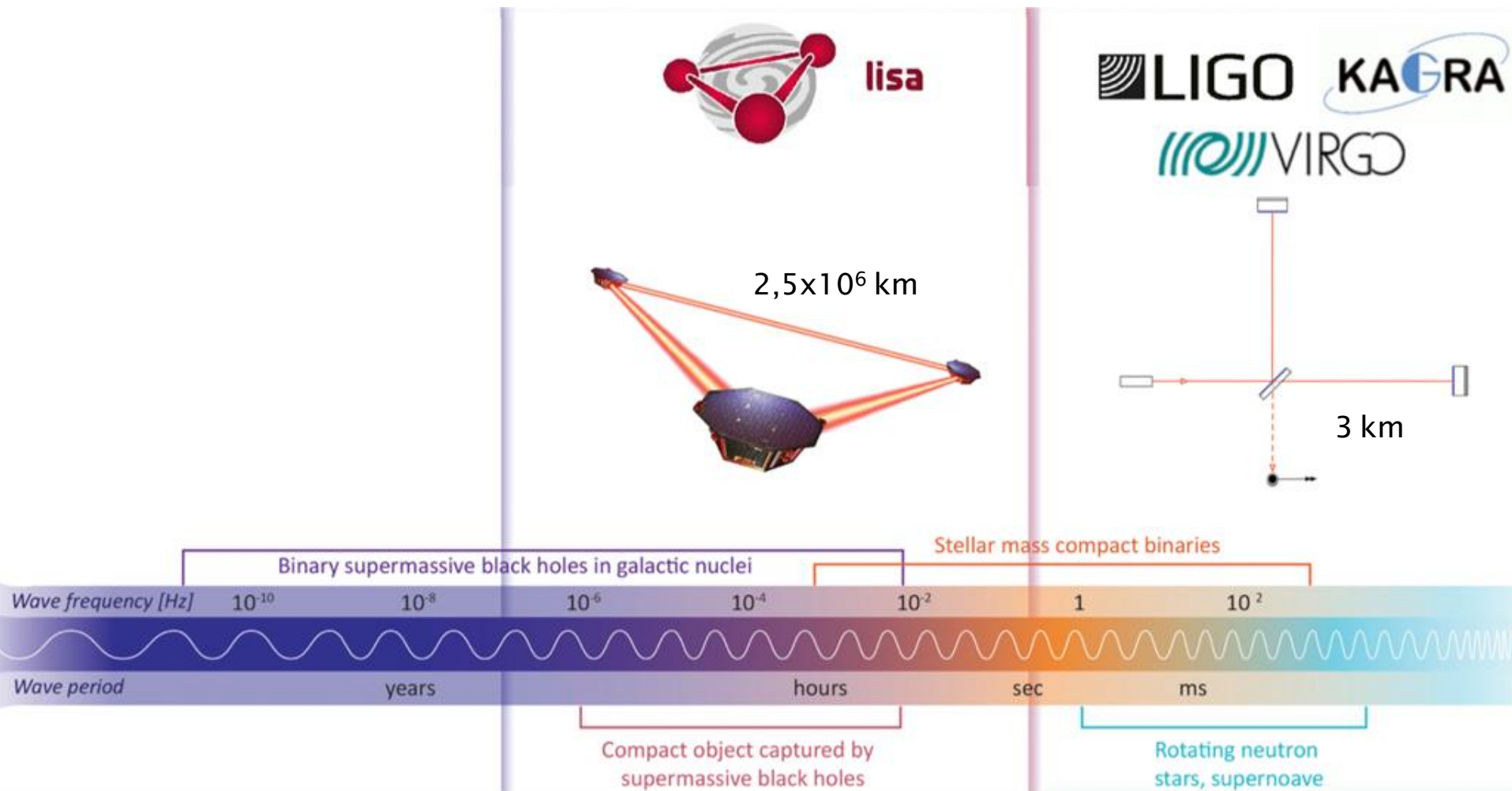
Gravitational waves spectrum



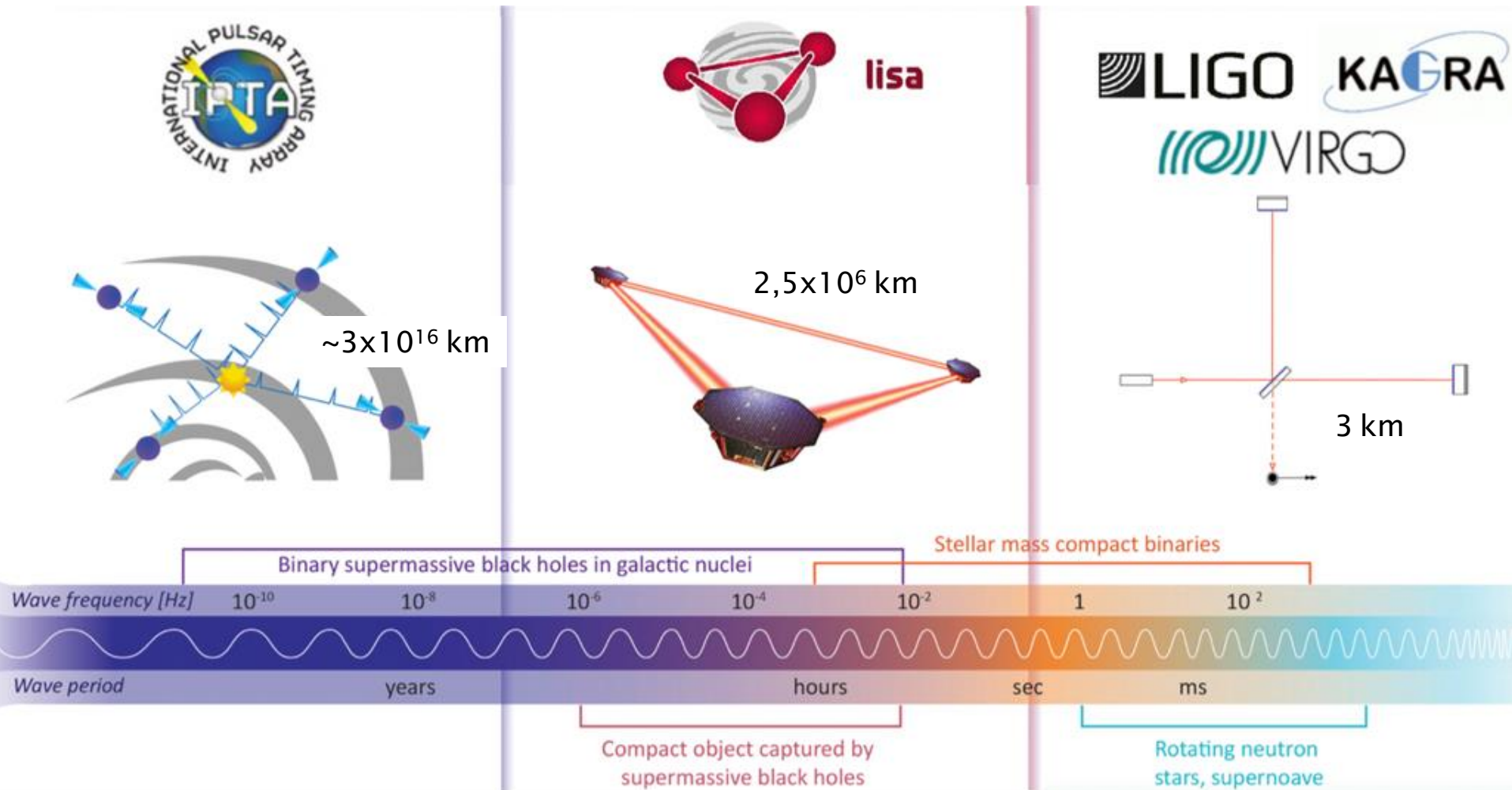
Gravitational waves spectrum



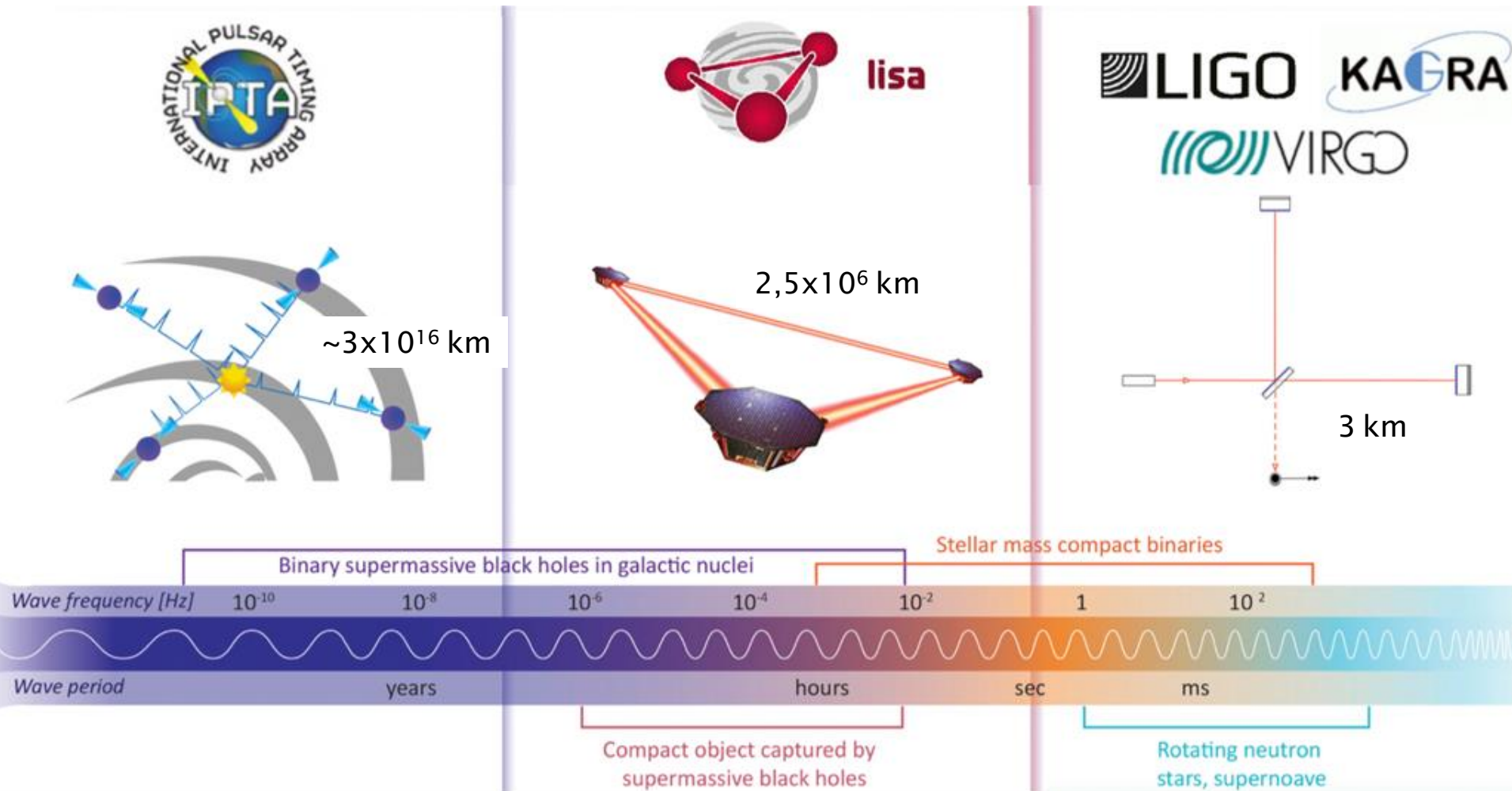
Gravitational waves spectrum



Gravitational waves spectrum

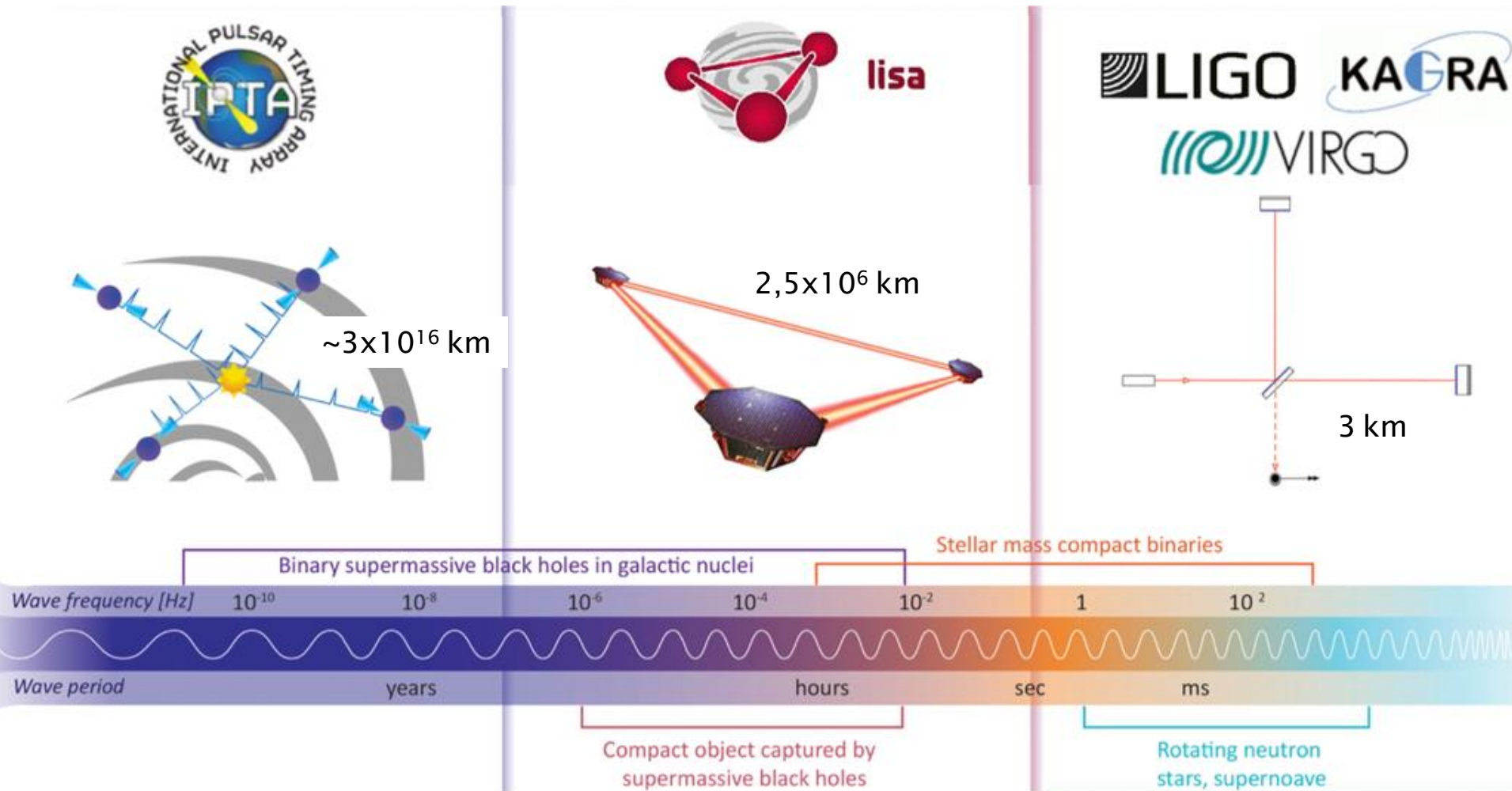


Gravitational waves spectrum



no astrophysical process can generate such a low-frequency GWs

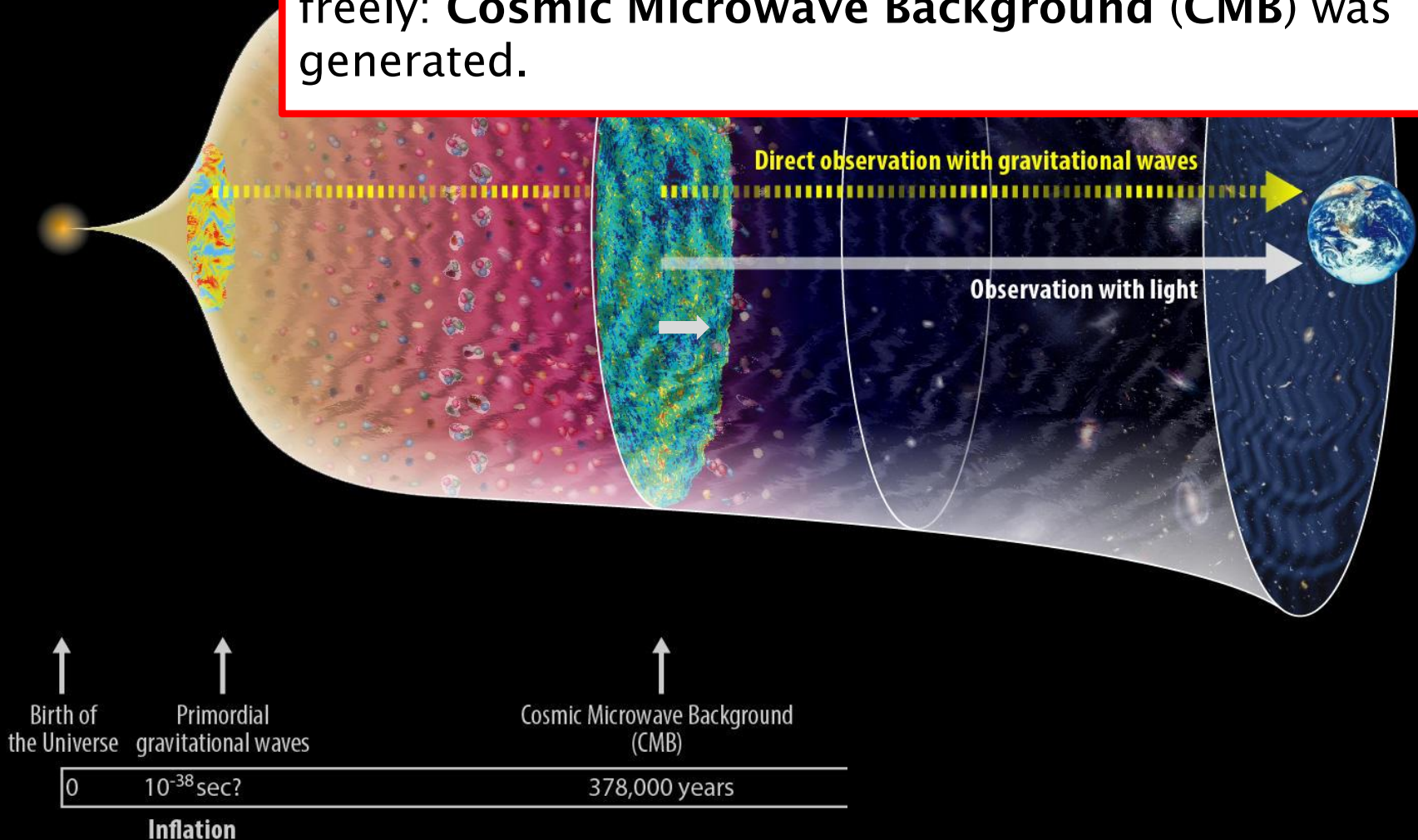
Gravitational waves spectrum

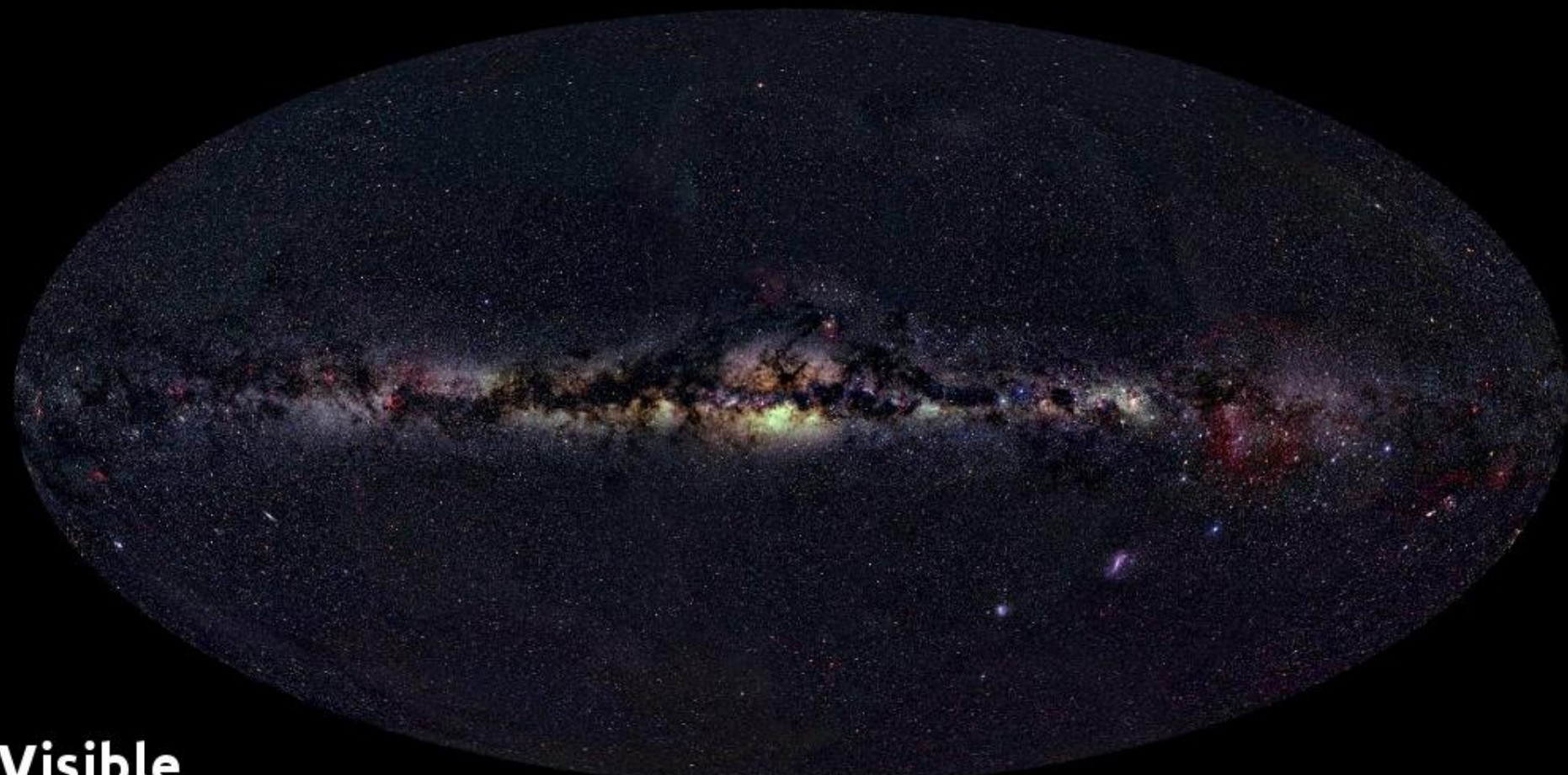


no astrophysical process can generate such a low-frequency GWs

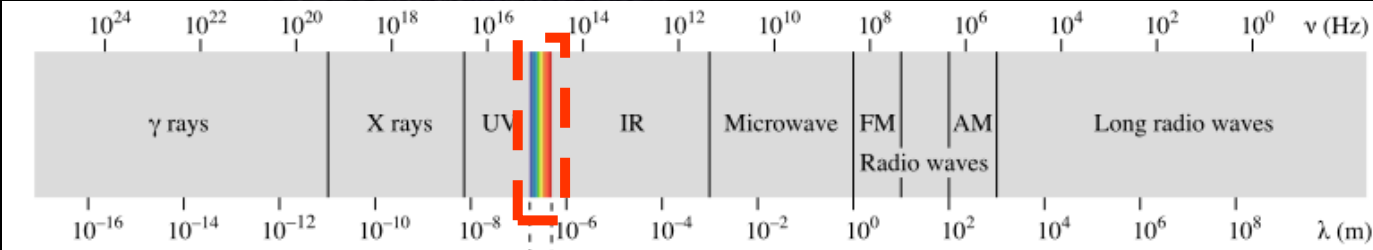
...use the **entire Universe** as a detector (CMB).

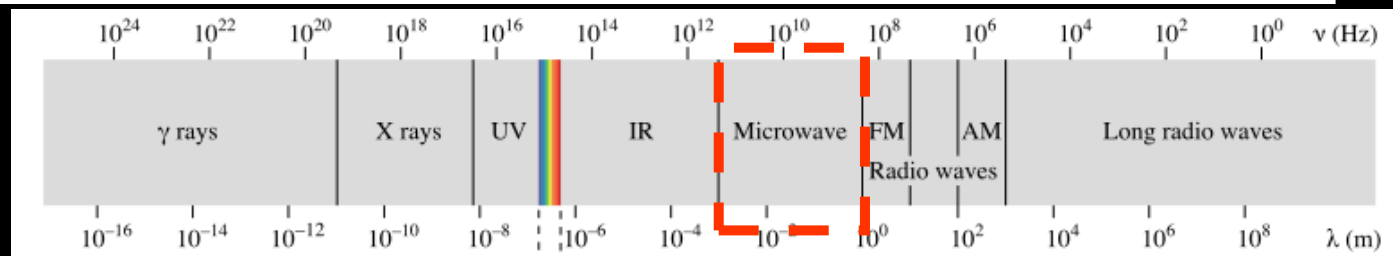
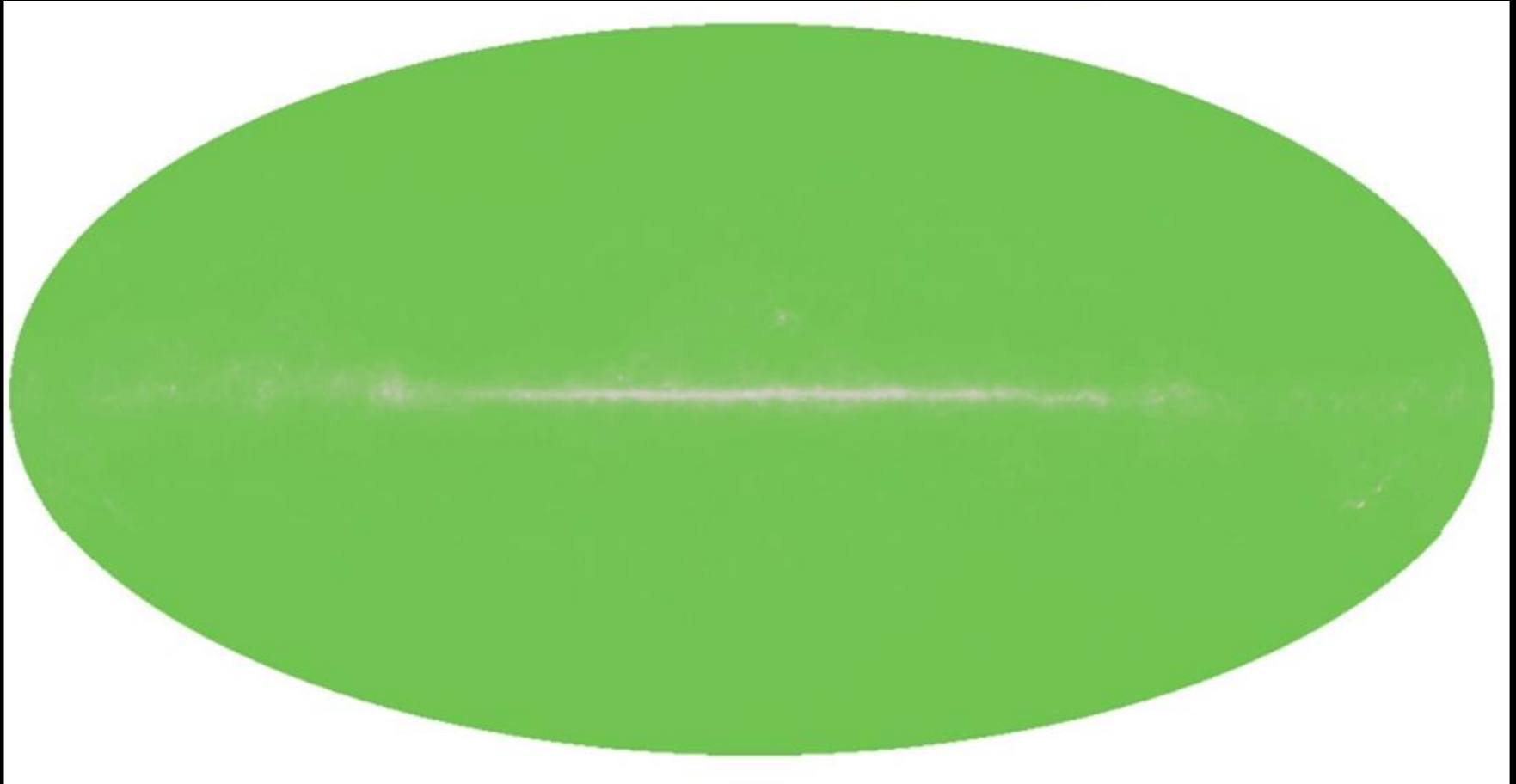
When the universe cooled down to a temperature at which atoms can form (about 3000°C), matter then became neutral, and allowed the light to travel freely: **Cosmic Microwave Background (CMB)** was generated.

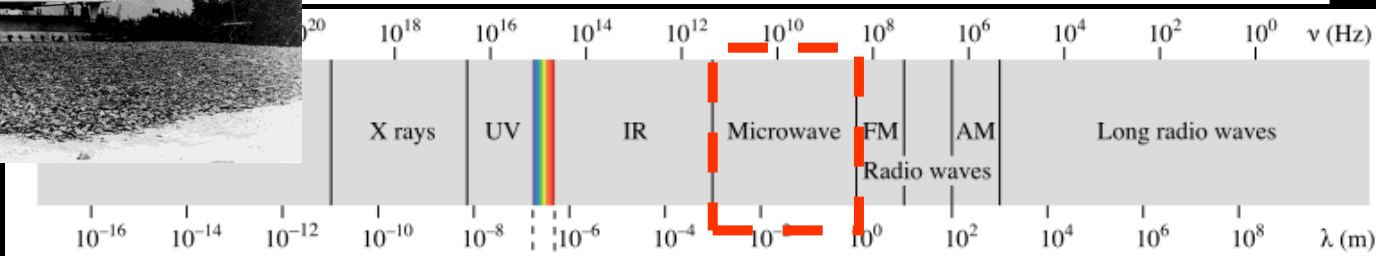
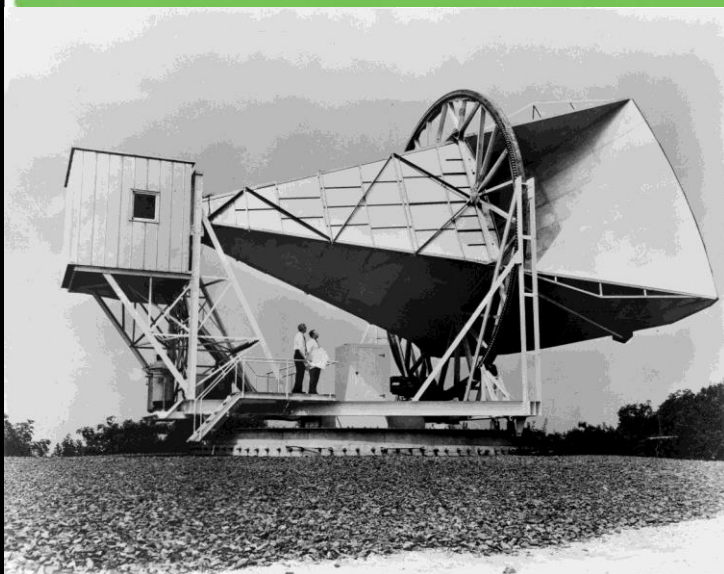
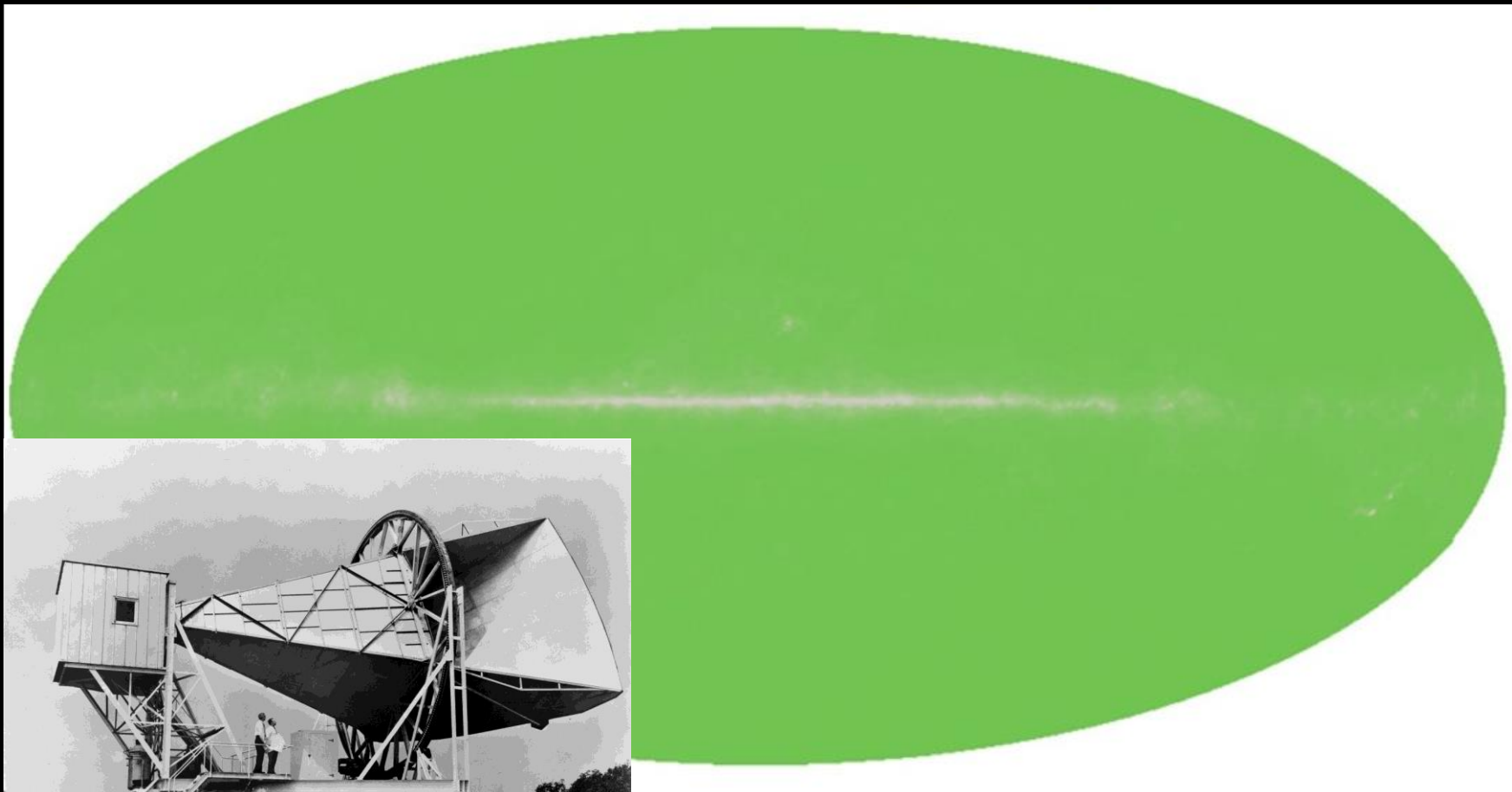


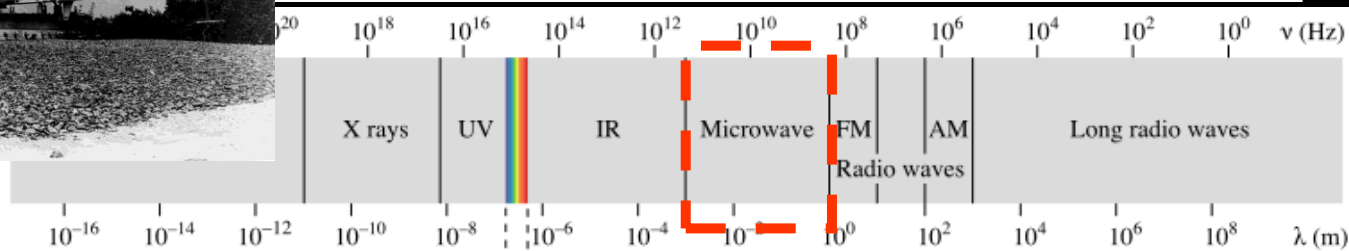
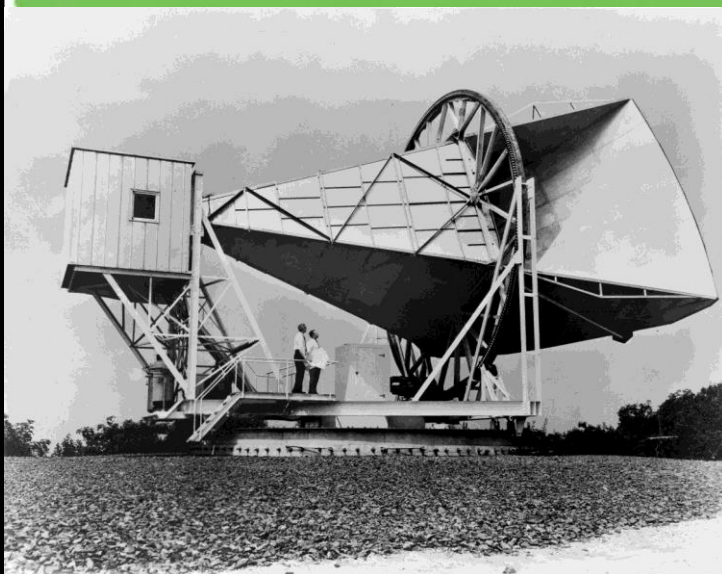
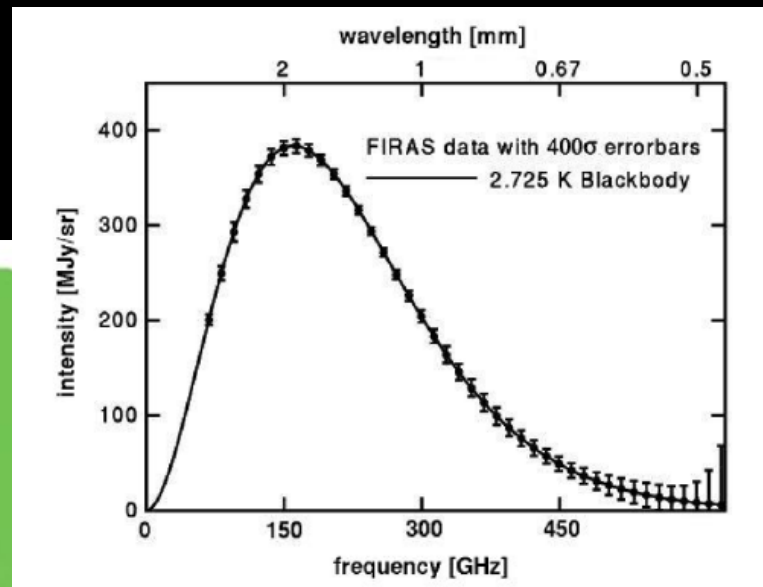
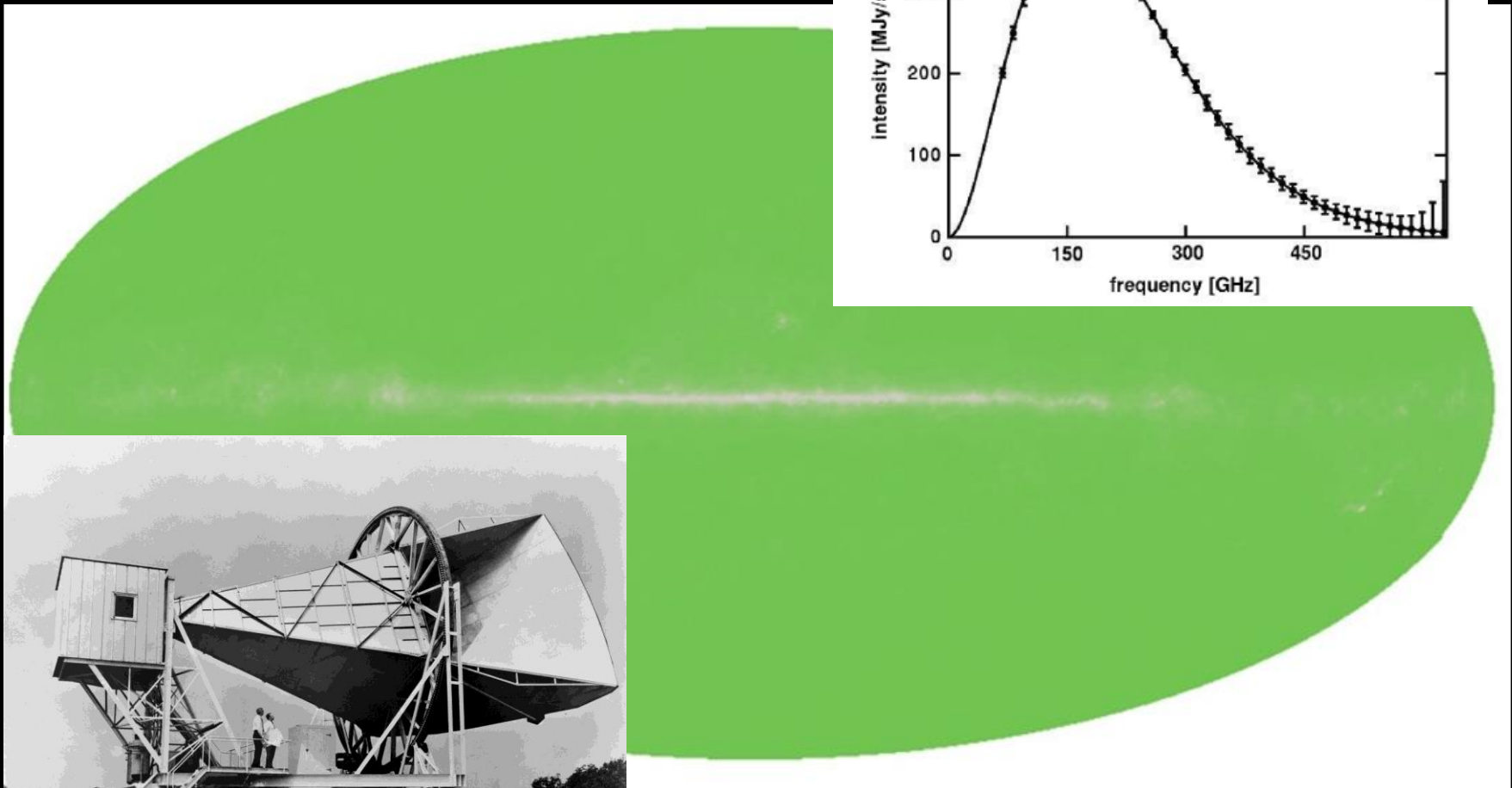


Visible











The Nobel Prize in Physics 1978

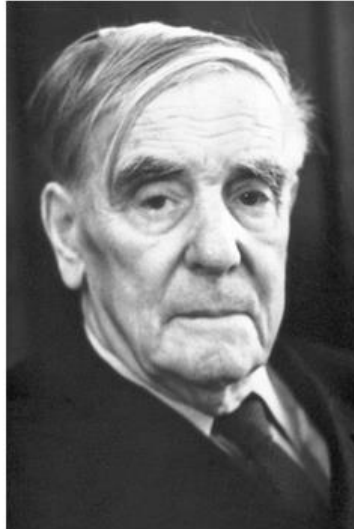


Photo from the Nobel Foundation archive.

Pyotr Leonidovich Kapitsa

Prize share: 1/2



Photo from the Nobel Foundation archive.

Arno Allan Penzias

Prize share: 1/4

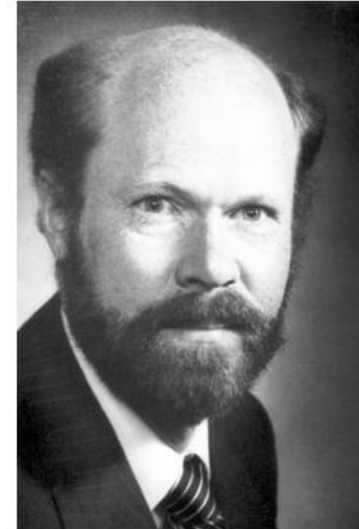


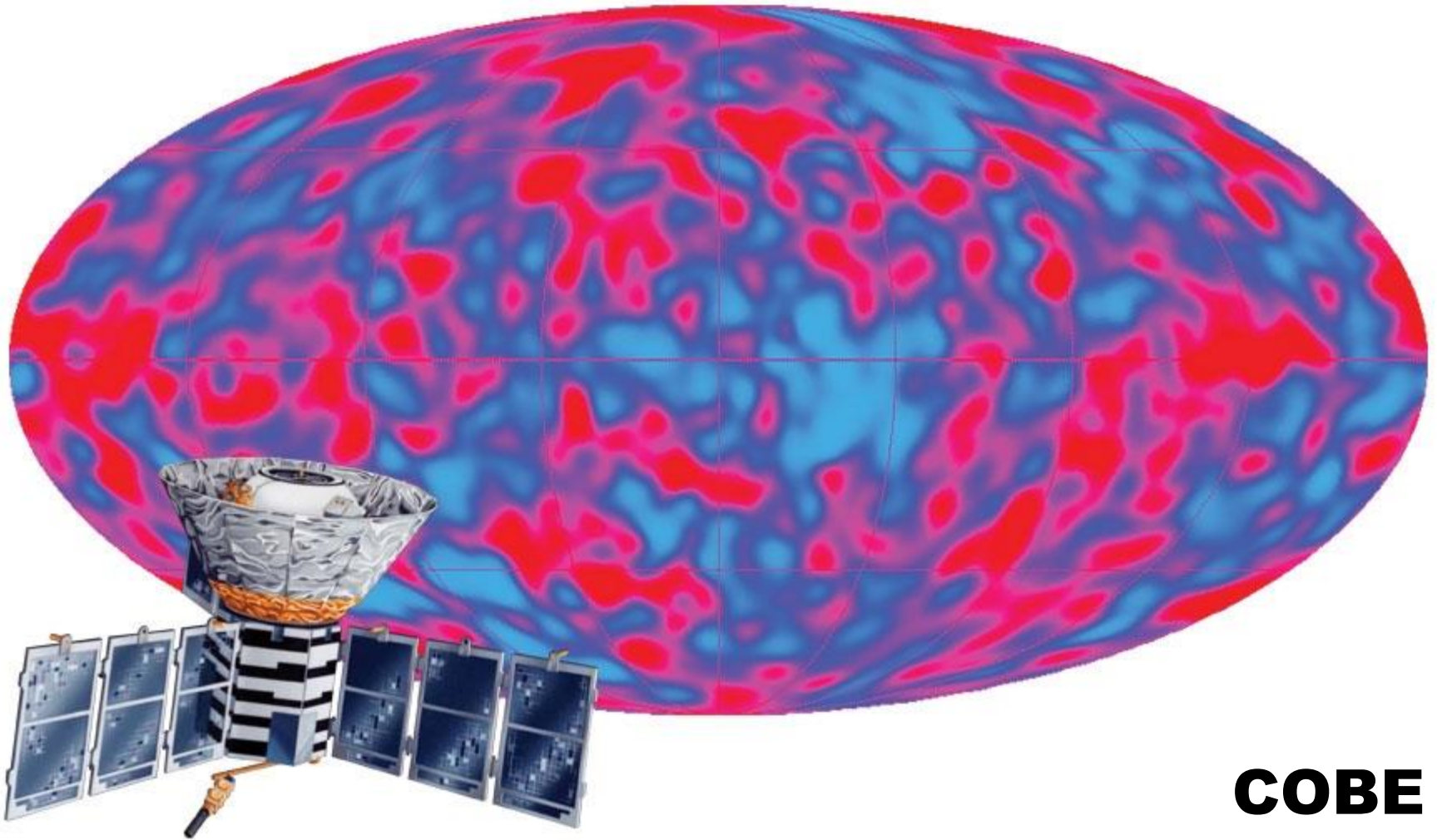
Photo from the Nobel Foundation archive.

Robert Woodrow Wilson

Prize share: 1/4

The Nobel Prize in Physics 1978 was divided, one half awarded to Pyotr Leonidovich Kapitsa "for his basic inventions and discoveries in the area of low-temperature physics", the other half jointly to Arno Allan Penzias and Robert Woodrow Wilson "for their discovery of cosmic microwave background radiation"

$$T = 2.7 \pm 0.00003 \text{ K}$$



COBE



The Nobel Prize in Physics 2006



Photo: P. Izzo

John C. Mather

Prize share: 1/2

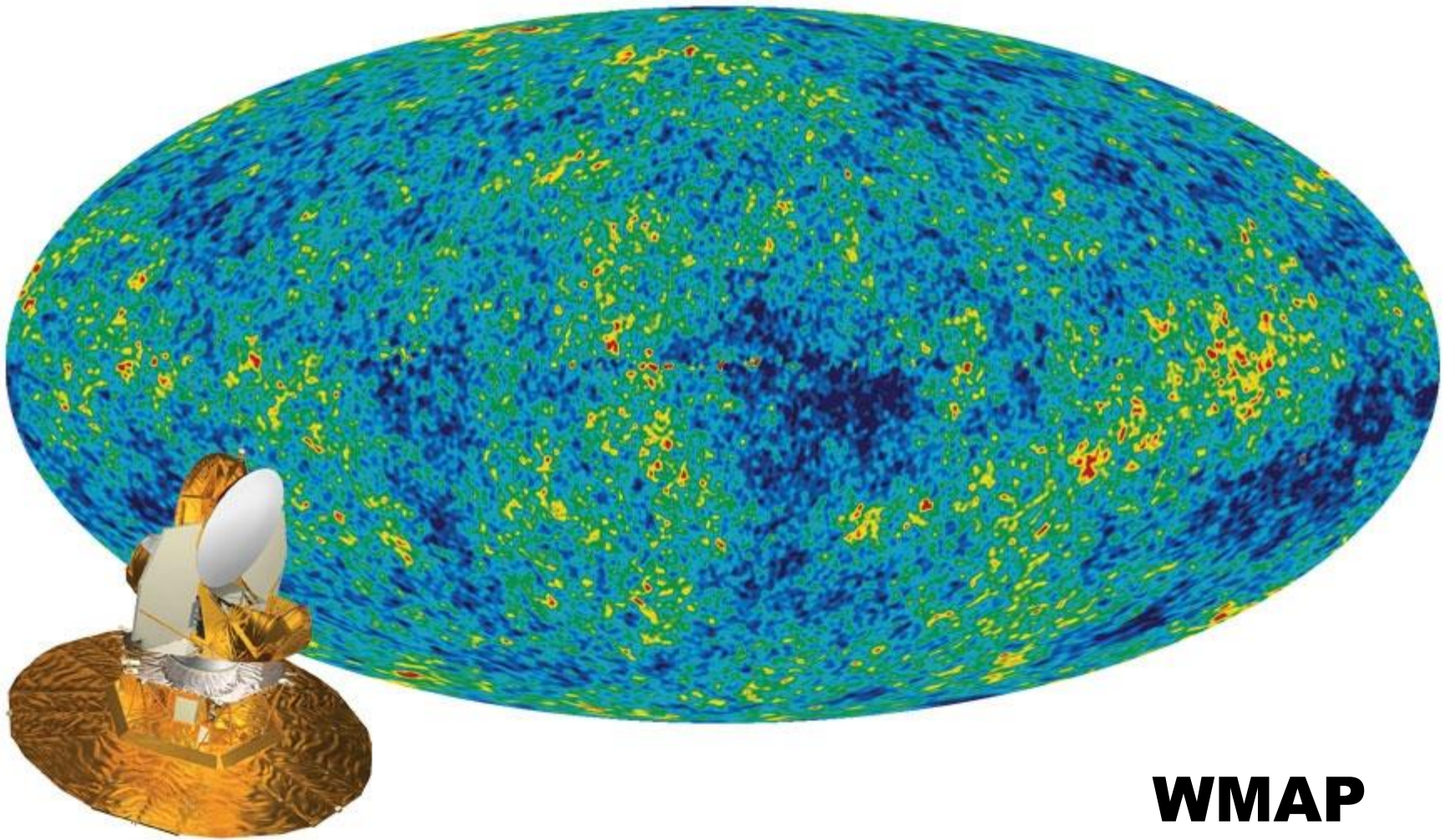


Photo: J. Bauer

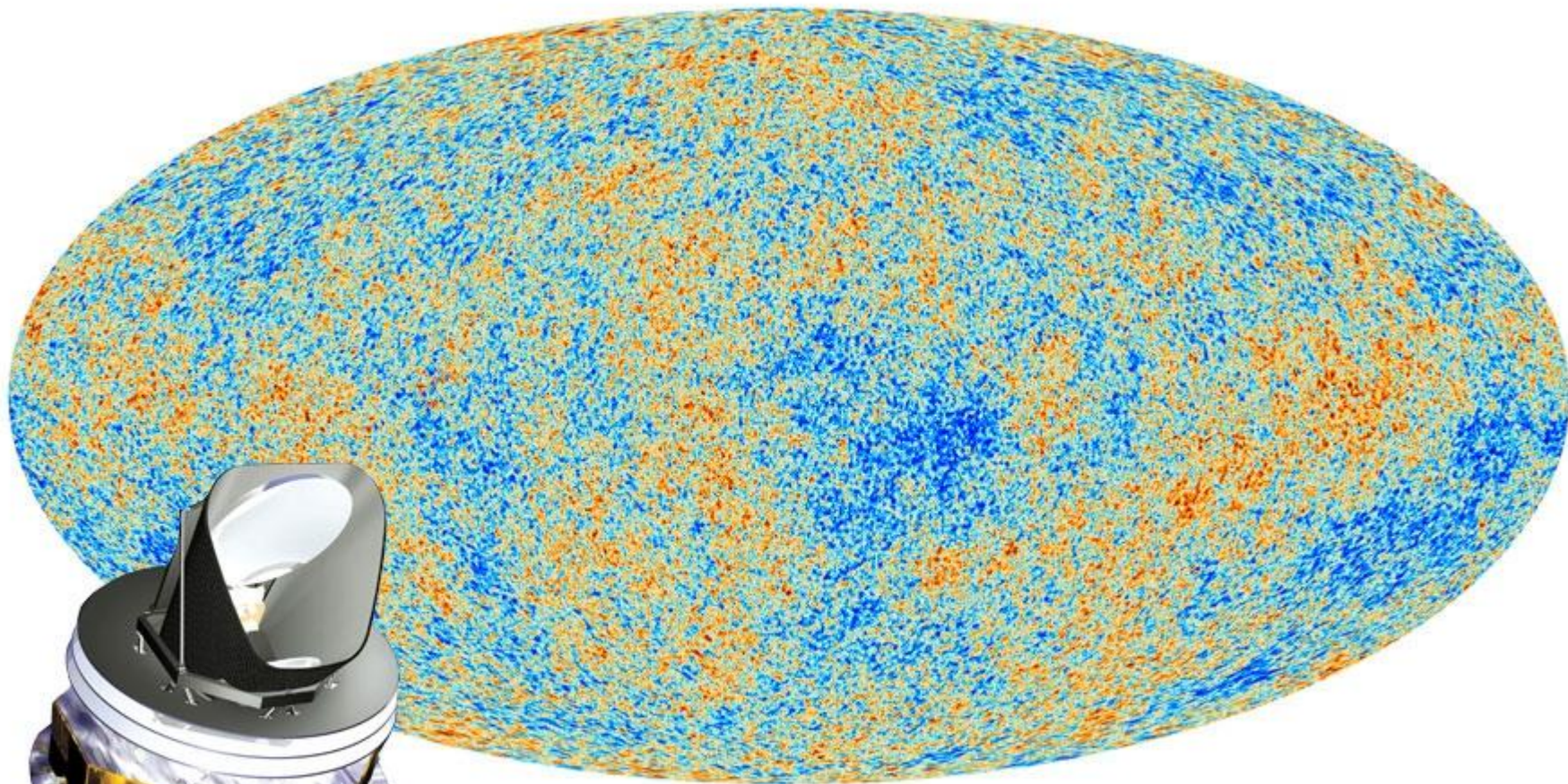
George F. Smoot

Prize share: 1/2

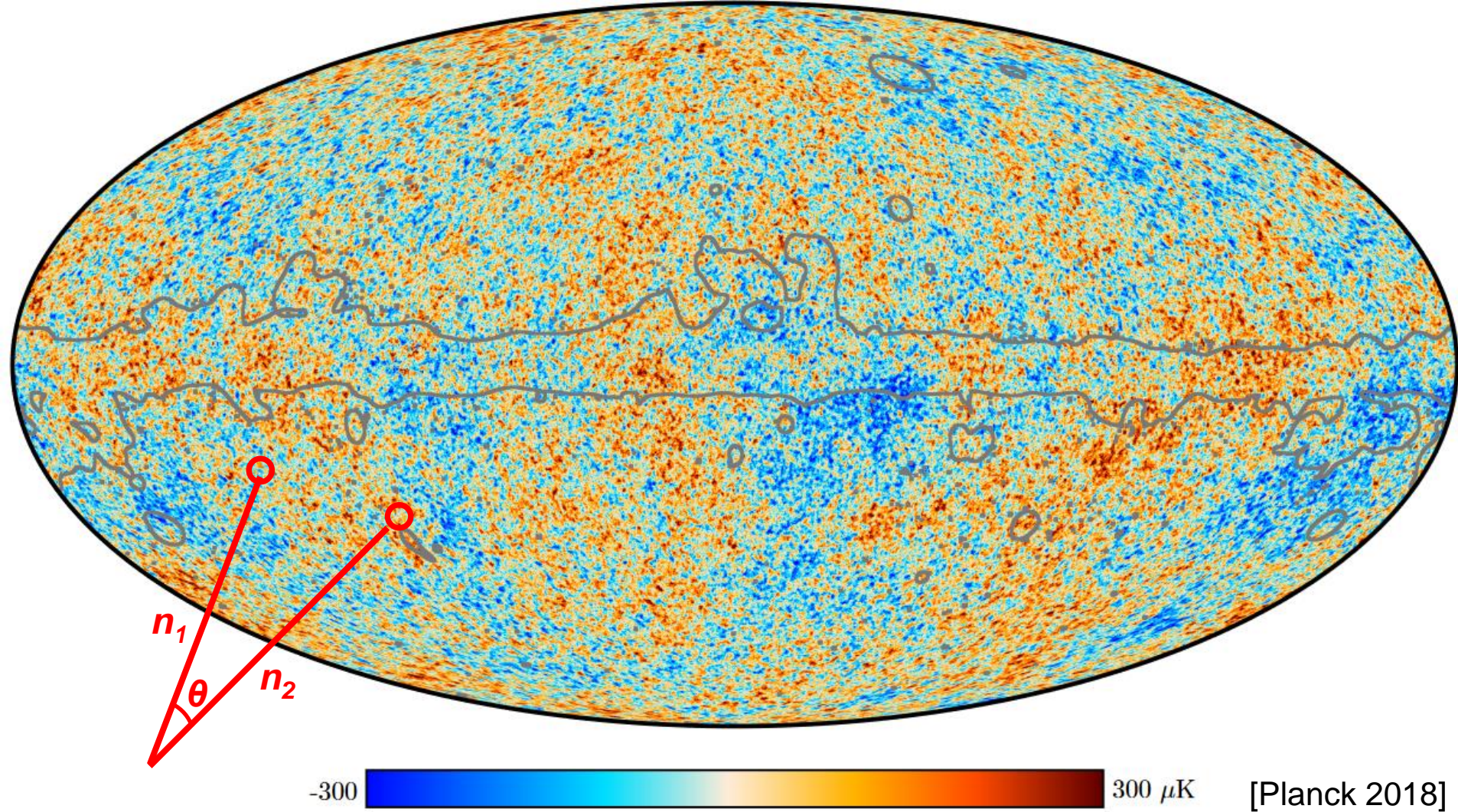
The Nobel Prize in Physics 2006 was awarded jointly to John C. Mather and George F. Smoot "for their discovery of the blackbody form and anisotropy of the cosmic microwave background radiation"



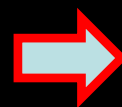
WMAP



PLANCK

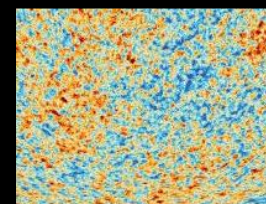
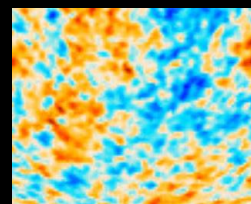
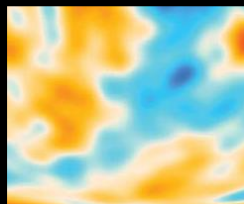


$$\frac{\Delta T(\theta, \phi)}{T} = \sum_{l=0}^{\infty} \sum_{m=-l}^{m=+l} a_{lm} Y_{lm}(\theta, \phi)$$



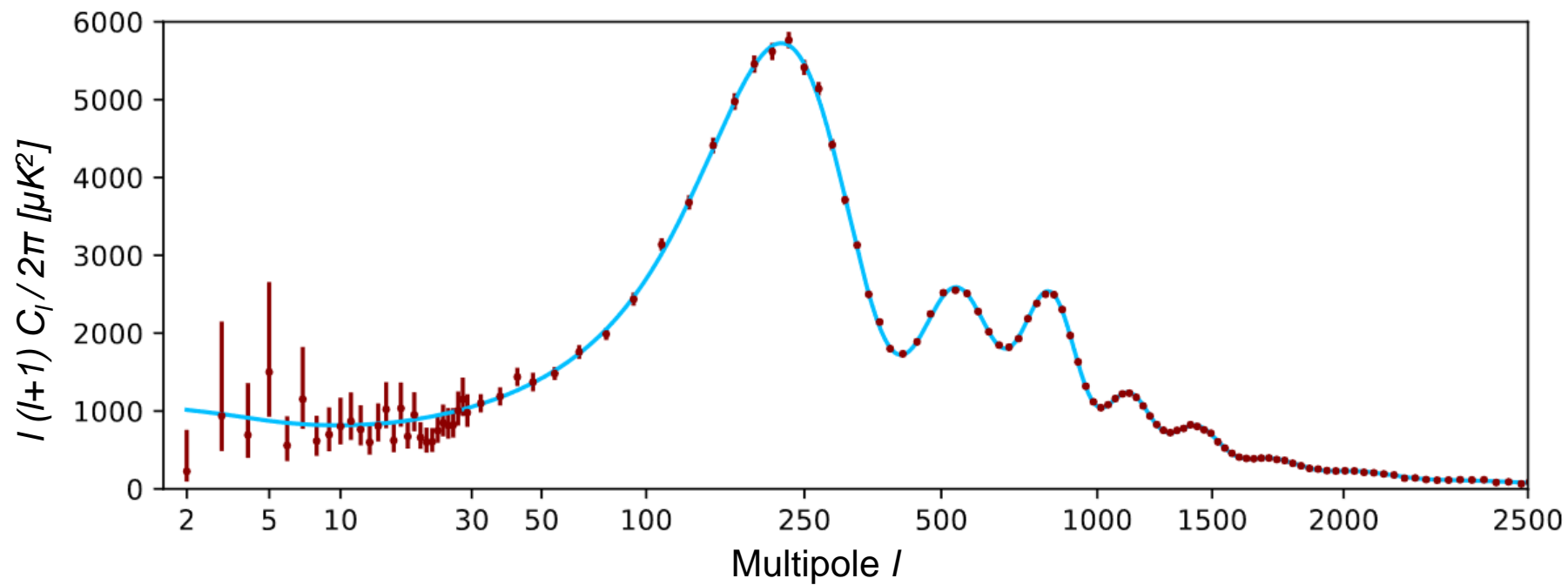
$$C_l \equiv \langle |a_{lm}|^2 \rangle$$

$$\theta \approx 60^\circ/l$$



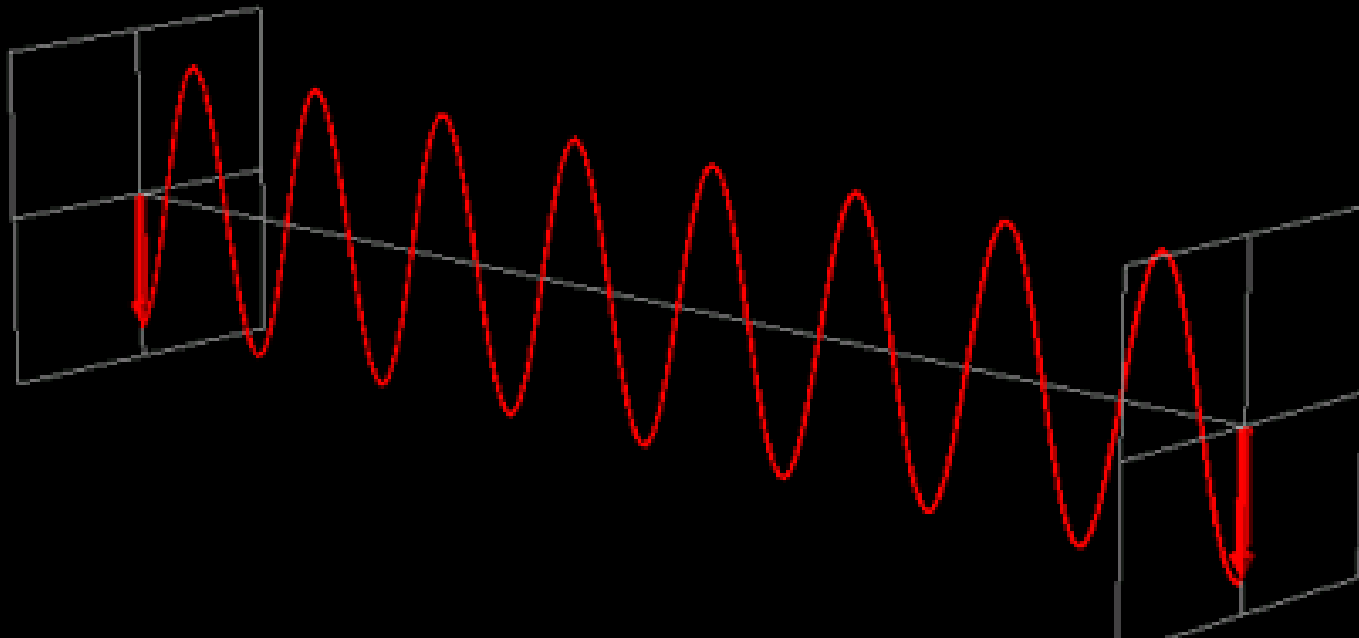
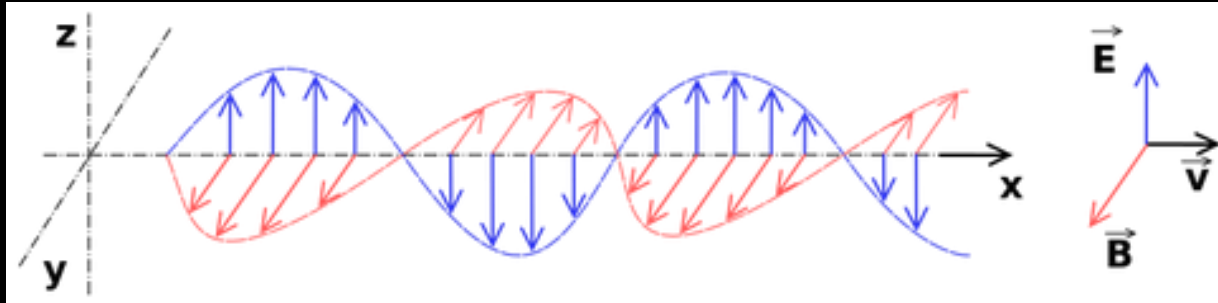
$$\theta \approx 1^\circ$$

Size of the fluctuations

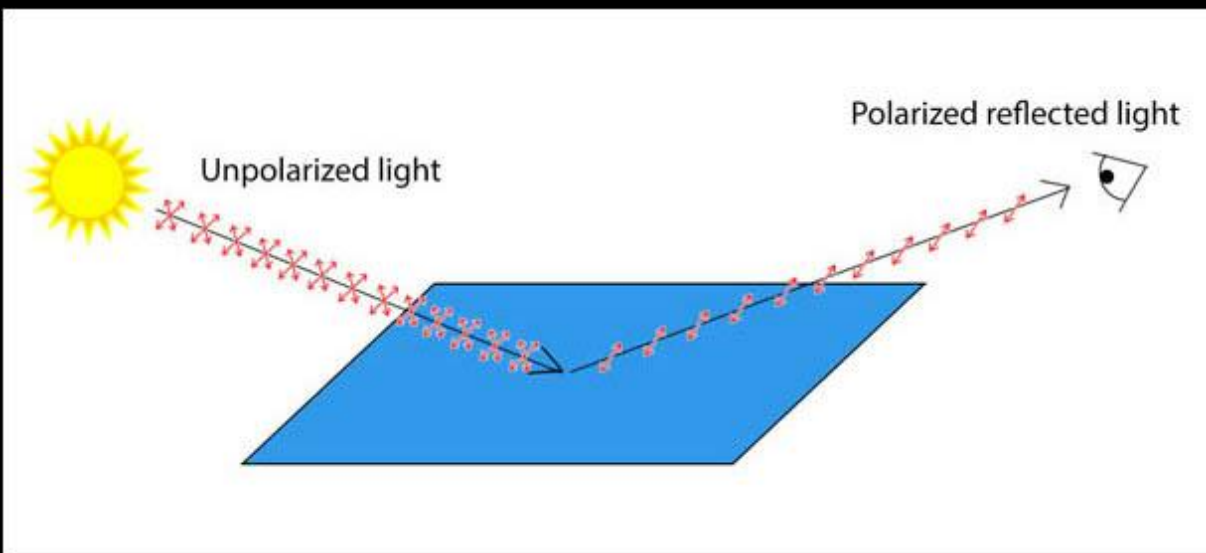


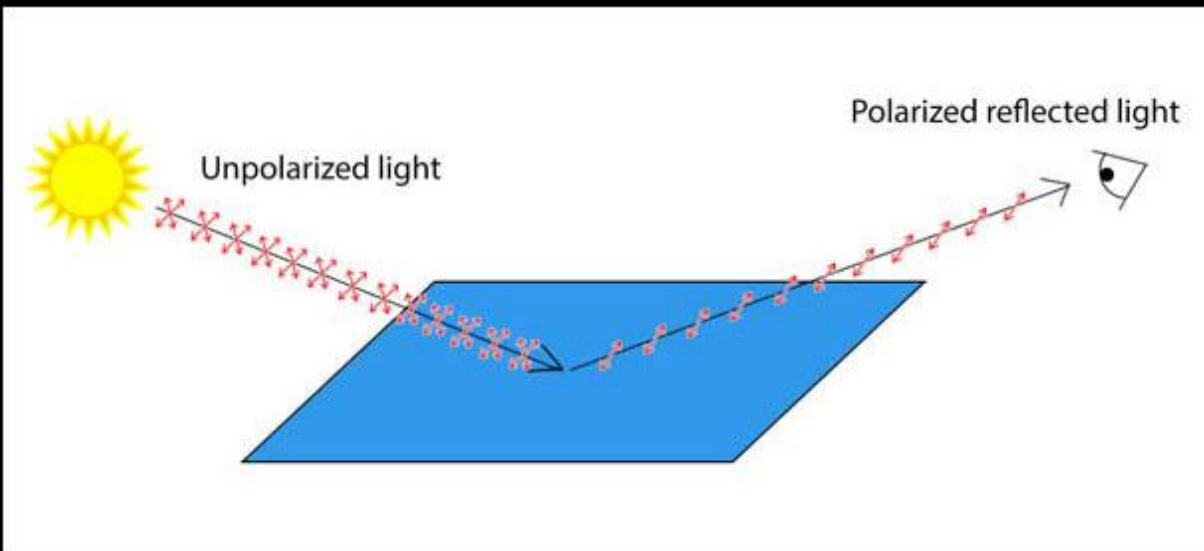
Angular scale

Polarization of light

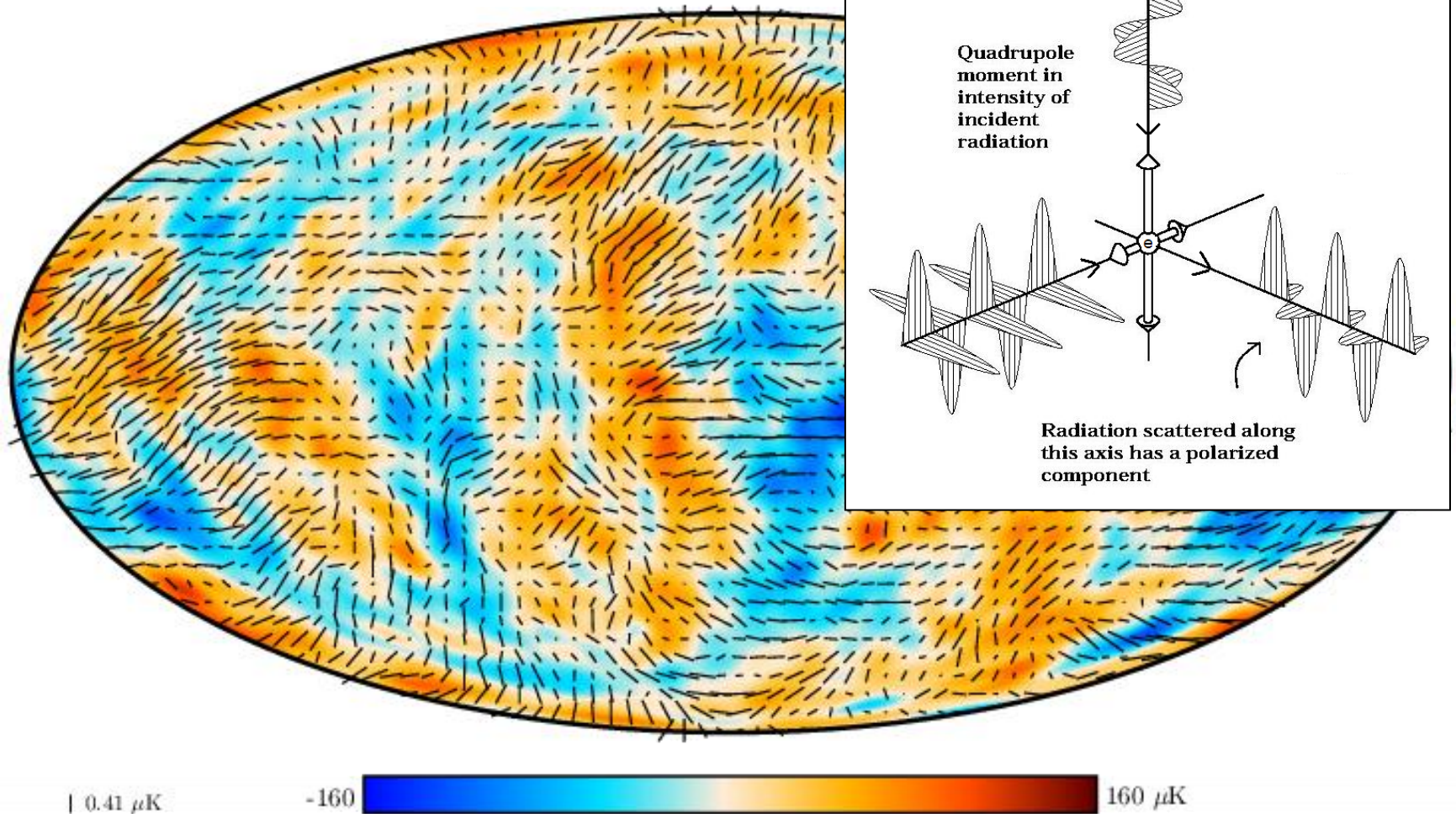


Linear polarization



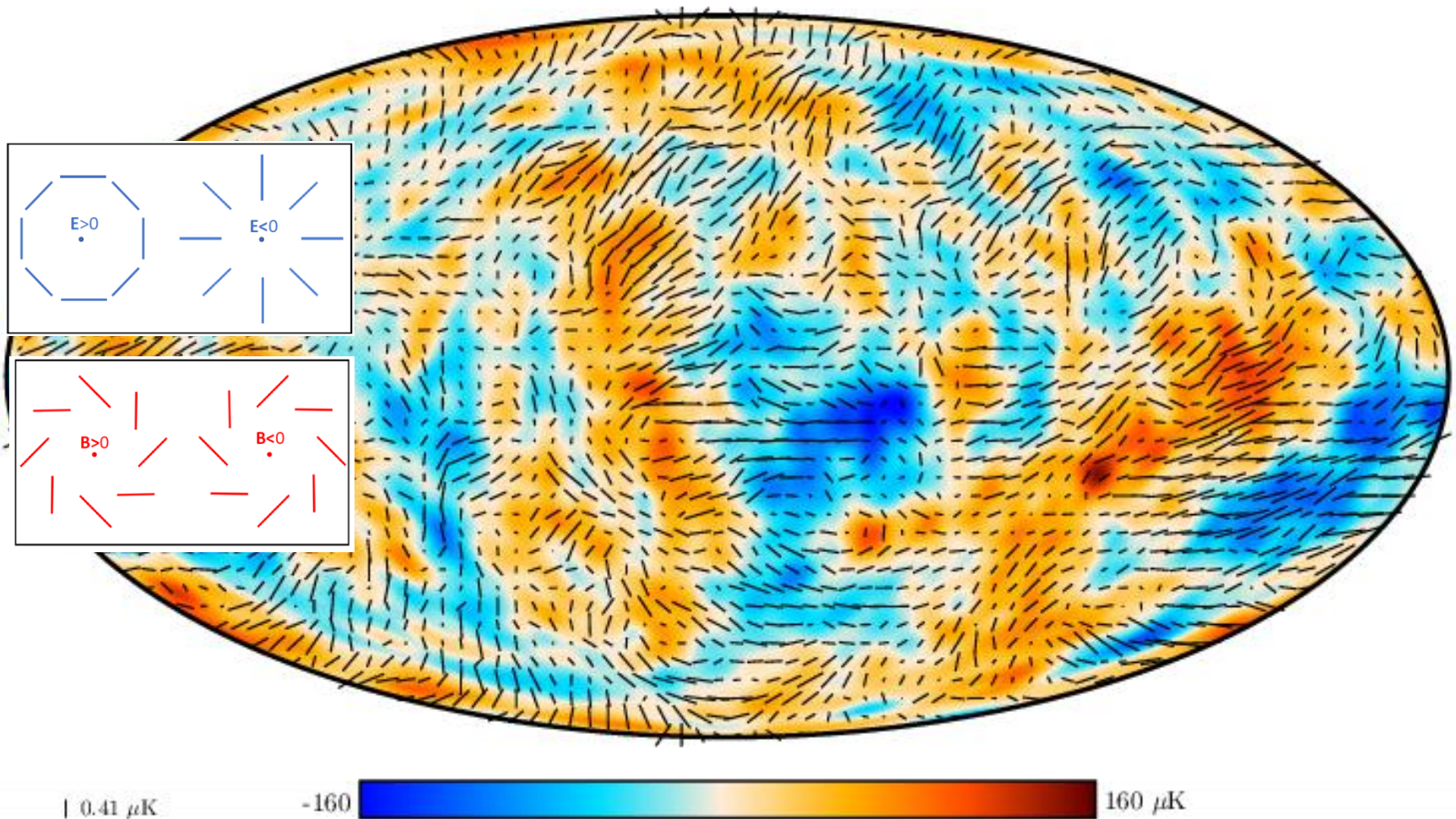


CMB polarization anisotropies

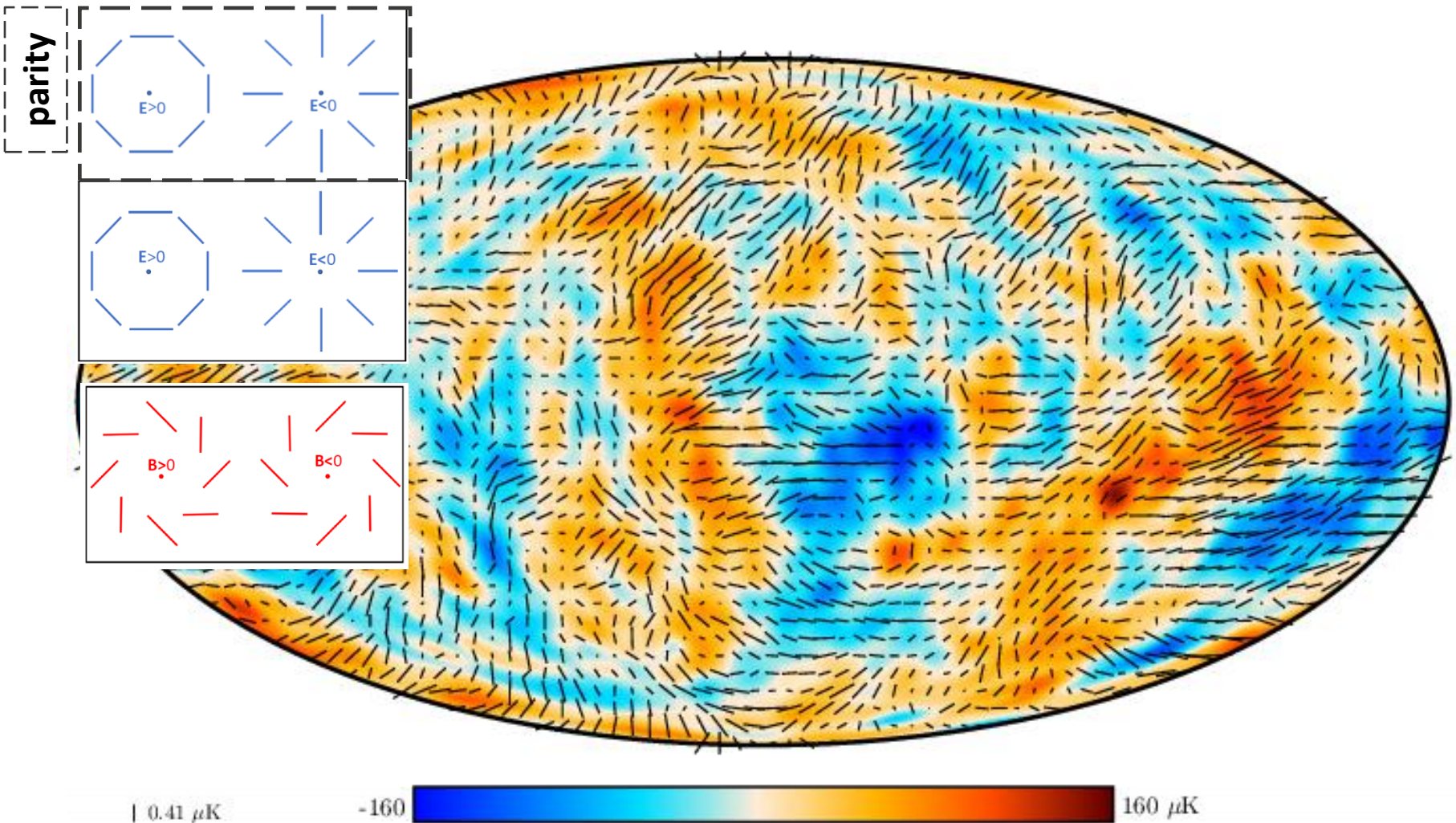


[2018 Planck map of the polarized CMB anisotropies]

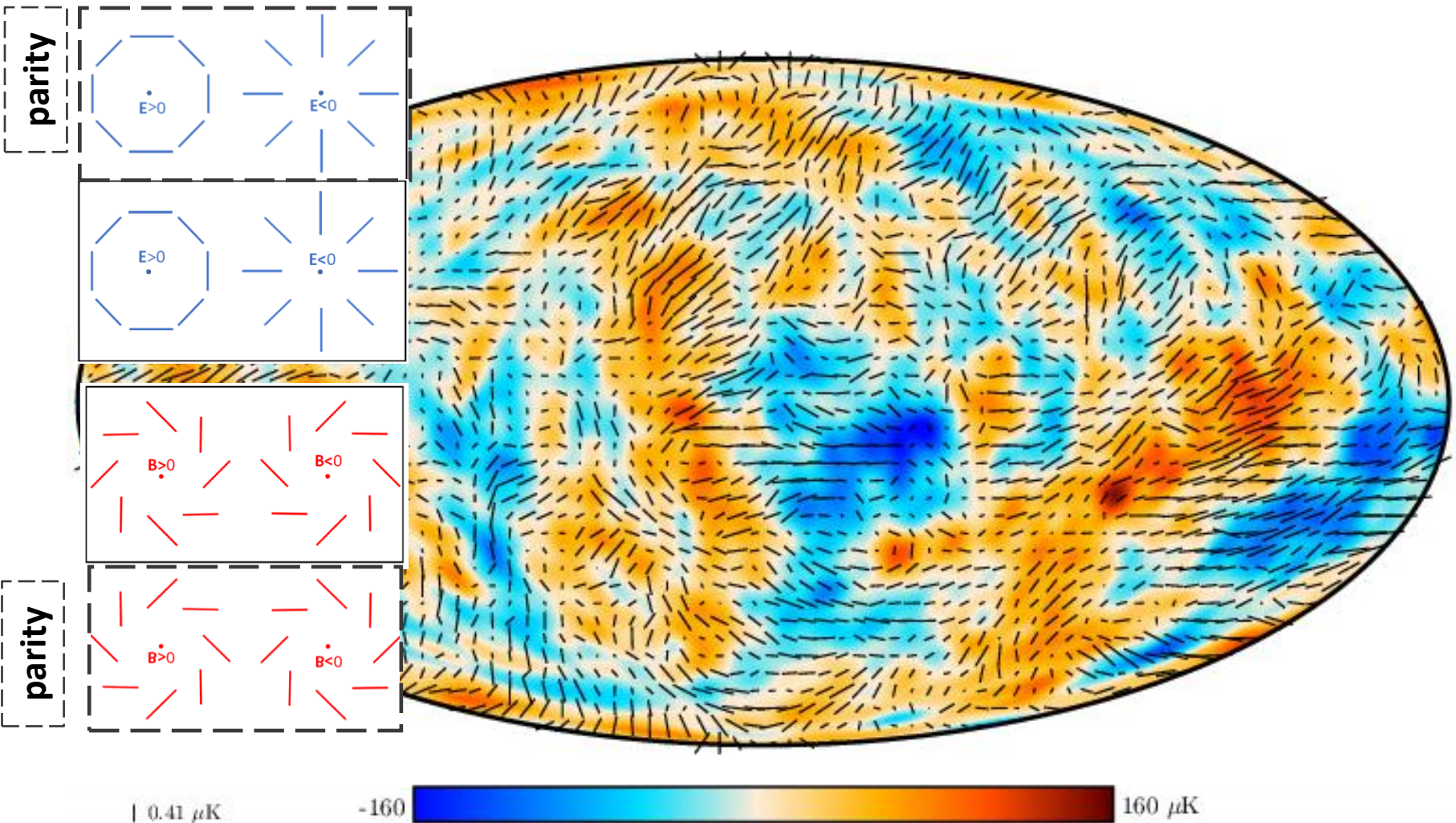
CMB polarization anisotropies

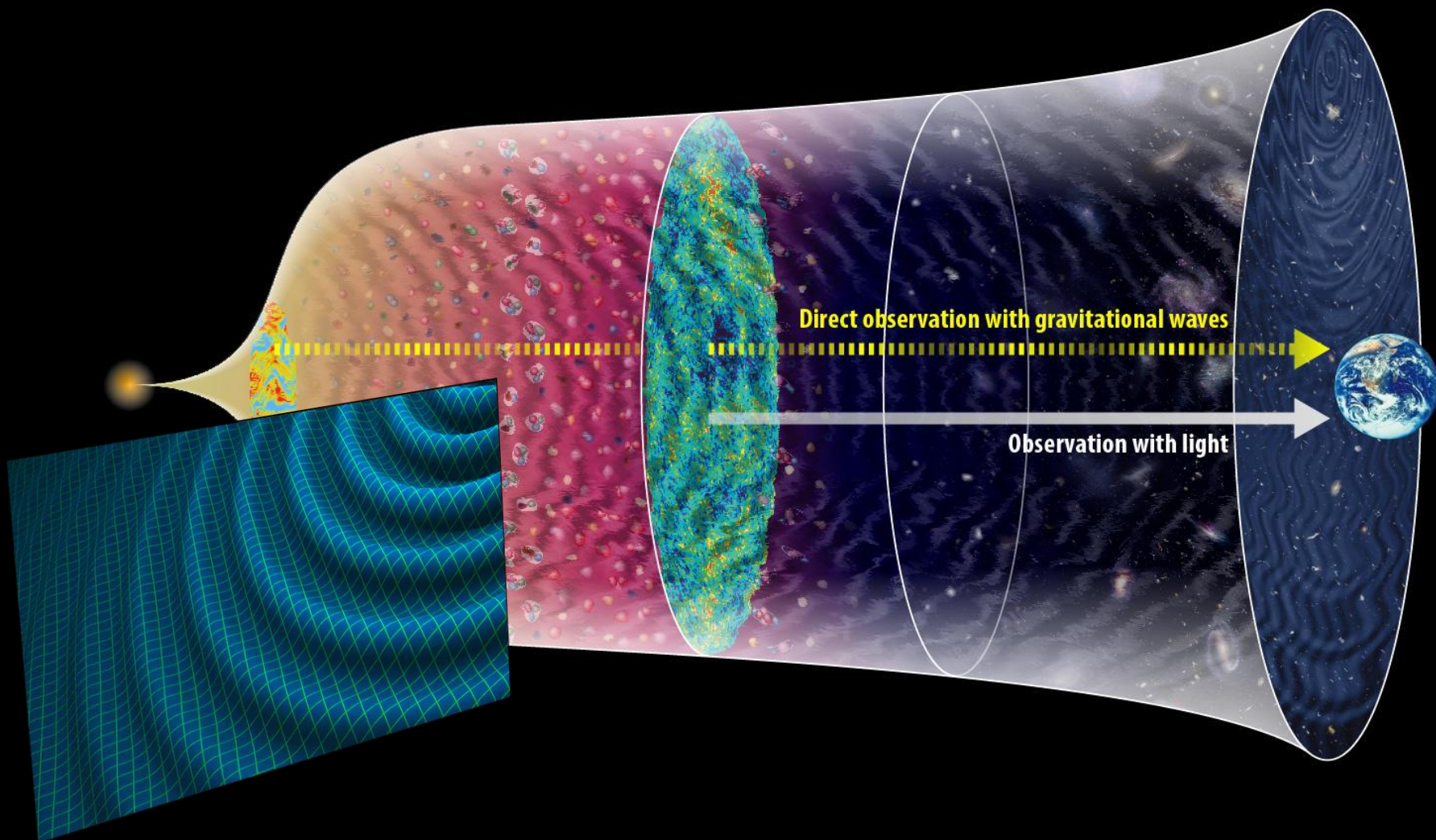


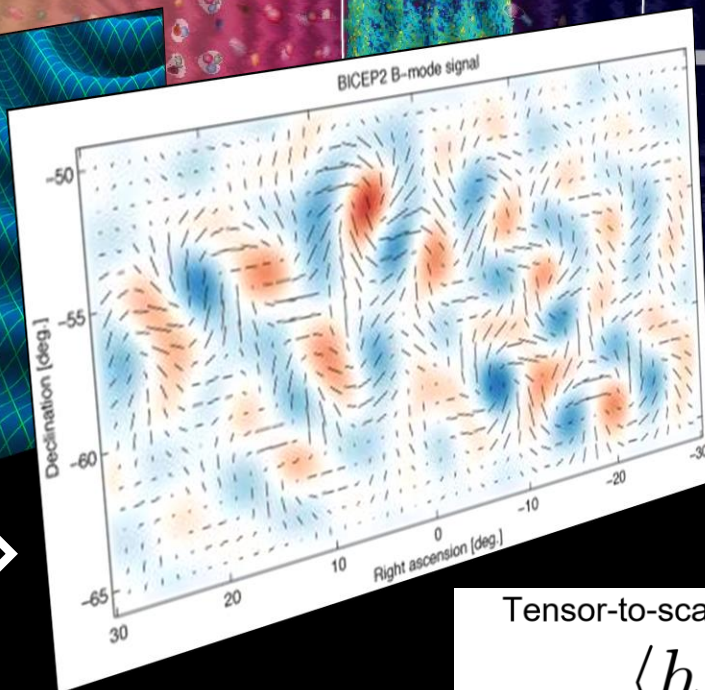
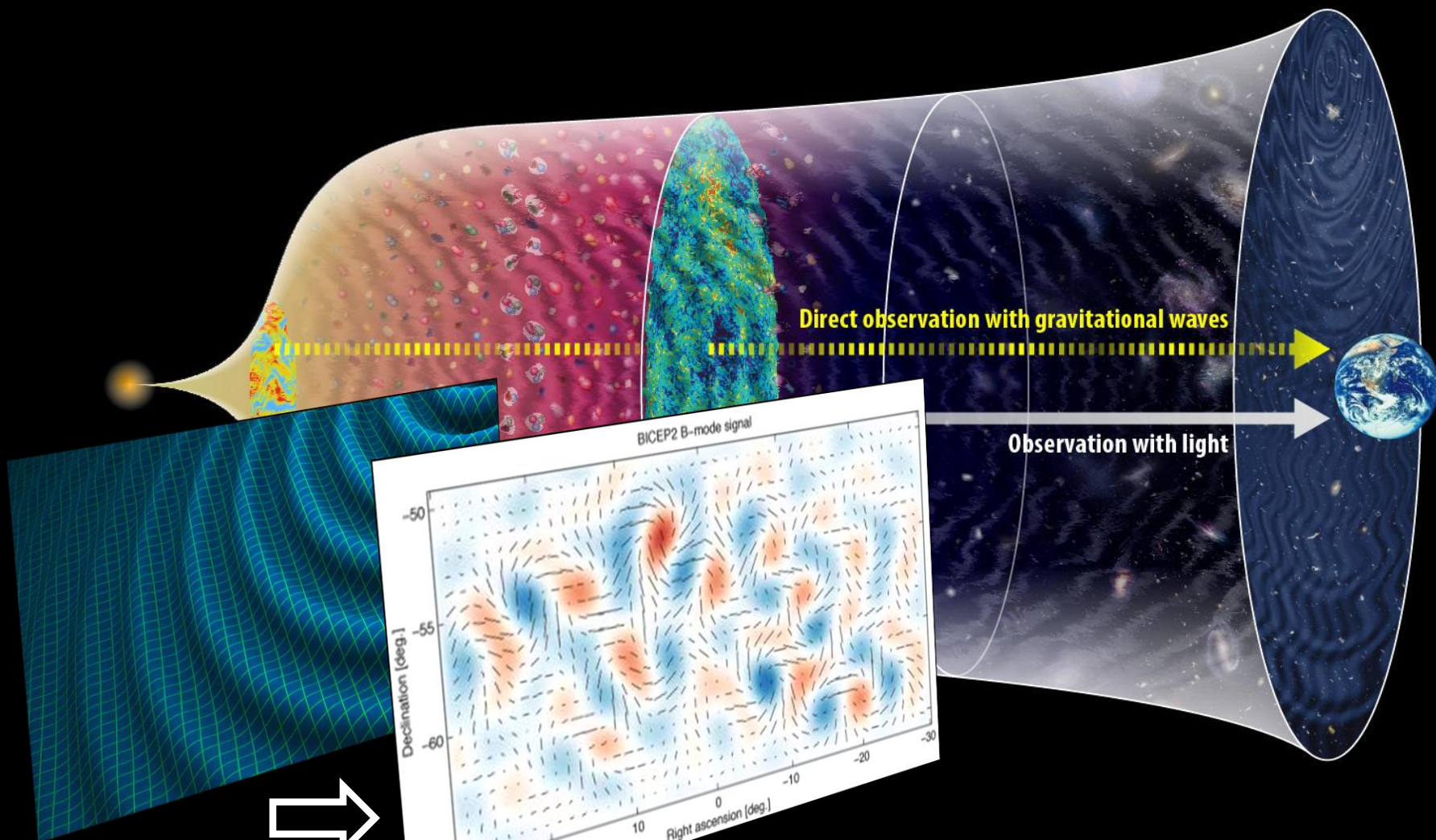
CMB polarization anisotropies



CMB polarization anisotropies







Tensor-to-scalar Ratio

$$r \equiv \frac{\langle h_{ij} h^{ij} \rangle}{\langle \zeta^2 \rangle}$$

Scalar mode



Detection of *B*-Mode Polarization at Degree Angular Scales by BICEP2

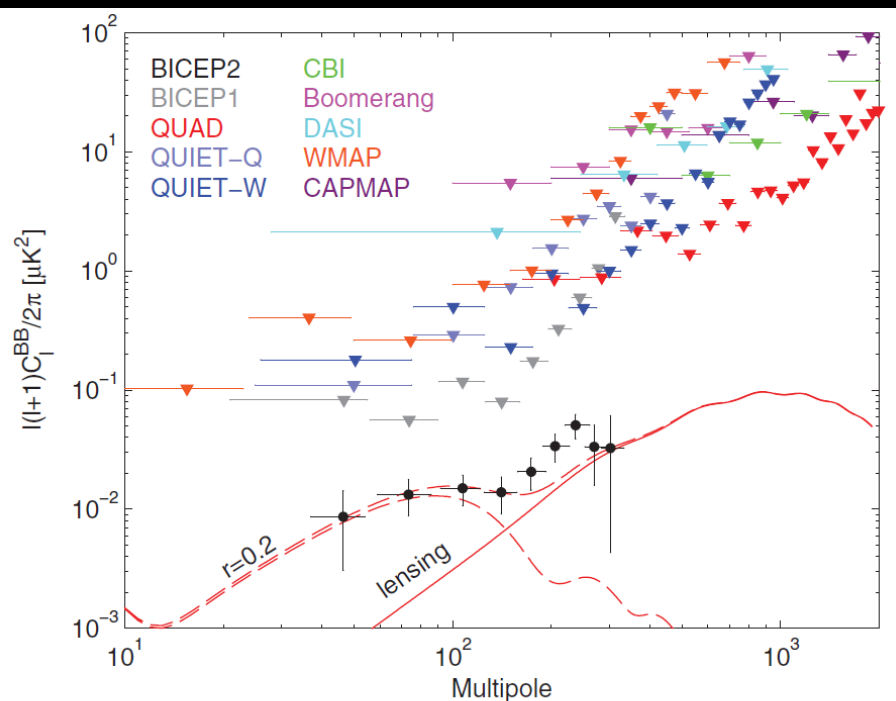


FIG. 14 (color). BICEP2 *BB* auto spectra and 95% upper limits from several previous experiments [2,40,42,43,47,49–51,107]. The curves show the theory expectations for $r = 0.2$ and lensed Λ CDM. The BICEP2 uncertainties include sample variance on an $r = 0.2$ contribution.



BICEP
 (Background Imaging of Cosmic
 Extragalactic Polarization)



Detection of *B*-Mode Polarization at Degree Angular Scales by BICEP2

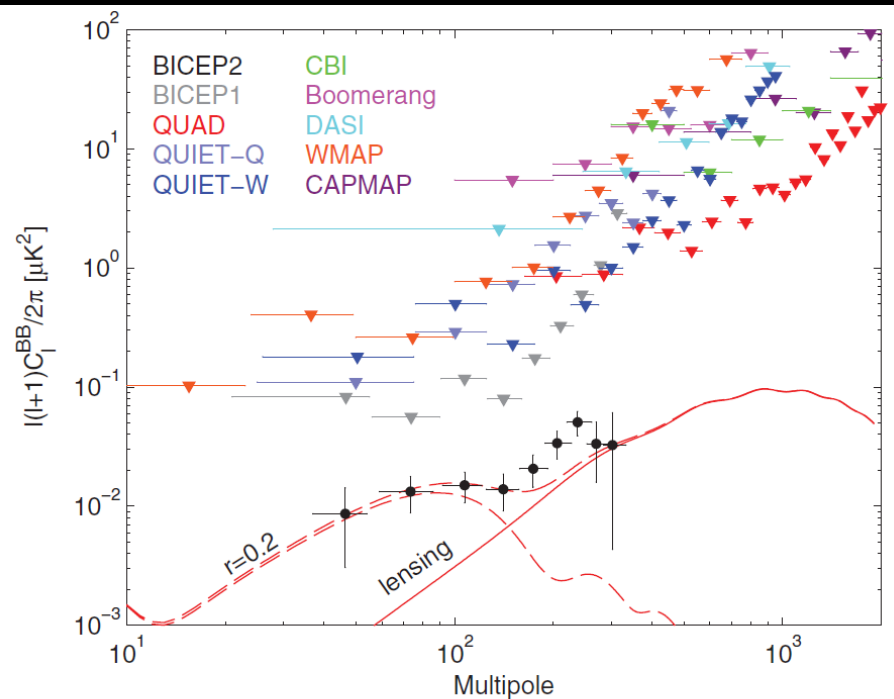
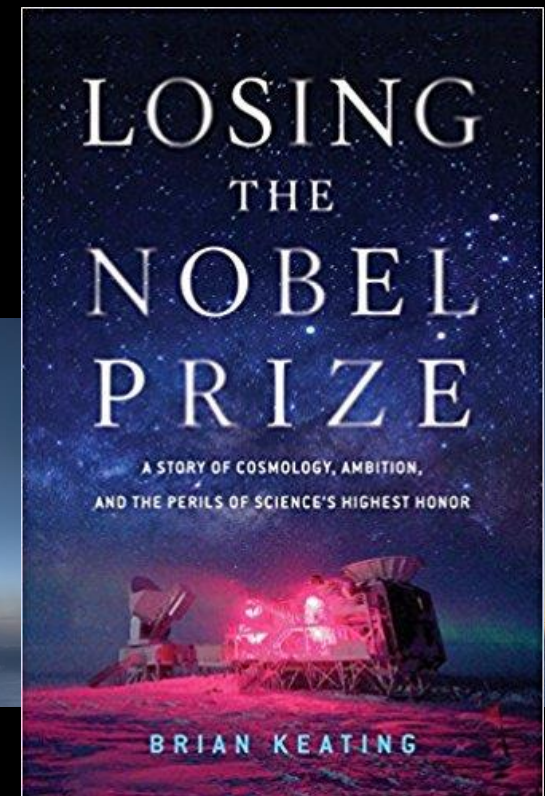


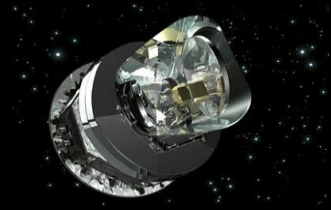
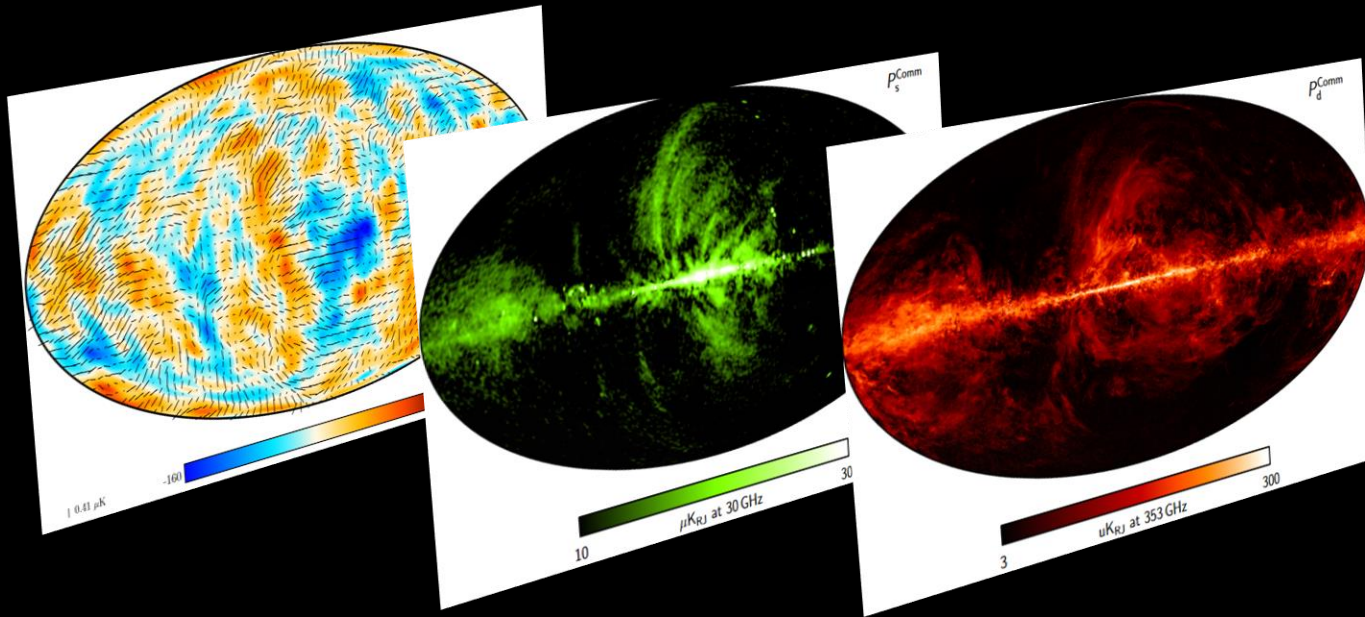
FIG. 14 (color). BICEP2 *BB* auto spectra and 95% upper limits from several previous experiments [2,40,42,43,47,49–51,107]. The curves show the theory expectations for $r = 0.2$ and lensed Λ CDM. The BICEP2 uncertainties include sample variance on an $r = 0.2$ contribution.



CMB

Synchrotron

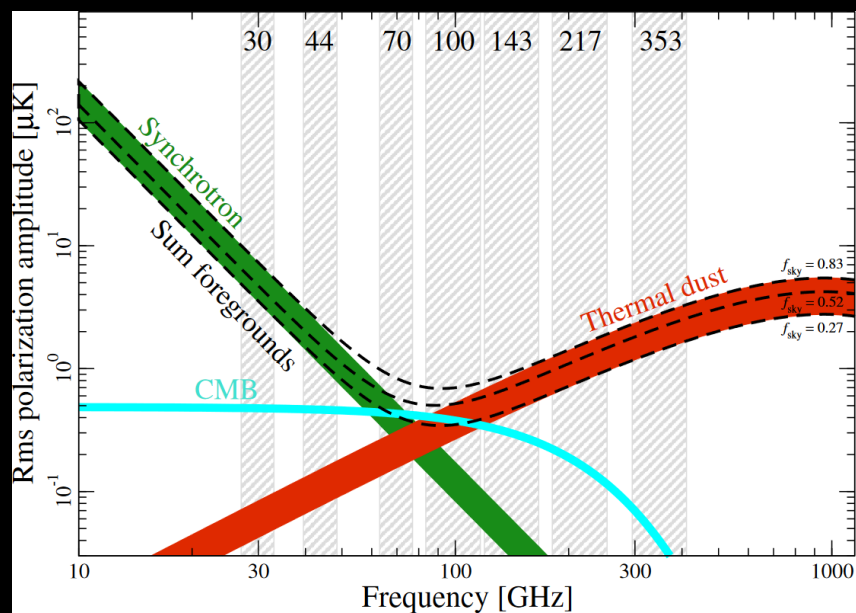
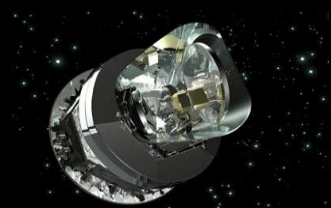
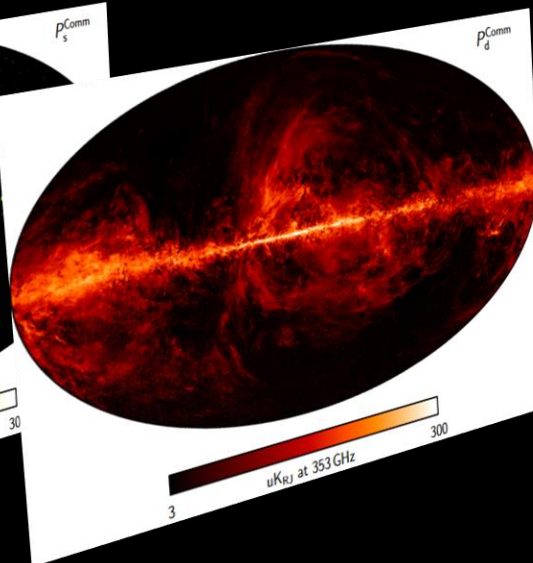
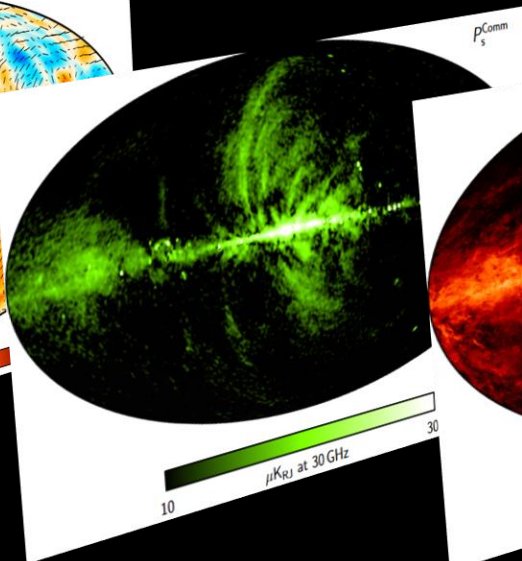
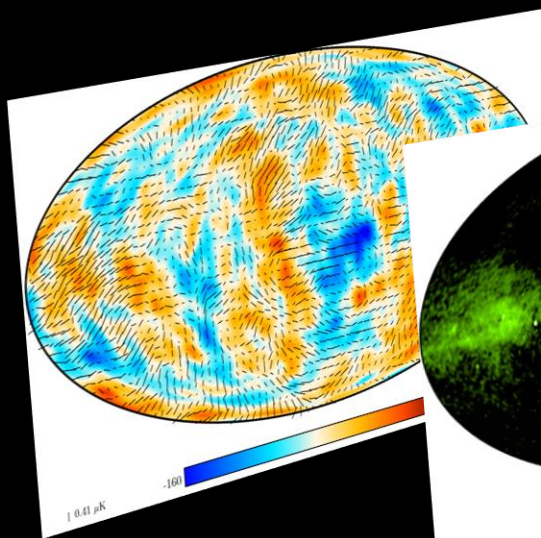
Dust



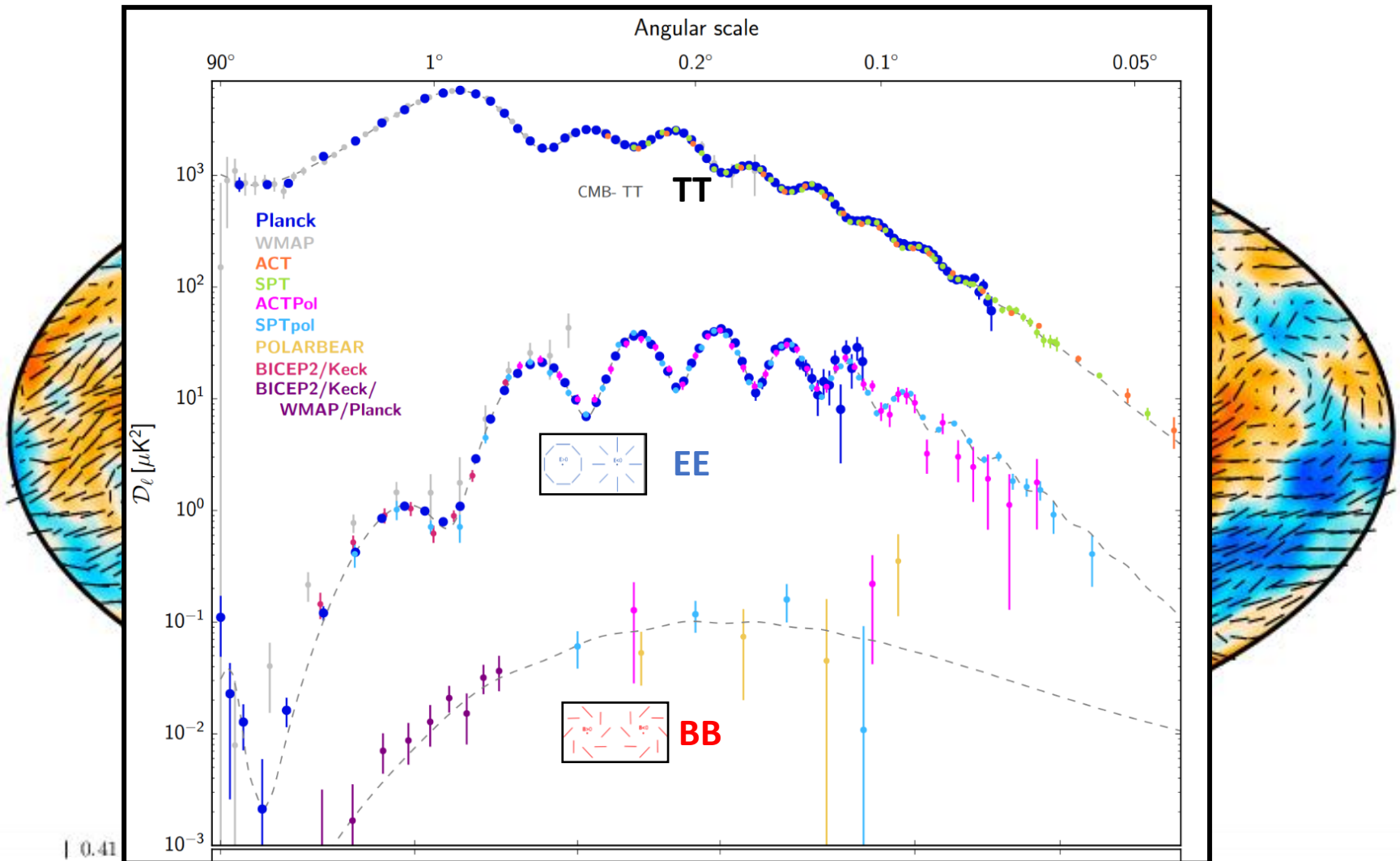
CMB

Synchrotron

Dust

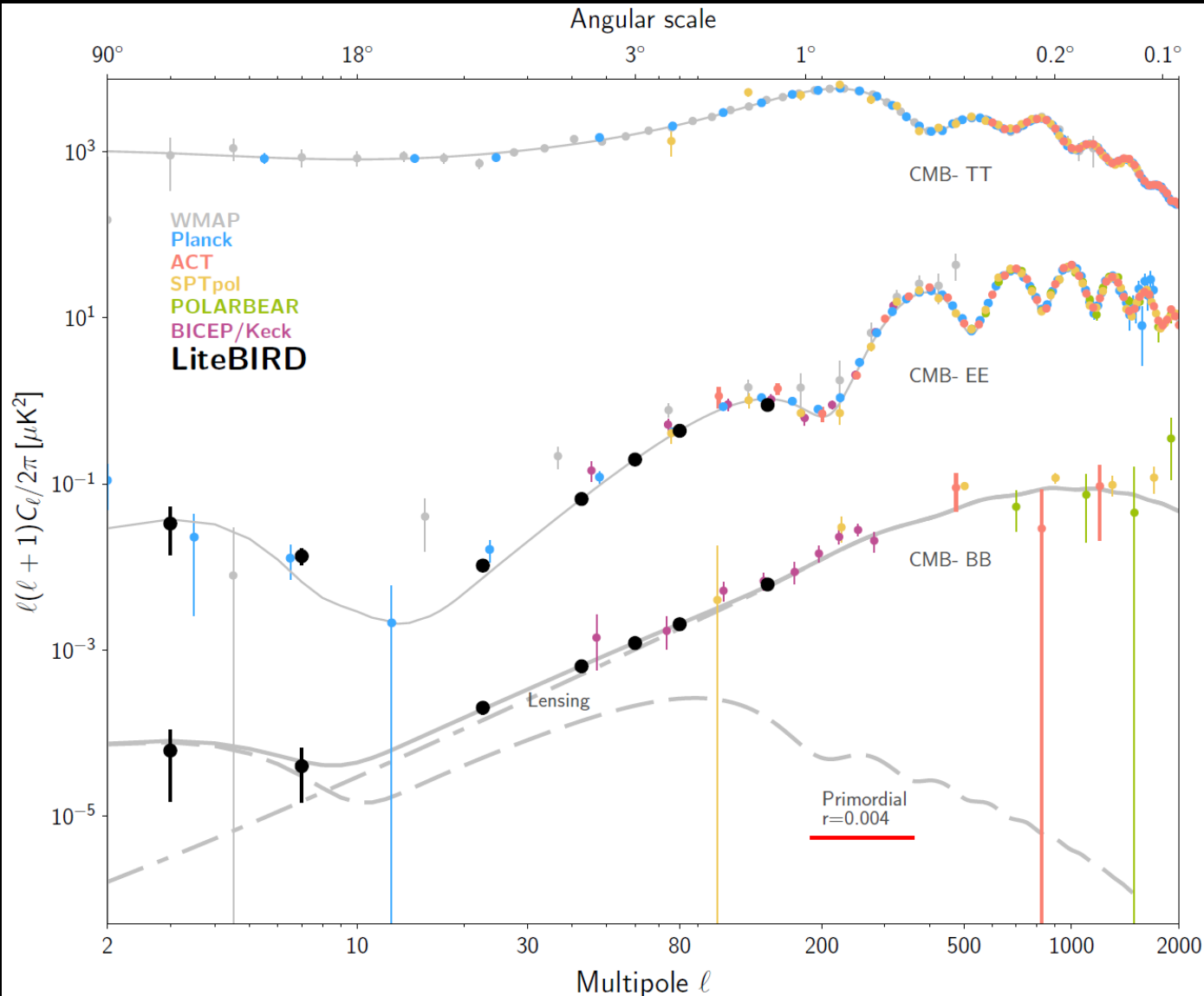


CMB polarization anisotropies



LiteBIRD

“Lite satellite for the study of B-mode polarization and Inflation from cosmic background Radiation Detection”



[LiteBIRD Coll
PTEP-arXiv:2202.02773]

Looking for Quantum Gravity imprints in the Universe

Brief introduction to the current search for Quantum Gravity imprints in the early Universe:

- Primordial Gravitational waves
- Cosmic Microwave Background Polarization

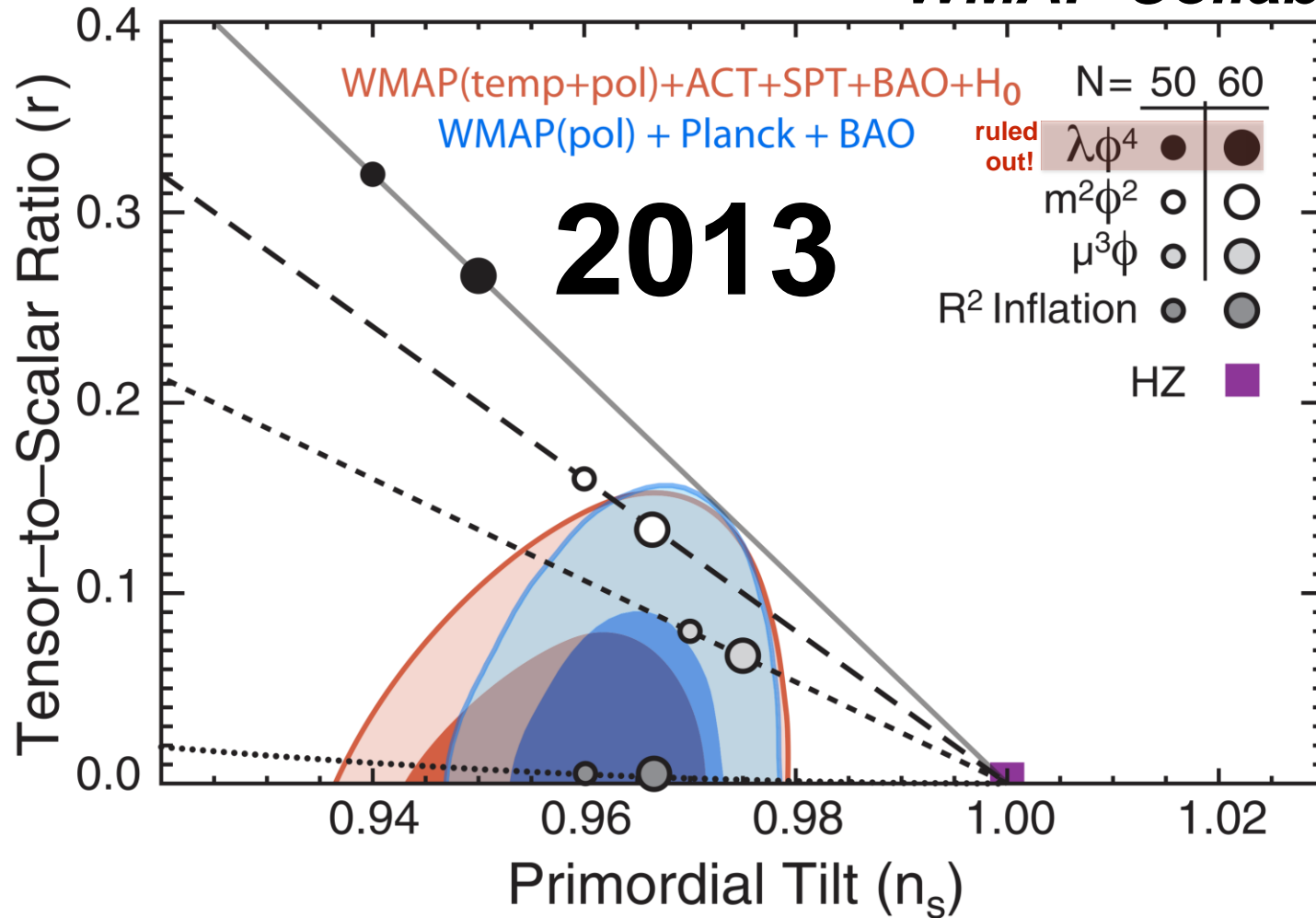
Looking for Quantum Gravity imprints in the Universe

Brief introduction to the current search for Quantum Gravity imprints in the early Universe:

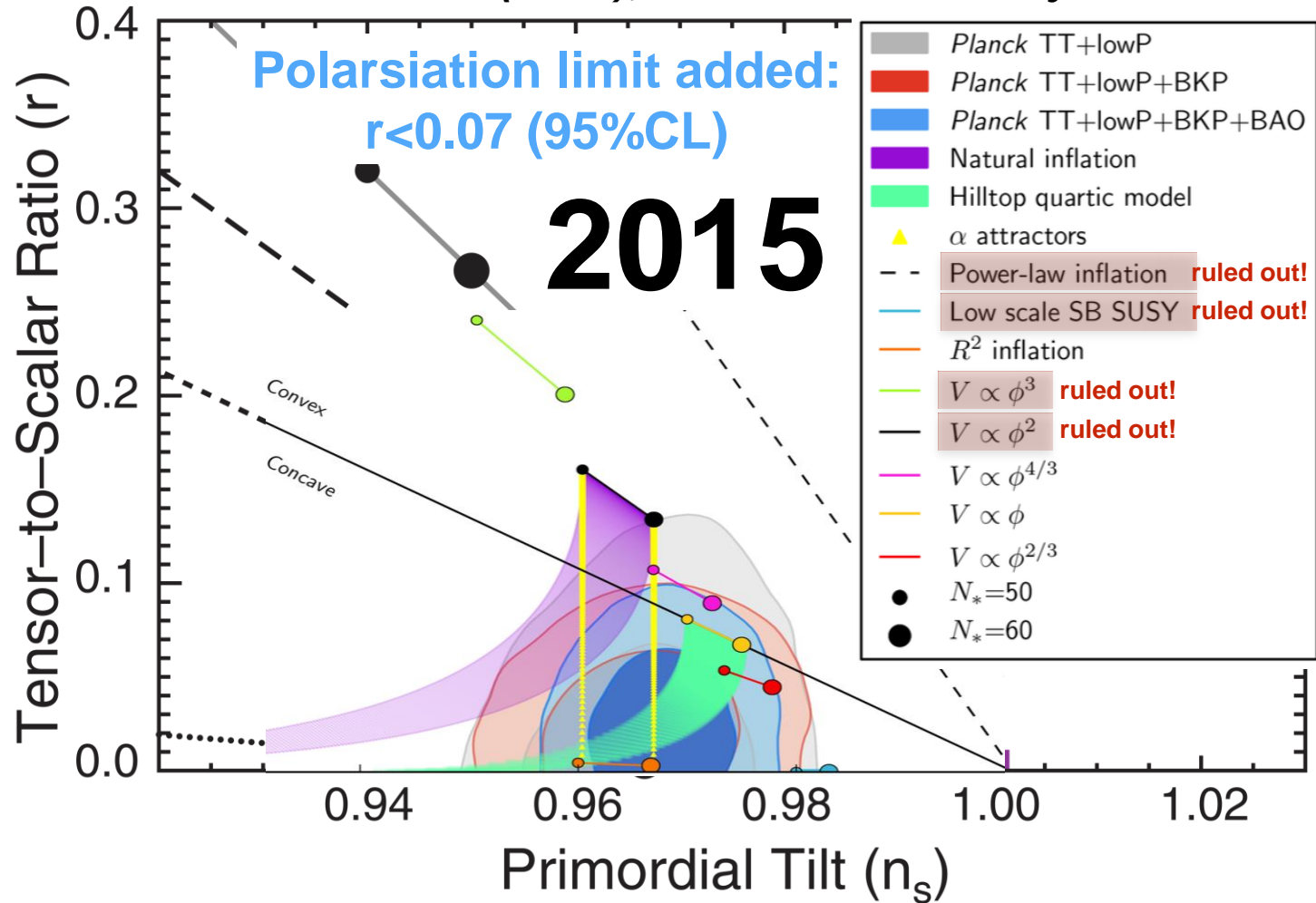
- Primordial Gravitational waves
- Cosmic Microwave Background Polarization

Detection of **CMB primordial B modes** induced by **primordial gravitational waves** would constitute a glimpse of **Quantum Gravity at work** (10^{-38} seconds after the singularity).

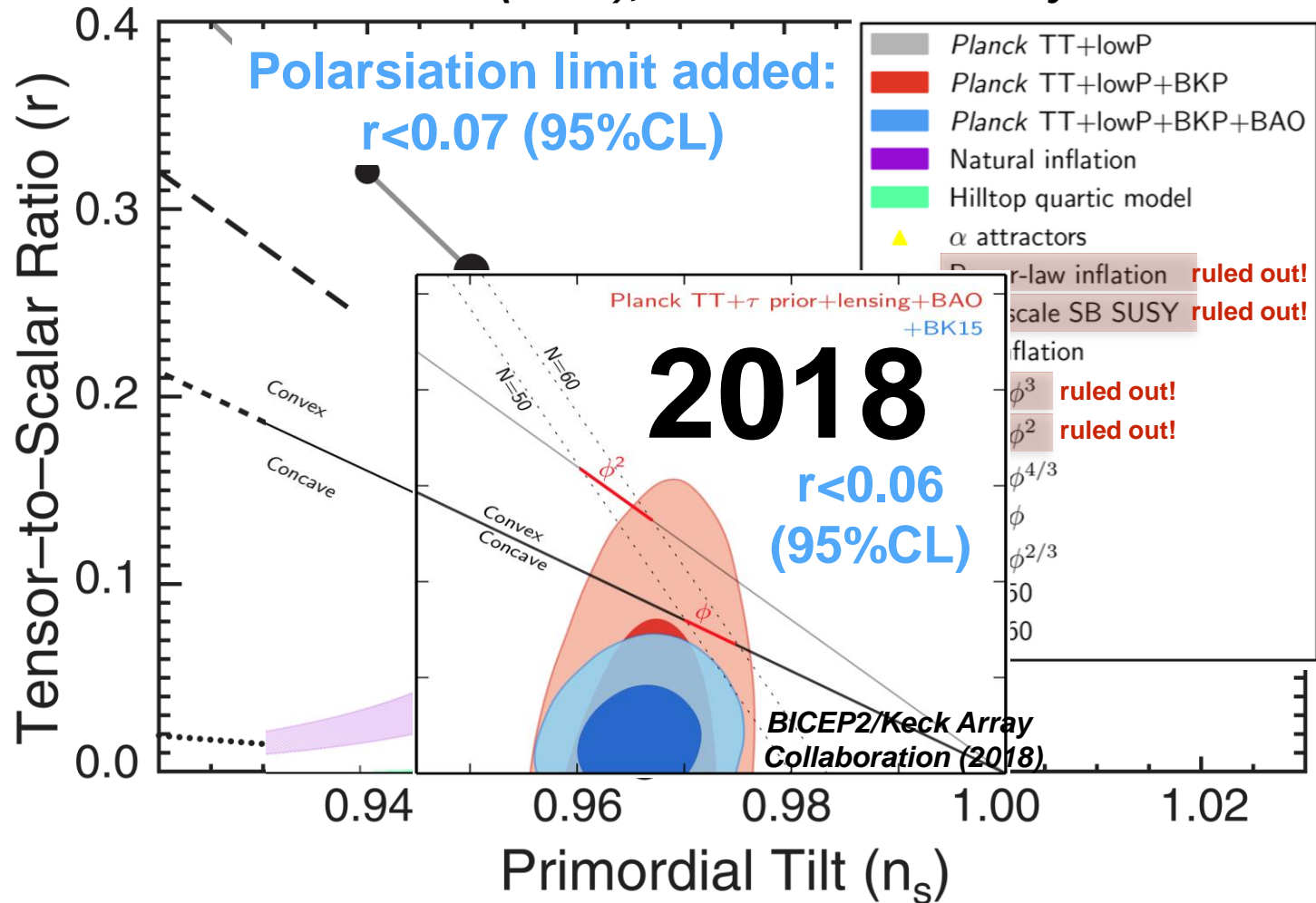
- *[II part → A short theoretical introduction to QG Gabriele Gionti, SJ]*



Planck Collaboration (2015); BICEP2/Keck Array Collaboration (2016)



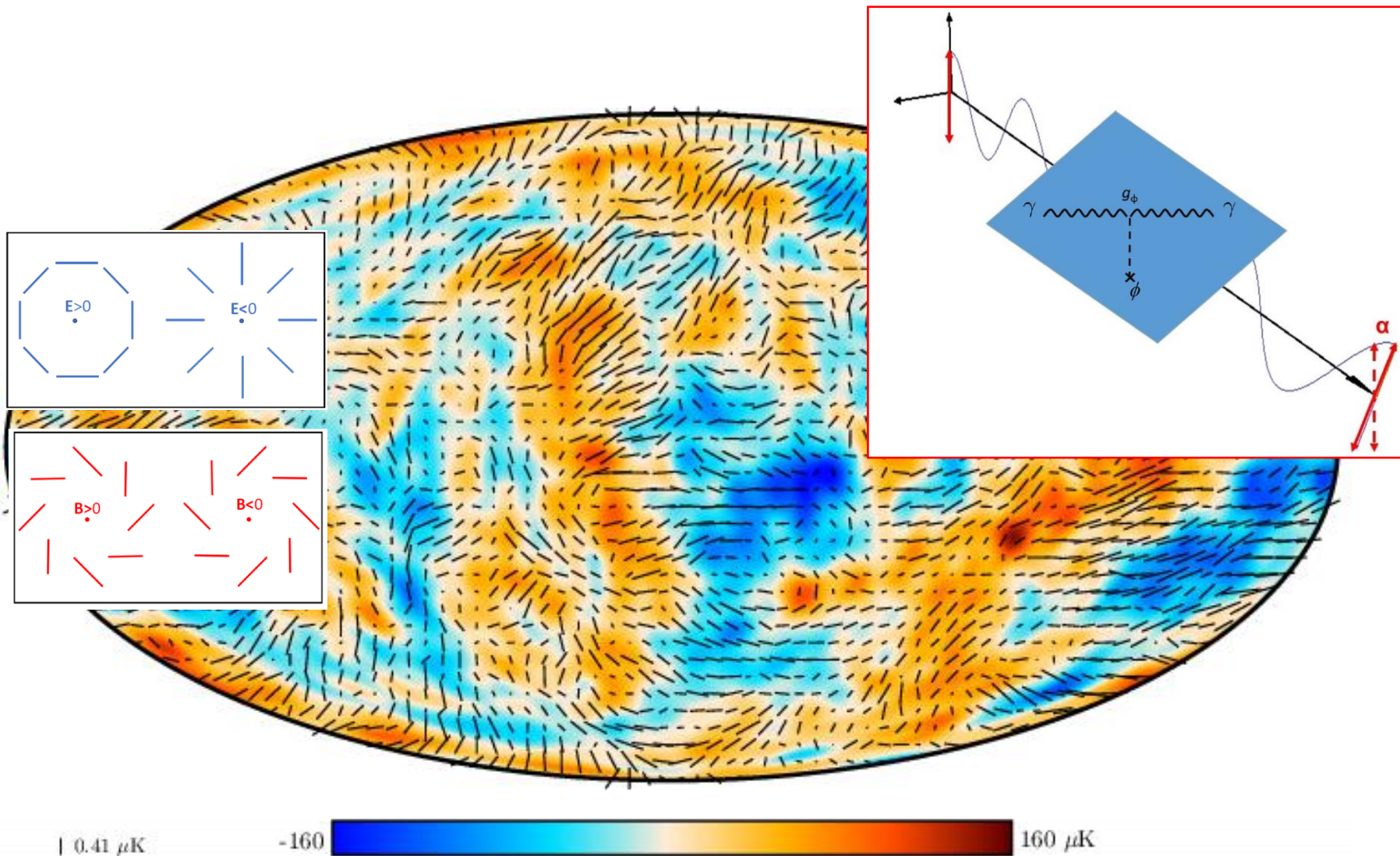
Planck Collaboration (2015); BICEP2/Keck Array Collaboration (2016)



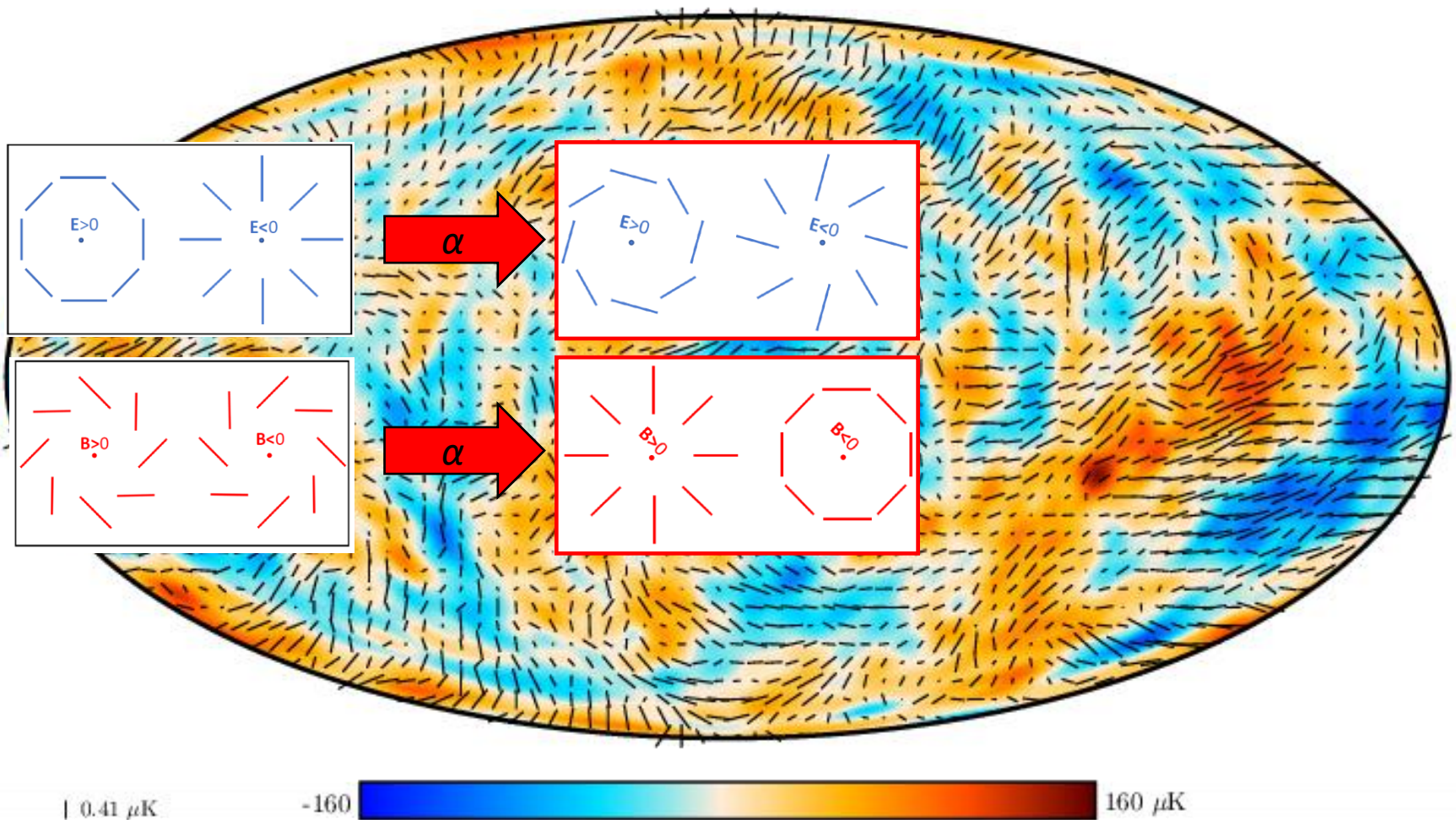
**Polarisation limit added:
 $r < 0.07$ (95%CL)**



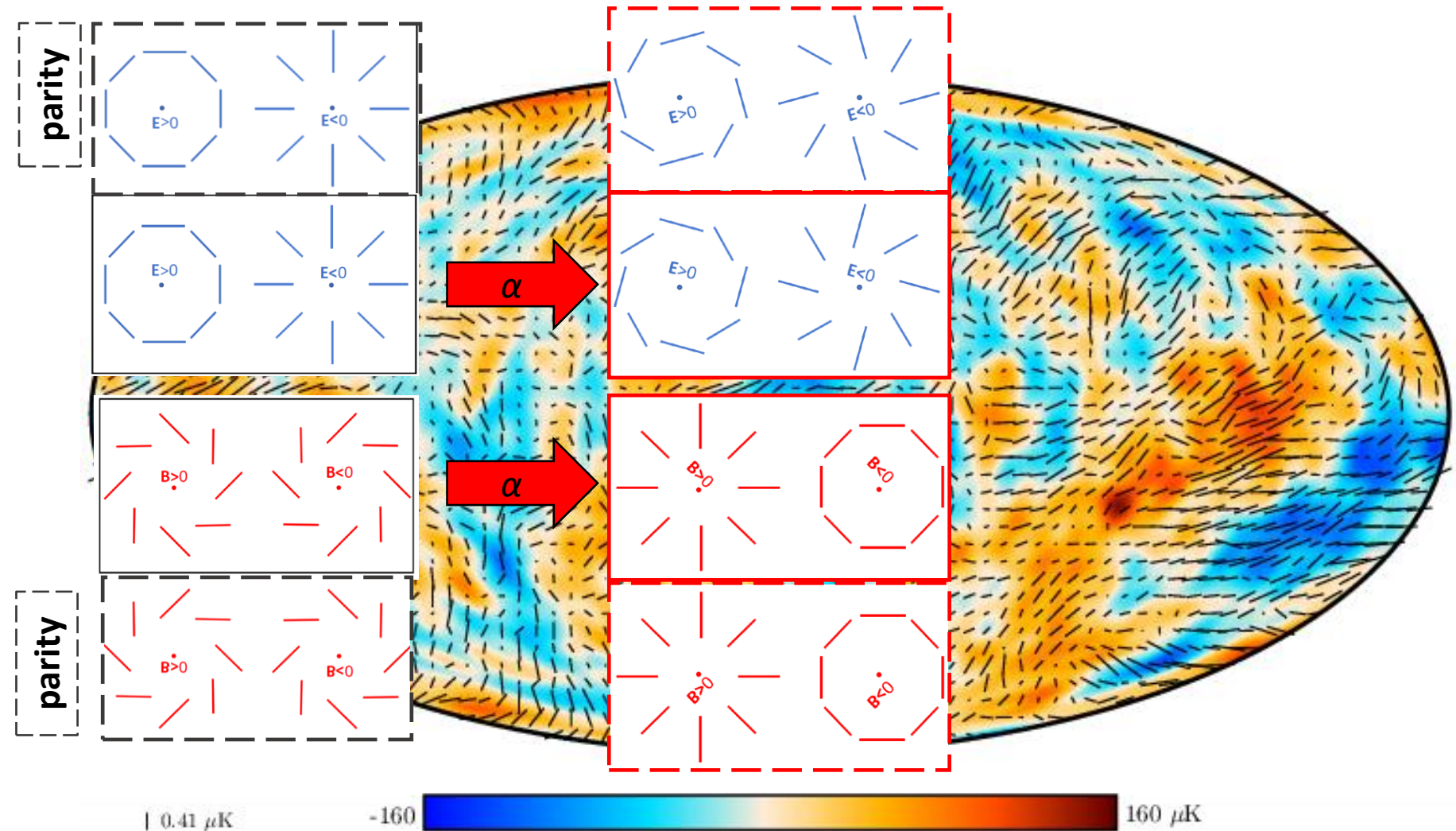
Cosmological birefringence



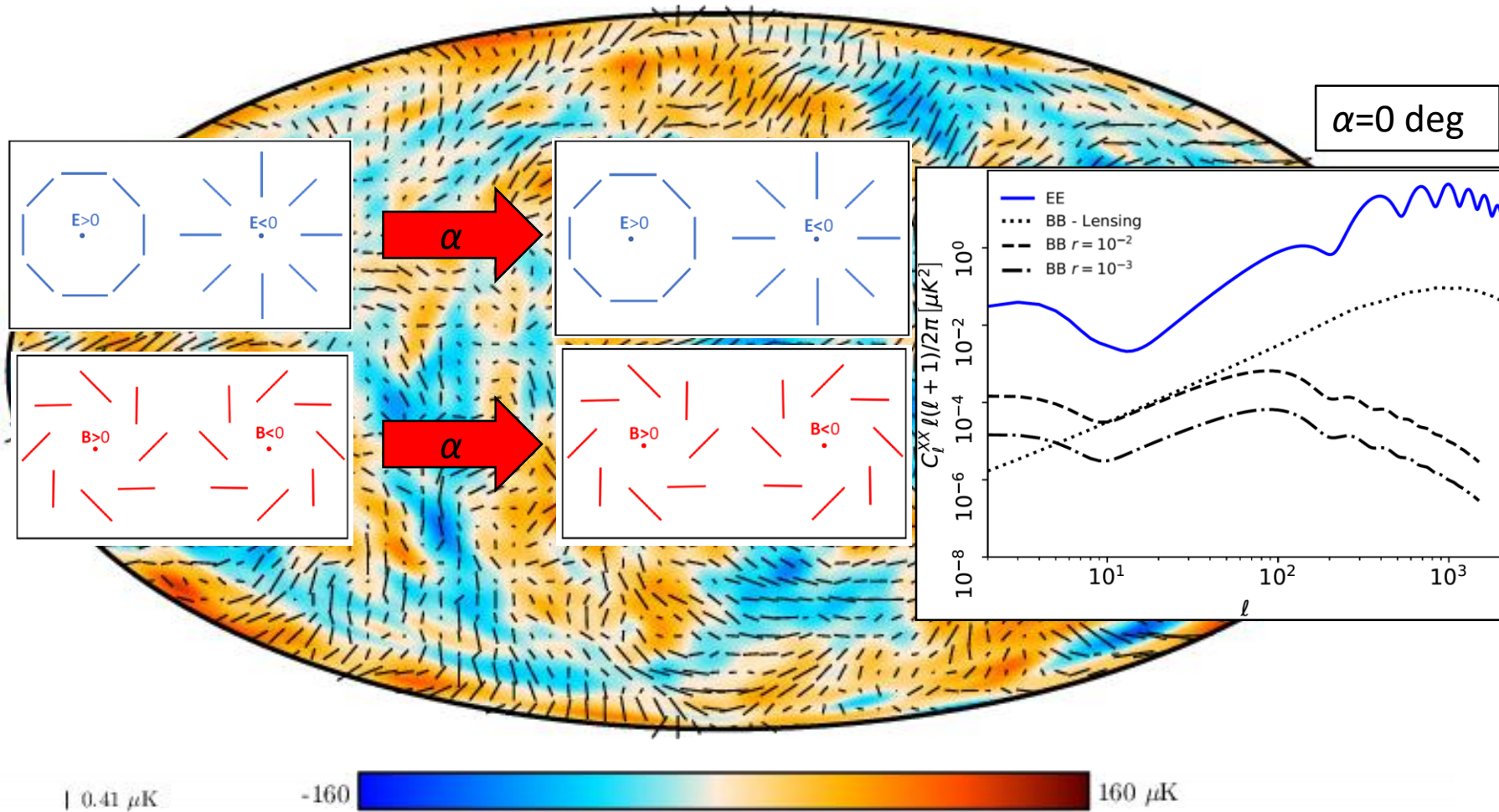
Cosmological birefringence



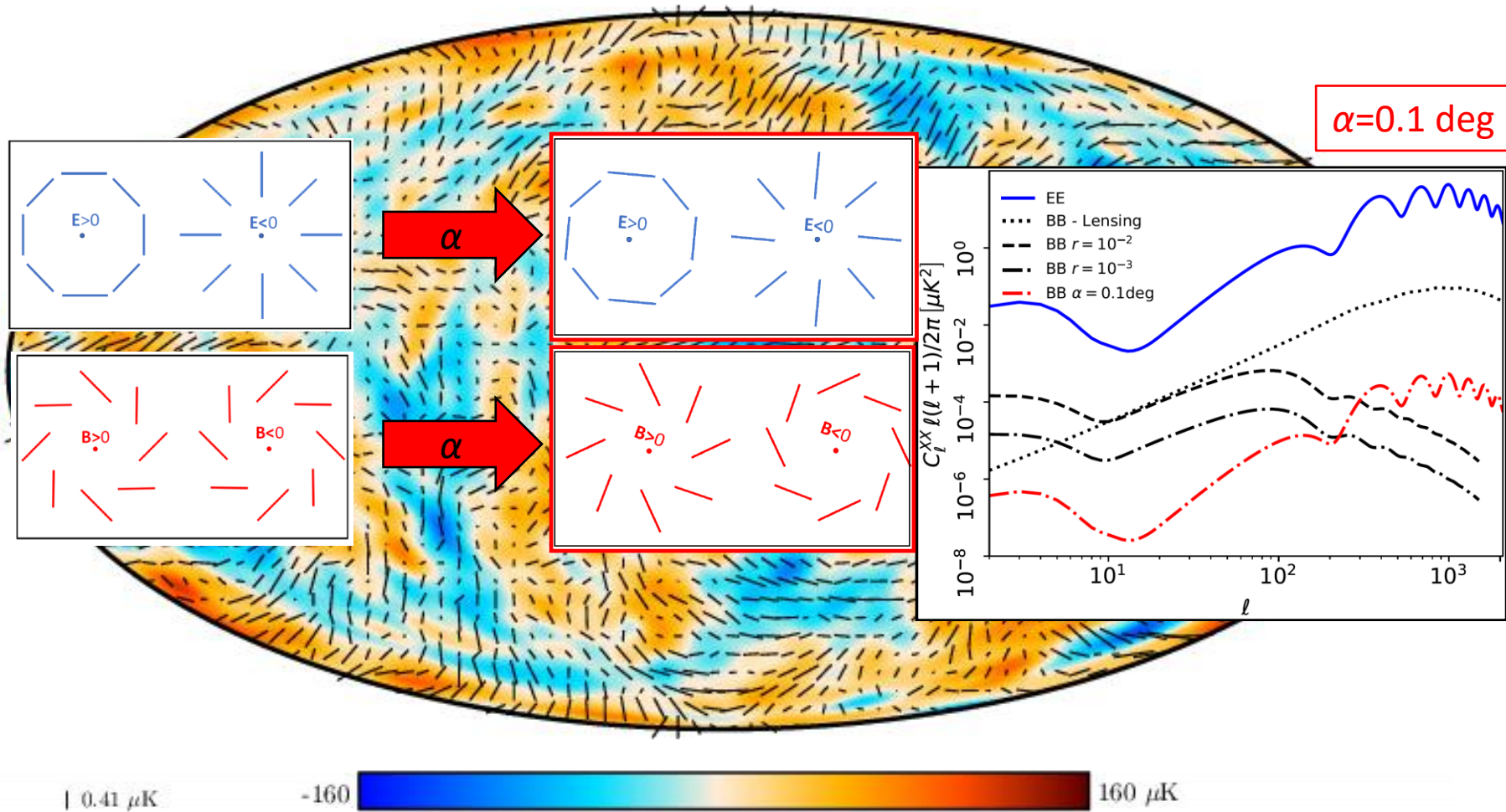
Cosmological birefringence



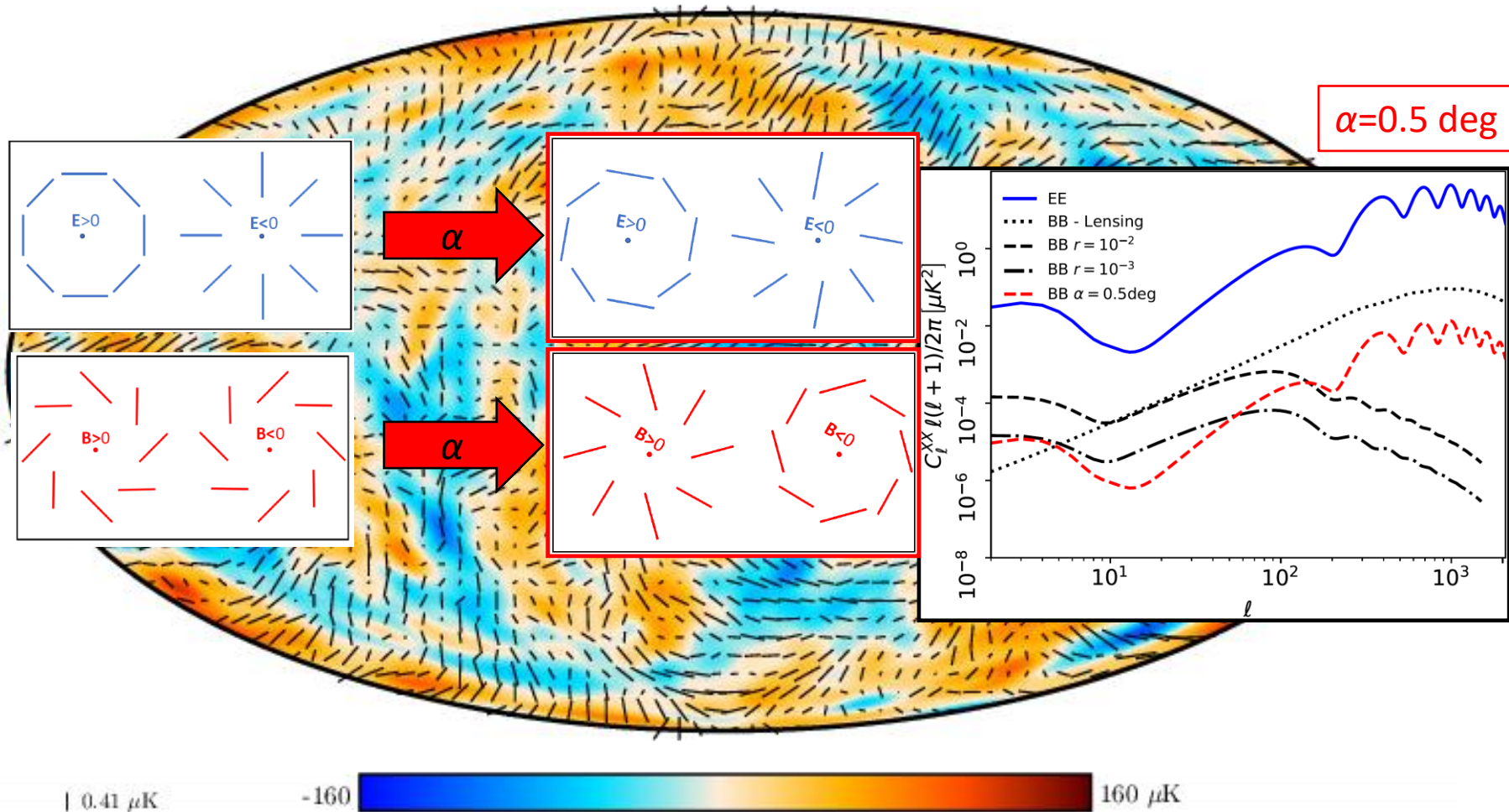
CMB polarization anisotropies



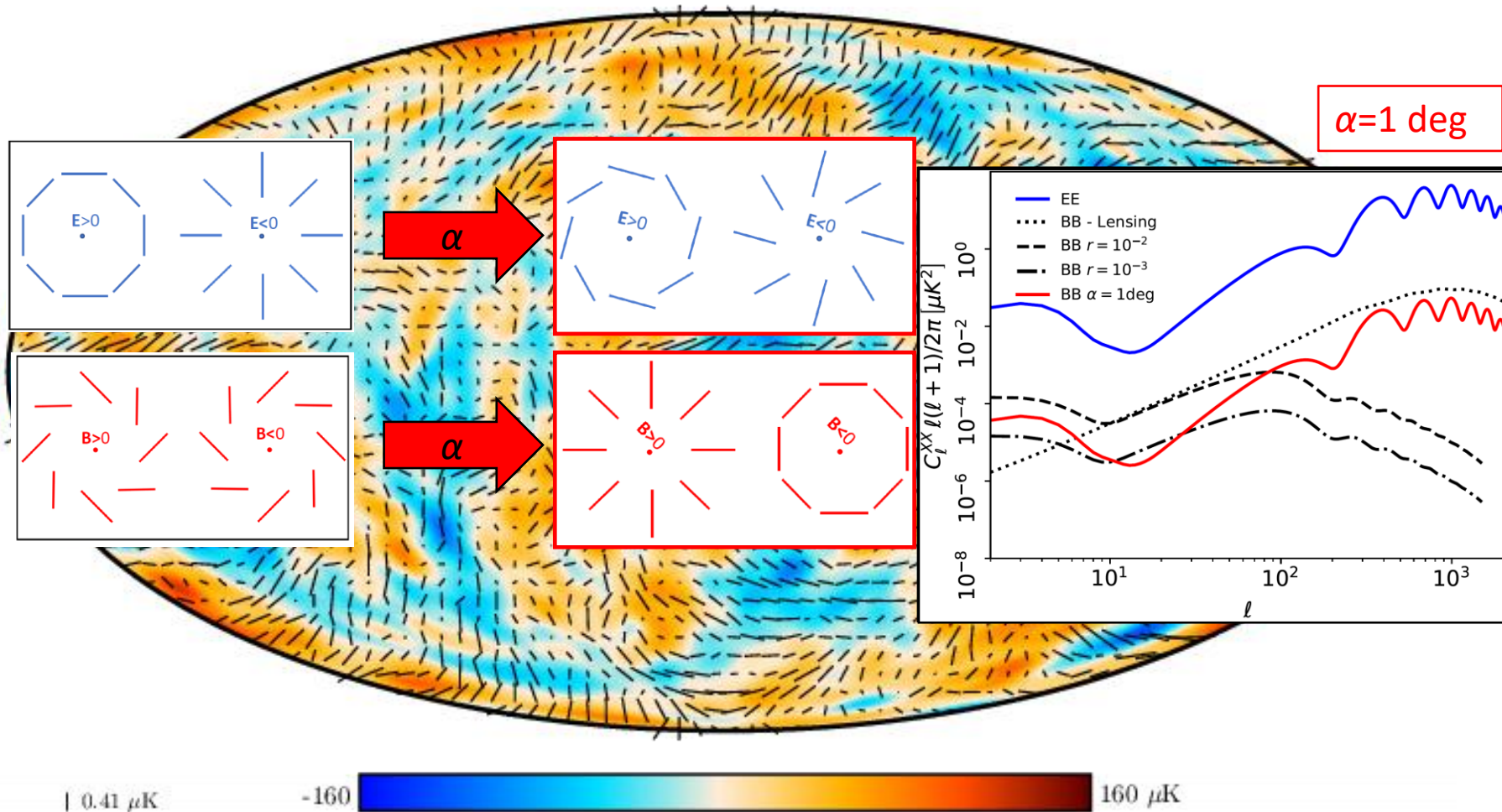
CMB polarization anisotropies



CMB polarization anisotropies



CMB polarization anisotropies



A SHORT INTRODUCTION TO QUANTUM GRAVITY

Gabriele Gionti, S.J.



SPECOLA VATICANA



SCIENCE AND THEOLOGY

-A STUDY PROGRAM FOR FUTURE THEOLOGIAN-

The Quantum Gravitational Challenge in Modern Cosmology

Pontifical Lateran University Rome, October 21 2022.

OUTLINE

- Brief introduction to Einstein's Theory of General Relativity.
- Canonical Quantum Gravity and Loop Quantum Gravity.
- String Theory
- Asymptotically Safe Approach to Quantum Gravity
- Conclusions



1915

“Annus Mirabilis” !



***David Hilbert:
Action of the Gravitational Field***



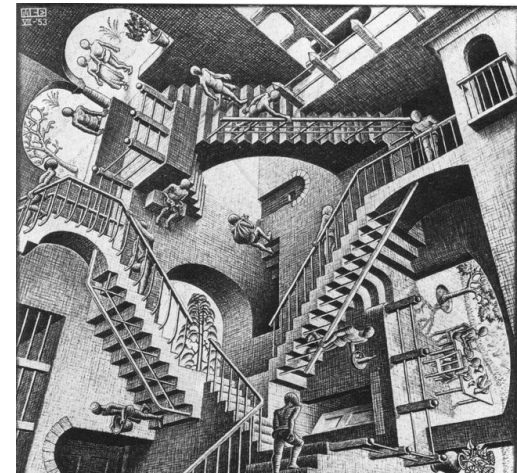
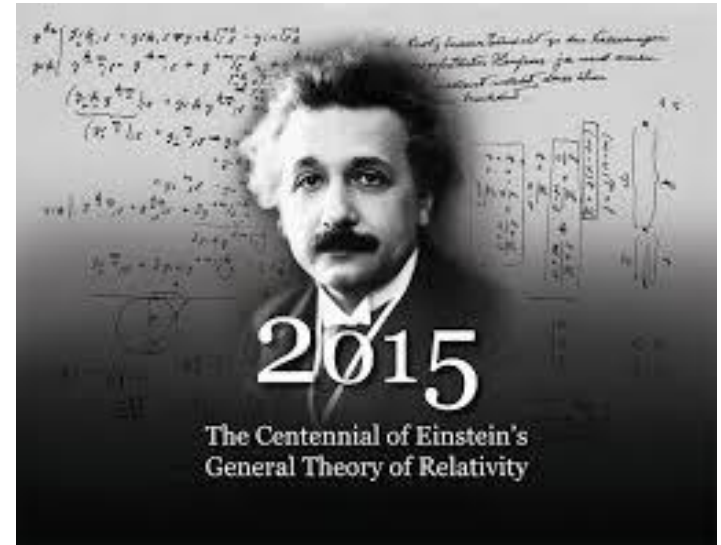
***Emmy Noether:
Conservations Laws***

GENERAL RELATIVITY

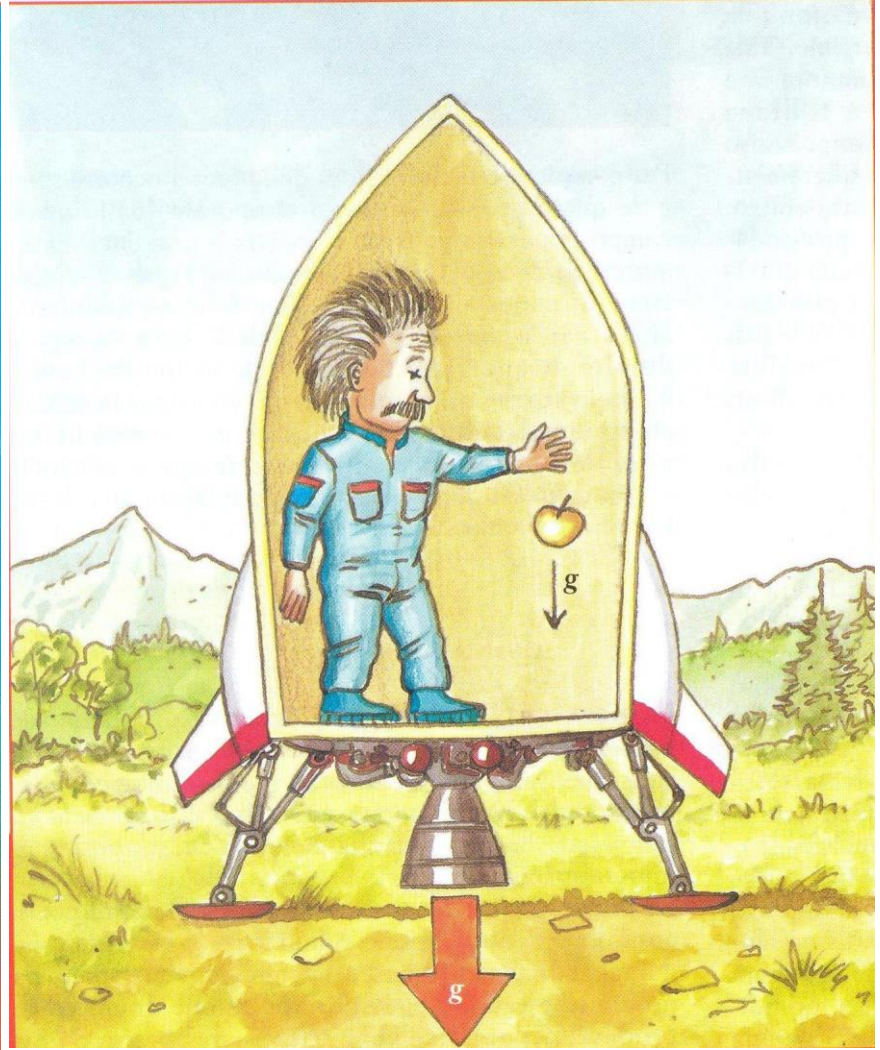
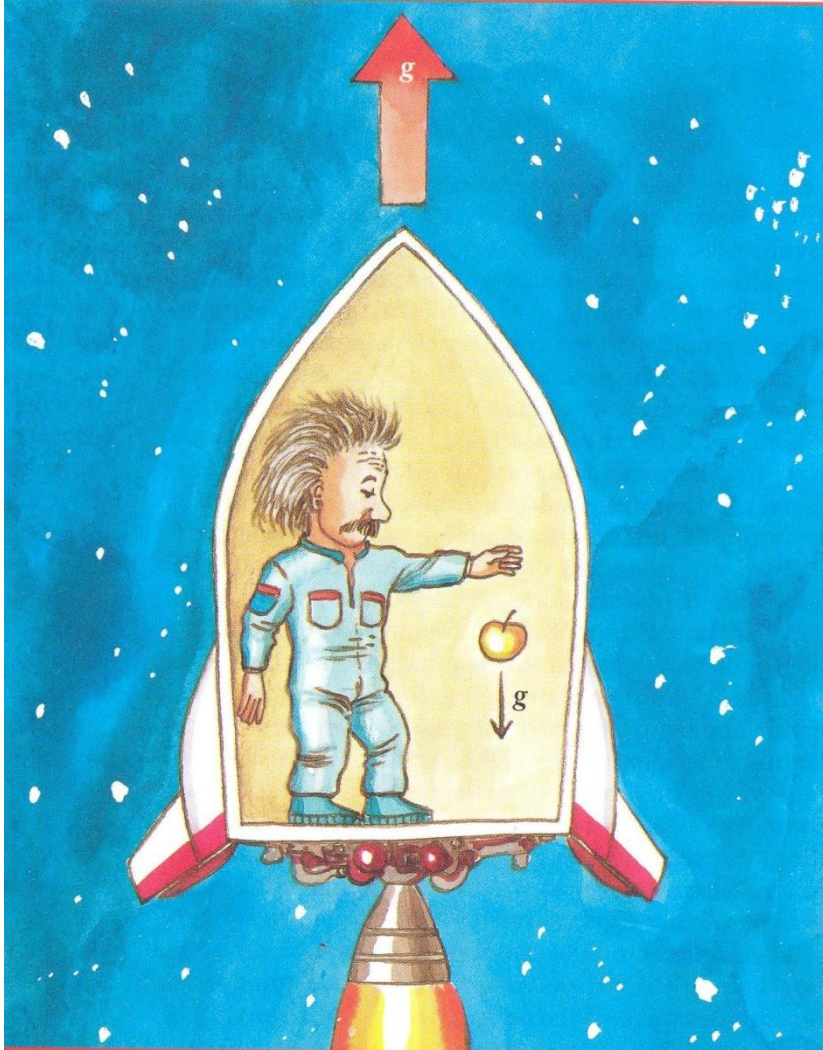
- “Extension” of Special Relativity.
- Deal with “non-inertial frames”
(case in which the frame “relative” velocity
is not constant).
- One fundamental principle:
The principle of equivalence “the mass equivalence”

$$m_g = m_i$$

- The gravitational effects are locally indistinguishable from the
acceleration effects.



Gravity and Acceleration



Gravity and Acceleration



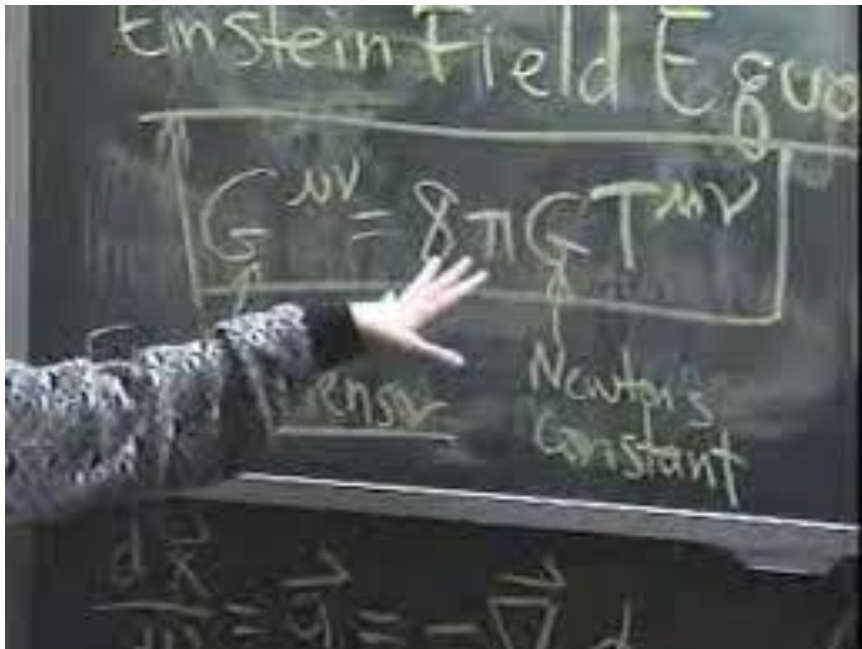
An astronaut will experience no weight in a free-falling starship in the empty space. The free-falling starship cancels the gravitational effects.

GENERAL RELATIVITY

- Alternative version of the Principle of Equivalence
- The “Covariance Principle”: the Laws of Physics are the same (covariant) in every reference frame! (therefore also non inertial..)

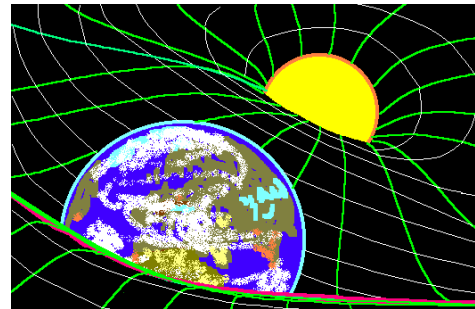
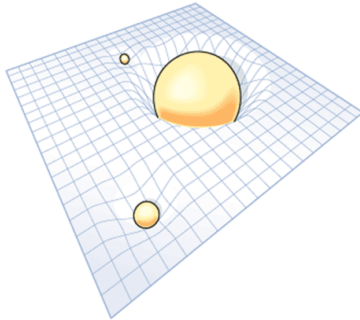
1) The physical laws agrees with Special Relativity in the absence of gravitation

2) The equations are generally covariant; they are preserved, in form, under arbitrary transformations of coordinates.



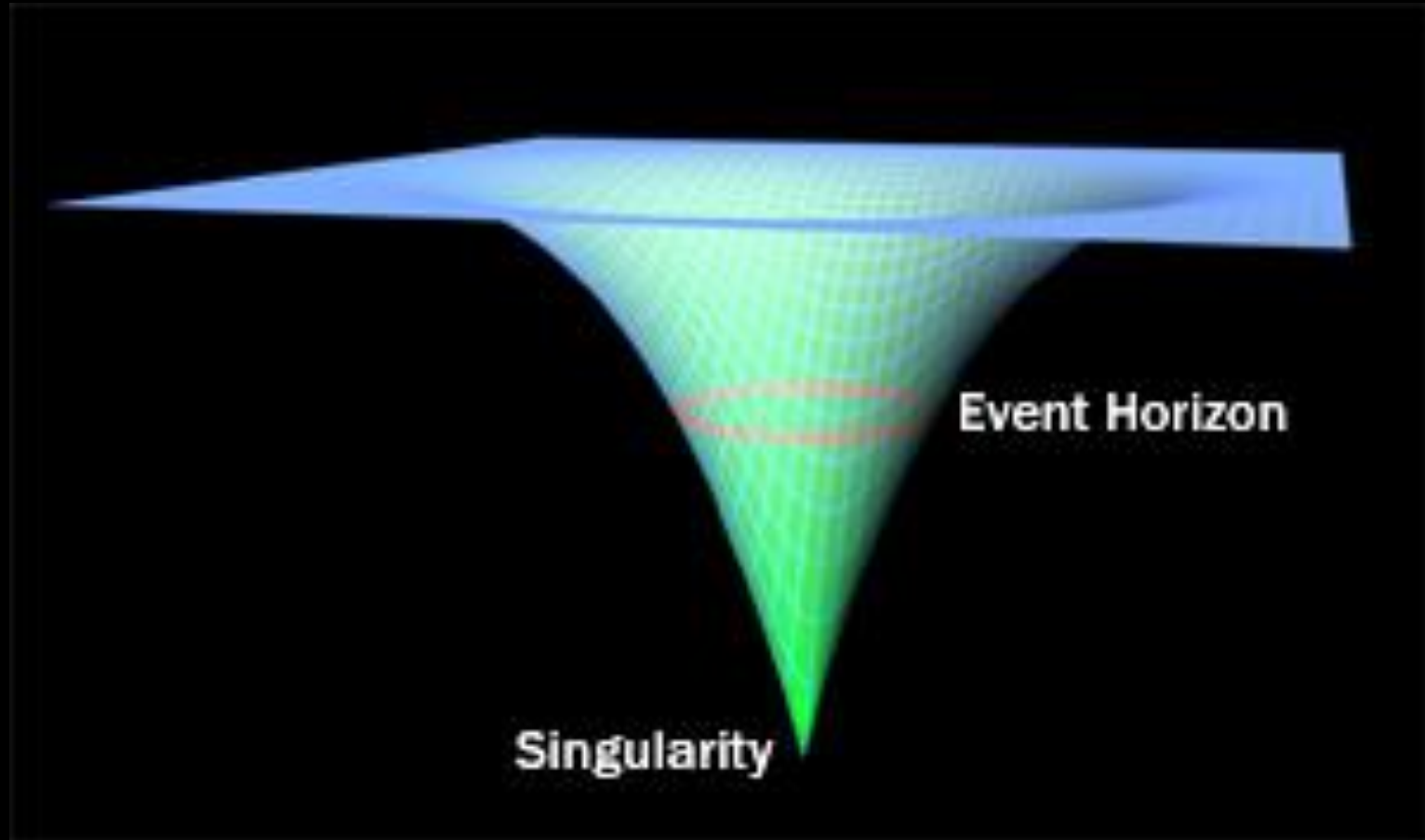
GENERAL RELATIVITY

- The Space-Time is a “physical entity”; it is a dynamical entity that is modified by the presence of massive bodies (as well as Energy).
- The massive bodies modify Space-Time, which gains curvature.



- Free falling bodies moves on the analogous of straight line, in inertial reference frames, which are called geodesic lines.
- The gravitational force is not, anymore, an action at distance; it is a field theory like in electromagnetism.

SINGULARITY IN EINSTEIN'S GENERAL RELATIVITY



Why Quantum Gravity?

$$\text{Planck Temperature} = \sqrt{\frac{\hbar c^5}{G k_B^2}} = 1.42 \times 10^{32} \text{ K}$$

$$\text{Planck Mass} = \sqrt{\frac{\hbar c}{G}} = 2.2 \times 10^{-8} \text{ kg}$$

$$\text{Planck Time} = \sqrt{\frac{G \hbar}{c^5}} = 5.4 \times 10^{-44} \text{ s}$$

$$\text{Planck Length} = \sqrt{\frac{G \hbar}{c^3}} = 1.6 \times 10^{-35} \text{ m}$$

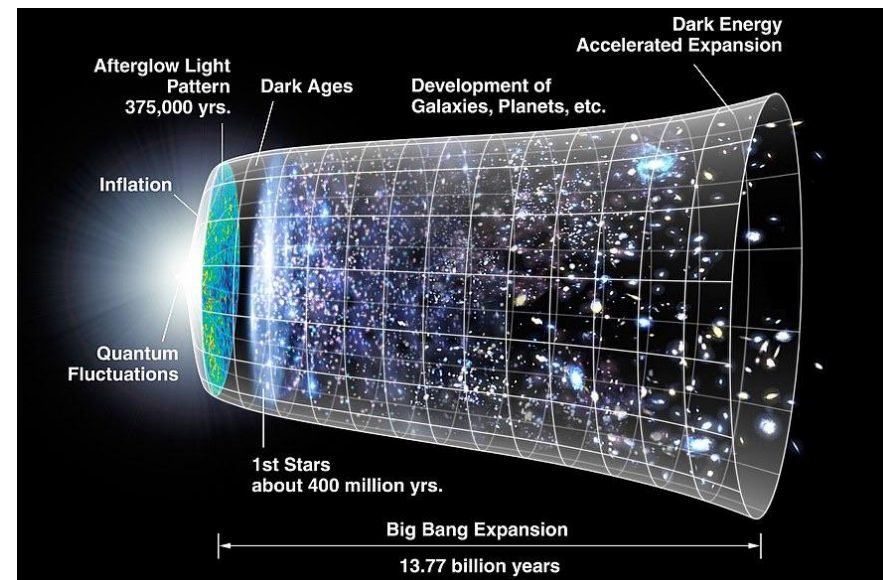
$$\text{Planck Energy} = \sqrt{\frac{\hbar c^5}{G}} = 1.22 \times 10^{19} \text{ GeV}$$

$$\text{Planck Density} = \frac{c^5}{G^2 \hbar} = 5.16 \times 10^{93} \text{ g/cm}^2$$

- All fundamental interactions have a quantum field theory behavior, then there could emerge a contradiction when we couple them to Gravity

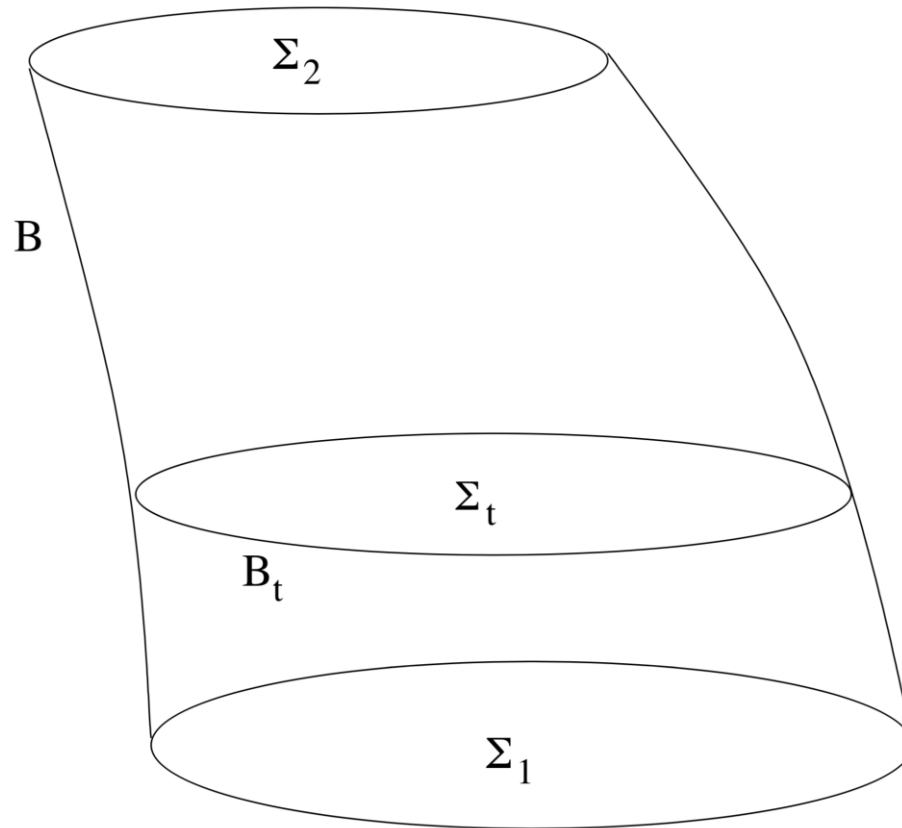
QUANTUM GRAVITY

- Einstein General Relativity is considered successful phenomenological theory at laboratory, solar system, galactic, for length scales $l \gg l_{\text{Pl}}$ ($=$ Planck length) $\equiv 1/\sqrt{G} \approx 10^{-33} \text{ cm}$
- Singularity problem and the quantum mechanical behaviour of matter-energy at small distance suggest a quantum mechanical behaviour of the gravitational field (Quantum Gravity) at small distances (High Energy).
- Many different approaches to Quantum Gravity: String Theory, Loop Quantum Gravity, Non-commutative Geometry, Causal Dynamical Triangulations, Asymptotic Safety etc.
- General Relativity is considered an effective theory. It is not perturbatively renormalizable (the Newton constant G has a $(\text{length})^{-2}$ dimension)



CANONICAL QUANTUM GRAVITY

(non-perturbative)



CANONICAL QUANTUM GRAVITY



It is one of the oldest approach in Quantum Gravity



It is based on ADM (Arnowit, Deser and Misner) technique: a three-dimensional space-like surface evolving in time.



The goal is to write a Hamiltonian density functional of the gravitational field.



This can be done and one can write the Wheeler-DeWitt equation for the wave-function of the Universe.



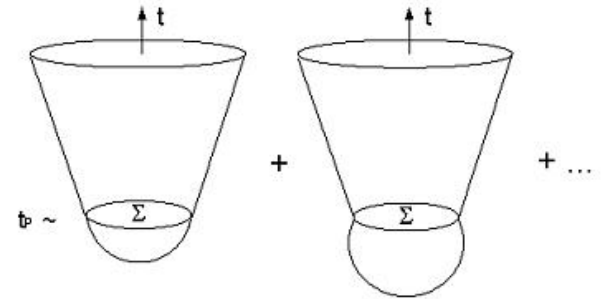
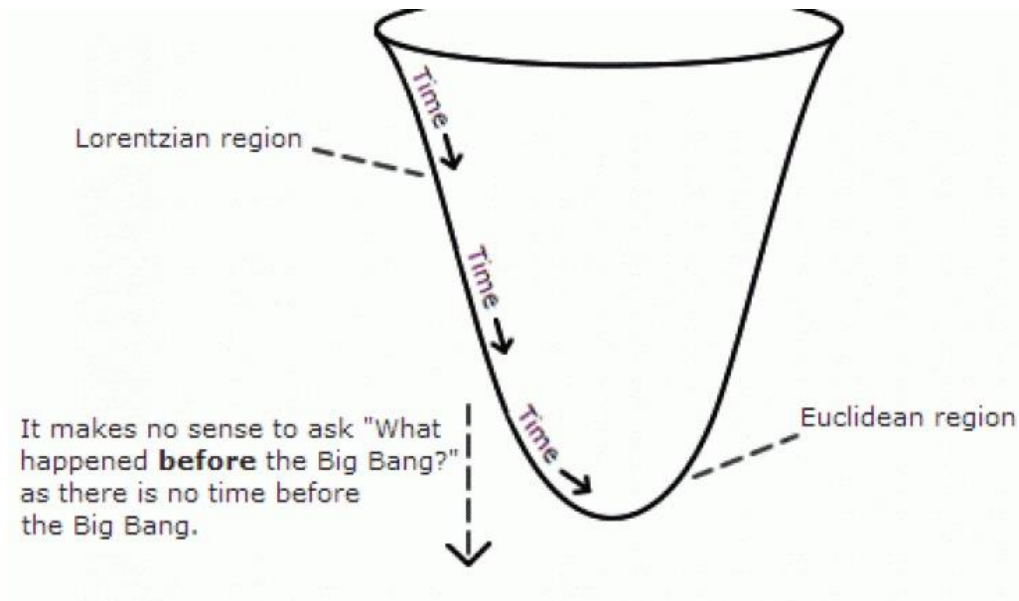
It is difficult to solve except in very particular cases called "mini-superspace" models of Quantum Cosmology.

$$\hat{H}\Psi = 0$$

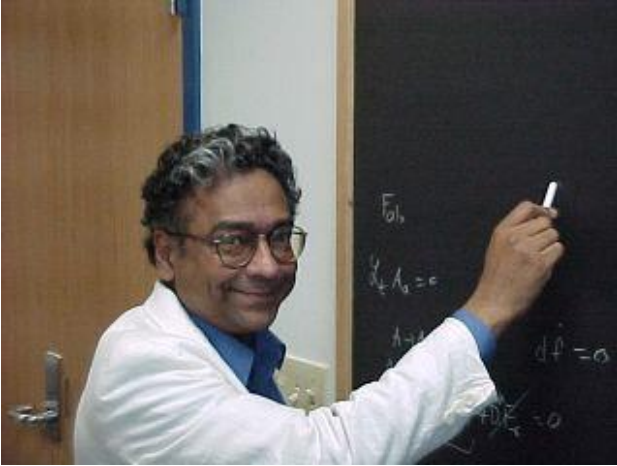
The wave function of the Universe gives a probability distribution for a certain stage of our universe, e.g., a probability before inflation.

CANONICAL QUANTUM GRAVITY

- Hartle-Hawking proposal: no-boundary-boundary proposal.
Solution of Wheeler-DeWitt equation for FLRW minisuperspace model



LOOP QUANTUM GRAVITY



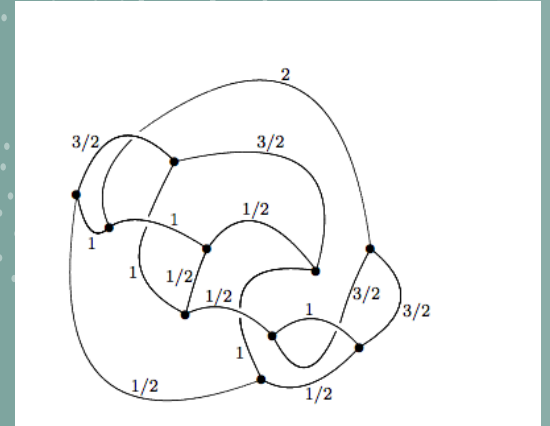
Abhay Ashtekar



Lee Smolin



Carlo Rovelli



SPIN NETWORK

- A VERSION OF CANONICAL QUANTUM GRAVITY IN THE ASHTEKAR'S VARIABLES

For any curve $\gamma : [0, 1] \rightarrow \Sigma$, consider the holonomy

$$U_\gamma(s_1, s_2) = P \exp \left\{ - \int_{s_1}^{s_2} ds \frac{dx^i(s)}{ds} A_i^{\hat{I}} \tau_{\hat{I}} \right\},$$

where P denotes path ordering. Then for a closed curve, the “Wilson loop” $\text{Tr } U_\gamma(0, 1)$ is gauge invariant. More generally, let Γ be a graph, and define a “coloring” as follows:

The area operator, for example, has eigenvalues of the form

$$A = 8\pi\gamma G \sum_i \sqrt{j_i(j_i + 1)},$$

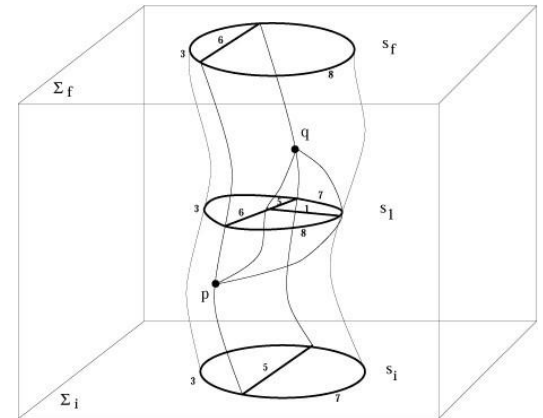
BLACK HOLE ENTROPY

- Bekenstein-Hawking formula:

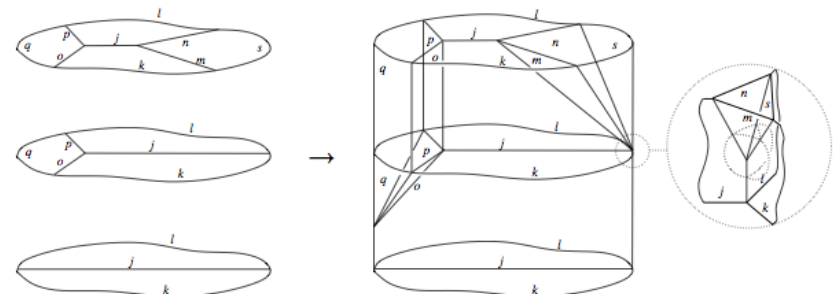
$$S_{BH} = \frac{A}{4L_P^2} = \frac{c^3 A}{4G\hbar}$$

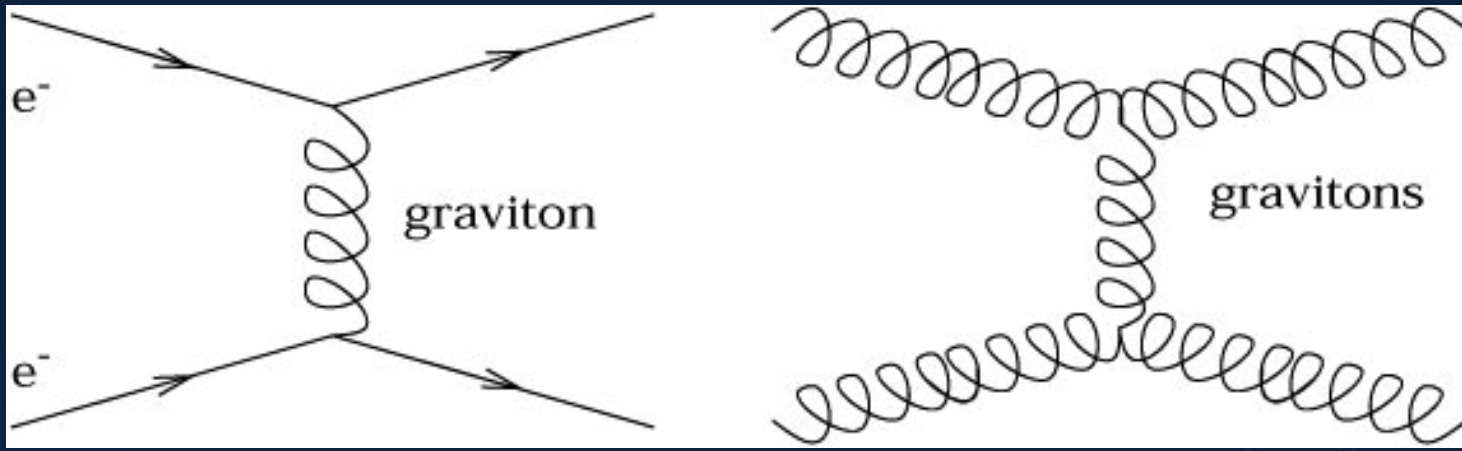
- The same formula can be derived from Loop Quantum Gravity starting with

$S = k \ln N(A)$, and the microstates are Spin networks intersecting the surface A



- Spin Foam (time evolution of Spin Networks)





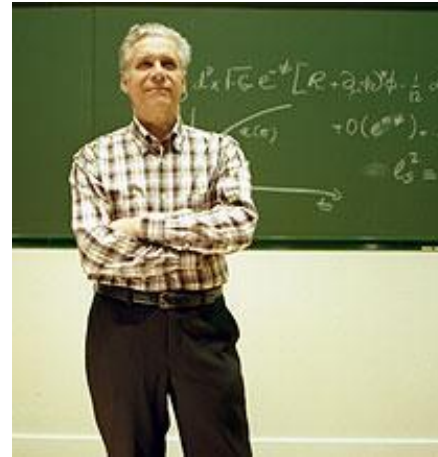
QUANTUM GRAVITY (via Path Integral)

- Quantized G.R. is perturbative non renormalizable. It is believed it is an effective theory valid for $l \gg l_{pl}$, rather than a fundamental (microscopic) theory valid at arbitrary small distances.
- In general, theories are fundamental if they are perturbatively renormalizable, if their infinities can be absorbed by re-defining only finitely many parameters (m , e , ...)
- Perturbative non-renormalizable theories: increasing number of counter terms as the loop order increases. Infinite many parameters, no predictive power

STRING THEORY

- Gabriele Veneziano's formula in dual Model for Strong interactions:

Duality in s and t channel interchange of strong interactions



- Generalizations of Veneziano Model (Nielsen, Nambu, Susskind) and Relativistic String first appearance.

- Some problem with the model: needed 26 dimensions, states with negative energy (tachyons), massless spin-2 unknown states (later identified as gravitons)

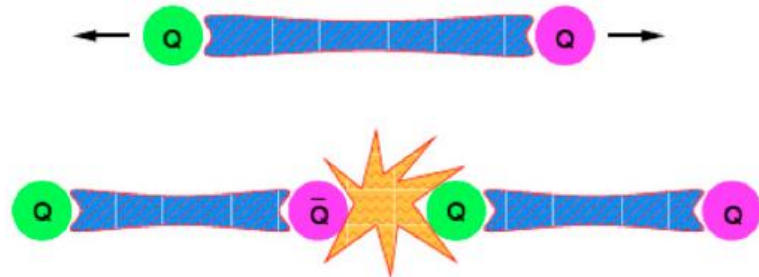
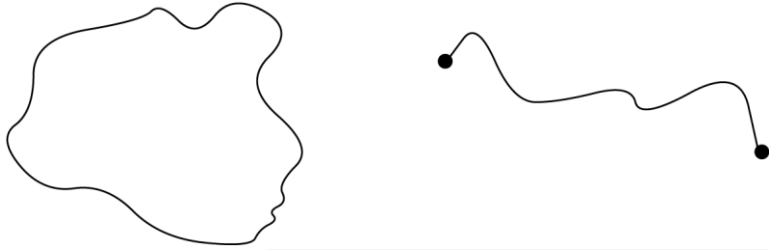


Figure 6: As quarks are pulled apart, eventually new quarks appear.

- A SU(3) Gauge theory (QCD) described better strong interactions

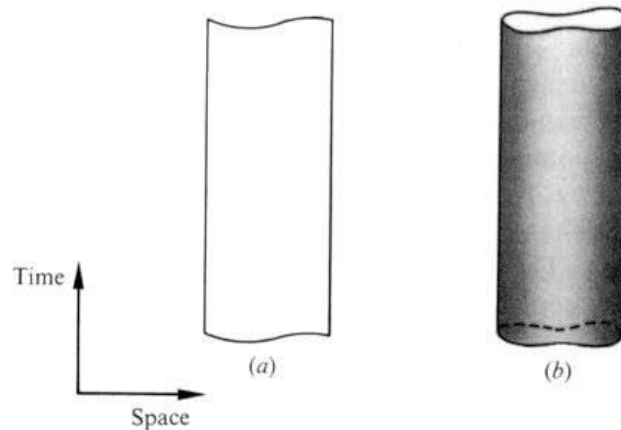
STRING THEORY



Polyakov action for Bosonic strings

$$I_{\text{str}} = \frac{1}{4\pi\alpha'} \int_S d^2\sigma \sqrt{-g} g^{ab} \partial_a X^\mu \partial_b X^\nu \eta_{\mu\nu}.$$

World-sheets for (a) open and (b) closed strings.

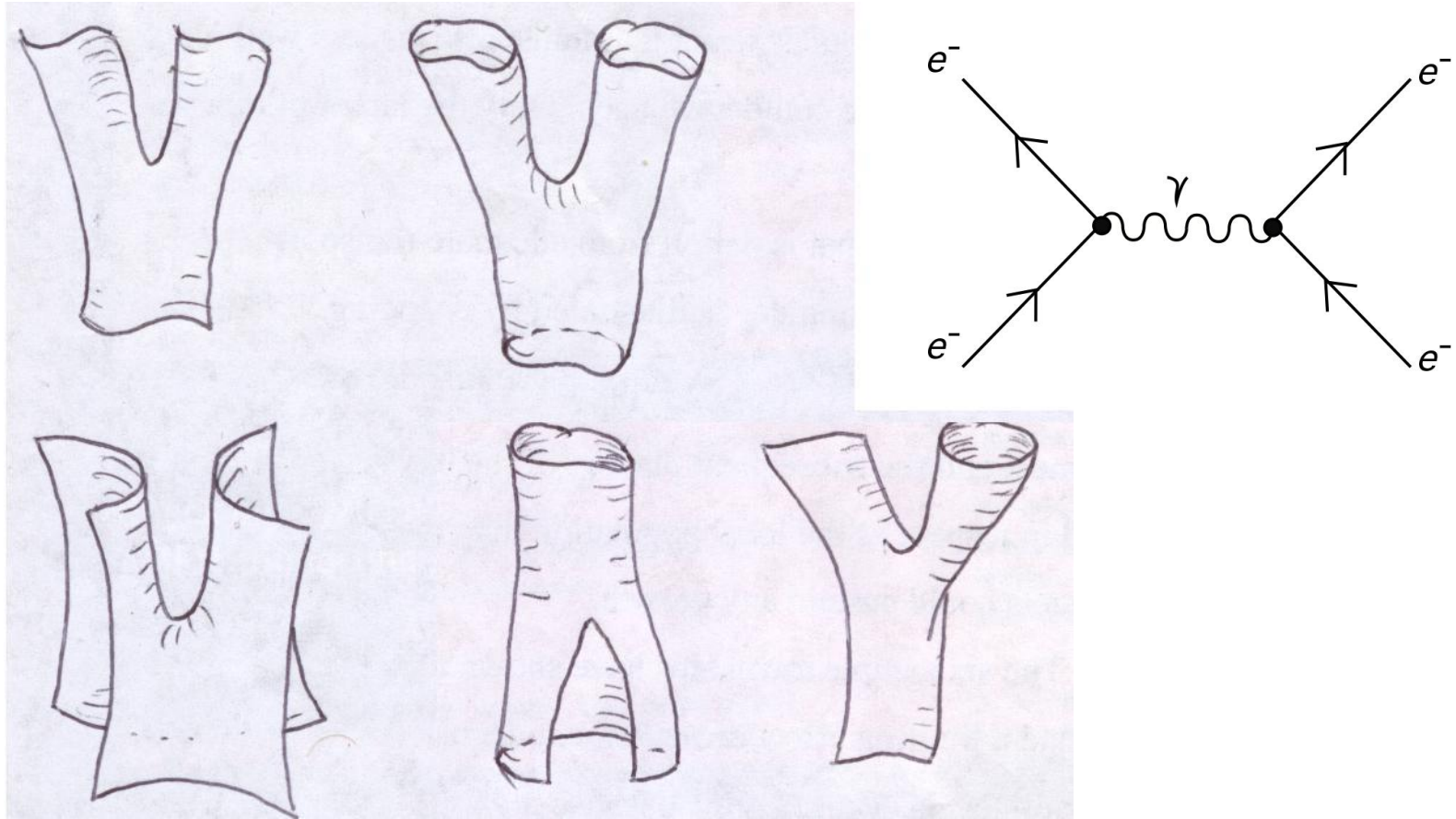


QUANTIZATION OF BOSONIC STRINGS

- One quantizes Bosonic String like any vector field in Quantum Field Theory (Expand the field in a Fourier base and impose commutation relations among the coefficients like the harmonic oscillator).
- Open and Closed Strings both have a tachyon (negative mass) in their quantum spectrum
- Closed Strings have a spin-two massless excited state and a massless scalar field called dilaton
- $d=26$ for consistency conditions
- The presence of tachyon makes Bosonic String Theory unstable

INTERACTIONS OF BOSONIC STRINGS

- Feynman diagrams of Bosonic String interactions



- Bosonic String Theory expansion is finite (one loop... really), no divergences...so perturbative Quantum Gravity looks renormalizable

SUPERSTRING THEORY

Bosonic String Theory is un-stable (tachyons)

It is possible to introduce a new String Theory such that for every Bosonic degree of freedom $X^m(t,s)$ there corresponds a Fermionic (anti-commuting) degree of freedom $\psi^m(t,s)$.

The theory does not have tachyons in its spectrum.

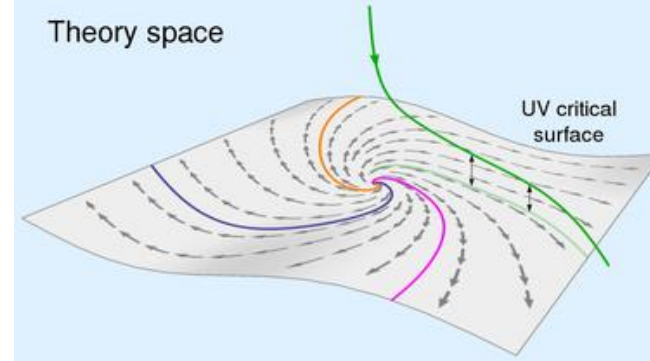
In order to be consistent, it needs ten (9+1) dimensions

There are five non-equivalent Superstring Theories

One of the important result in String Theory is that they reproduce Bekenstein-Hawking formula for Black-hole Entropy in the Quantum regime

ASYMPTOTIC SAFETY APPROACH TO QUANTUM GRAVITY

- The “Asymptotic safety approach to Quantum Gravity” is based on “Weinberg conjecture” (1979). He suggested to run the coupling constant as function of a cut-off. Find a Non Gaussian Fixed Point (NGFP) in this space of parameters, define the Quantum Theory of Gravity at this point.
- $d=2+\epsilon$: F. P. exists (Weinberg); $d=4$ NGFP in the Einstein-Hilbert truncation exists (Reuter and Sauressing 2002).
- There exist fundamental theories which are not perturbatively renormalizable (along the line of K. Wilson’s general principles of renormalization)
- They are constructed by performing the infinite-cut-off limit at a non-Gaussian fixed point ($u_* \neq 0$) (pert.theory: trivial (Gaussian) $u_* = 0$)



ASYMPTOTIC SAFETY APPROACH TO QUANTUM GRAVITY

The effective average action is used in modern Asymptotic Safety approach to Quantum Gravity.

The effective average action contains all momenta $p > k$ (=cut off) and not yet those momenta $p < k$.

The effective average action should provide the dependence by k of the fundamental constant.

The Einstein-Hilbert truncation is implemented.

CONCLUSIONS

- A well established theory of Quantum Gravity does not exist yet.
Lack of experimental tests
- We have analyzed some approaches to Quantum Gravity
 1. Loop Quantum Gravity (Mathematical problems)
 2. String Theory (no supersymmetry found..)
 3. Asymptotic Safety (quite young...evidence for the existence of the Non-Gaussian Fixed Point, no final proofs).
- More work appears needed to define a final theory of Quantum Gravity. This theory should reproduce all semi-classical results (e.g. Black Hole entropy) and it should have classical Einstein General Relativity as a limit when $\hbar \rightarrow 0$.